

Moxon



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Principatus Catholici

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Donatus de Moxon

The Catholique PLANISPHER:

Which Mr *Blagrove* calleth The
Mathematical Jewel;

Briefly and plainly discribed, in
Five Books.

The first shewing *The making of the Instrument.*

The rest shewing the manifold Use of it.

1. *For representing several Projections of the Sphere.*
2. *For resolving all Spherical Triangles.*
3. *For resolving all Problemes of the Sphere; Astro-
nomical, Astrological, and Geographical.*
4. *For making all sorts of Dials, both without Doors
and Within; upon any Walls, Cielings, or
Floores, be they never so Irregular, where-so-ever
the Direct or Reflected Beams of the Sun may
come.*

All which are to be done by this Instrument, with won-
drous Ease and Delight.

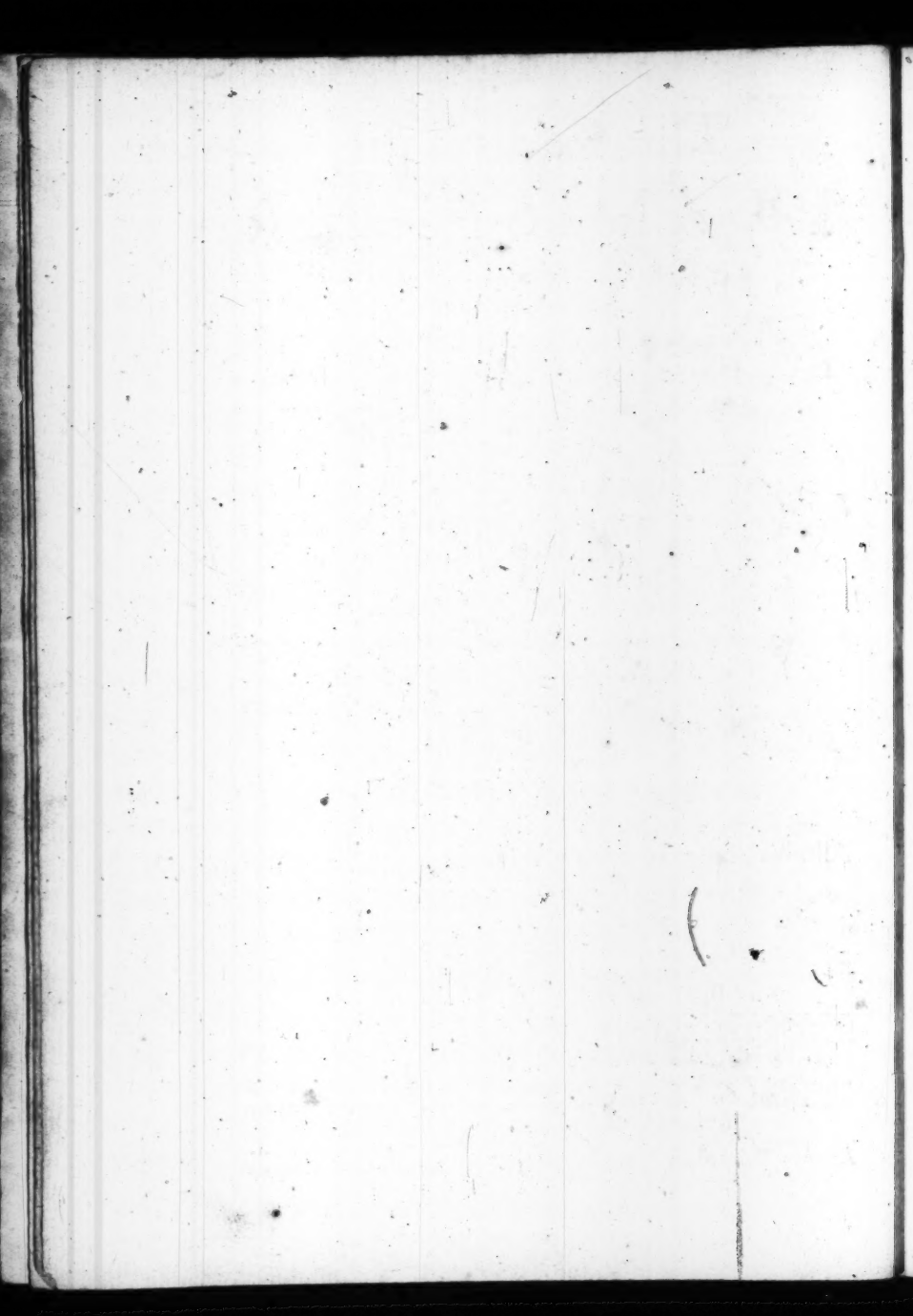
*A Treatise very usefull for Marriners, and for all Ingeni-
ous Men, who love the Arts Mathematical.*

By JOHN PALMER. M. A.

Hereunto is added a brief Description of the *CROSS-STAFF.*
And a Catalogue of *Eclipses*, Observed by the same I. P.

*The Heavens declare the Glory of God; and the Firmament sheweth his
Handi-work. Psal. 19.*

London, Printed by *Joseph Moxon*, and sold at his Shop on
Corn-hill, at the Signe of *Atlas*. 1658.





To my Honoured Friend,

JOHN TWYSDEN

Doctour of *Physick*.

Sir,

MAny Learned Men have complained that Mr. Blaggrave's Mathematical Jewel, (as he calls it) both the Instrument and the Book are rarely to be found. That the Book also by reason of the Interpolation of Gemma Frisius his precepts is longer then needed, and by reason of the Authors frequent interruptions by vexatious Suits in Law is somewhat confused; whereof himself complains in his Preface to the Reader, and in the Conclusion of the Fourth Book, and elsewhere, wishing an amendment. At your request especially I undertook the reformation of that Treatise, which now at length I have finished. Gemma Frisius was the first that brought this Instrument to some good perfection, calling it Astrolabium Catholicum, but he did that by a Cursor and Brachialum which Mr Blaggrave happily devised to perform by a Reet and Label, with more ease and delight. I have no designe to deprave the labours, or to obscure the Names or Fame of those ingenious Men, by whom this Instrument was contrived, and advanced to so great perfection; but as Mr Blaggrave said when he took upon him to reform Gemma Frisius his Treatise; so I say of my last Edition of the Instrument after both, Facile est Inventis addere. Surely if men deceased have any knowledge or regard to what is done after them in this

Epistle Dedicatory.

World, and could have communication with those that remain here, I suppose Mr Blagrave's Ghost would give me, thanks for doing that which he heartily wished to be done but for want of leasure left unfinished: and I should likewise thank him by whose means I became acquainted with this excellent Instrument: which, next to the Sphear or Globe it self, is the best Instrument, in my judgement, that ever was devised for Astronomy: and for the easier making and portableness, is to be preferred before the Sphear it self.

My aime hath been throughout this Treatise to Write Plainly, Methodically, and with as much brevity as might consist with perspicuity, remembring that of the Poet, Brevis esse laboro, Obscurus fio. How far I have attained my Intention, the Reader will judge. If this work shall be found usefull to the World, the thanks is due to you, who first ingaged me in it, and for the furtherance thereof took the pains to delineate the Instrument for me with your own hands, in Brass Plates of fifteen inches Diameter; which I esteem very highly, both for the exactness of the work, and for the work-man's sake, to whom for more then twenty Years past I am also many other wayes obliged. I confess I have been somewhat slow in performing my promise to you, because this Treatise hath taken up onely my spare hours, which by reason of infirm health, and more necessary employments, are not many.

Sir, I am

Your Servant.

Edon Apr. 1.
1658.

John Palmer.



The first book of the
Catholique Planisphear.
 Wherin

The whole Fabrick or making thereof is plainly Described.

CHAP. I.

*Of the parts of the Planisphear. And of the Mater,
 his matter and Lineaments.*

- T** His Planisphere is made up of five parts
- 1 The lying plate, called *Mater*.
 - 2 The moving plate; called the *Rete*, *Reet*, or *Net*.
 - 3 The *Ring* or *Limb*.
 - 4 The *Label*.
 - 5 The *Sights*.

The *Mater* is a round plate of metal or past-board flat, smooth, and stiff: the larger the better. And if you will have the circles actually drawn for every degree, it had need be ten Inches at least in Diameter. If it be made of metal (as Silver Brasse or Tin and Tin-glasse in equal quantity melted together) it must be well polished: but it may very well be made on a fair past-board, pasted on a Masse board: for thereon the Lineaments may be distinguished with inkes of several colours, which cannot be if it be made in metall.

The Lineaments of the *Mater* (though they be fitted to represent

present other circles of the Sphear also, as shall be shewed, yet) most aptly represent the Meridians and Parallels: and therefore so we call them here, while wee speak of the *Fabrique*. Among the Parallels the two Tropiques and the two Poles circles are to be inserted. And lastly to these you shall add the Ecliptique: and so you have all the Lineaments of the *Mater*.

For the Declination whereof,

1 Upon the center of the *Mater* plate, describe the fundamental circle, (about an inch within the edge, if your plate be 12 inches Diameter) that so a convenient space may be left for the Limb. This circle shall be the great Meridian passing through the Poles of the world, and also through the *Zenith* and *Nadir* of your Countrey; and is the bound by which all the Lineaments of the *Mater* are inclosed. Draw two Diameters crossing one another in the center at right angles, and dividing this Meridian into his quarters, let one of these Diameters be A B the Axtree-line, the other C D the Equator or his Diameter: divide also every quarter of this Meridian into 90 equal parts or degrees.

This Meridian onely of all the circles of the *Mater*, falleth out to be a full circle in this projection, because the bisection of the Sphear is supposed here to be made in the plain thereof, and because the eye is supposed to be the Pole thereof, and to equidistant from every part thereof. The rest of the Meridians and Parallels their Semicircles are in this *Planisphere* fore-shorned according to Optique reason, (as shall be further explained Ch 2) because they all either are great circles passing through the eye-point, and cutting the Meridian at Right angles, as the Axtree-line or East Meridian, the Equator, and the Ecliptique, which are therefore projected upon their Diameters and become straight lines; or else lie Oblique to the eye, as do all the rest of the Meridians and Parallels, which are all of them projected into arches less then a semicircle; and yet every one of them is to be accounted a semicircle fore-shorned, and to be divided as a semicircle into 180 degrees.

2 To describe the rest of the Meridians, you shall lay a Ruler from the Pole A to the several degrees of the semicircle C B D (or from the Pole B to the several degrees of the semicircle

cle C A D, for all comes to one) and mark where the Ruler intersects the Equinoctial line C D for every degree; so shall you have the Equinoctial divided into 180 deg. (*viz.* 90 deg. on one side the center, and 90 deg. on the other) through which divisions or degrees the severall Meridians shall pass, and all of them must meet in both the Poles. Therefore having three points given for every Meridian (*viz.* the two Poles A and B, and a middle point in the Equator C D, bring these three points into a circle, and you shall have the true arch of every Meridian drawn on the Planisphaer; as they appear in this Projection; which how to do shall be further shewed Chap. 3.

3 To describe the Parallels, you shall first divide the Axtree-line A B into 180 deg. (as you divide the Equator C D) by laying your Ruler from C or D to the severall degrees of the opposite Semicircle, and marking where the Ruler intersects the Axtree-line A B; or with your Compasses transfer the division of the Diameter C D to the Diameter A B; so shall you have three points given for every Parallel, whereby his arch may be drawn: as for example, the tenth Parallel North shall be drawn from the tenth degr. of the Quadrant D A, counted from D, by the tenth division of the Semidiameter E A, counted from E, to the tenth degr. of the Quadrant C A, counted from C; and so of the rest. The Tropiques and Poler circles are described as the Parallels. Yet of them see Chap. 6.

4 To describe the Ecliptick, number his greatest Declination (23 degr. 30. mi.) in the Meridian from C, towards A to F, and again from D toward B to G; then joyn the points F and G with a straight line which shall pass through the center of the *Mater* and be the Ecliptick. For dividing whereof you shall only transfer the division of the Axtree-line or Equator upon this Ecliptick line (for all Diameters have like divisions) and you shall distinguish every tenth and 30 degr. by longer stroaks, and shall set γ at G; γ and α at the center; β at F; and the rest in their order.

CHAP. II.

Of the reason of this Declination.

FOr the better understanding of the reason of this Declination, either take or suppose to your self an hollow Sphear or
B 2
Globe,

Globe, of equal diameter with your great Meridian before drawn. Cut this Sphear by the Meridian into two dishes or Hemisphaers, the one representing the Eastern, the other the Western Hemisphaer of the Heaven: So in each of these Hemisphaers the Meridian is an whole Circle, being the Base of the Hemisphaer, or brim of the dish: but the rest of the Meridians, the Parallels, Equinoctial, and Ecliptick, are all bisected by the great Meridian, and so you can have but half their circles in the Eastern Hemisphaer, and the other half is in the Western.

Next suppose also the plain *A C B D*, to be a thin plate of some transparent matter, as clear horn, glass, or cristall; and this plate fitted to stick in the dish mouth (that is, in the Meridian of the Hemisphaer) and upon the center *E* a straight wyre to be erected perpendicular to the plain *A C B D*, and the length of the said wyre to be equal to the semidiameter *E A*. Now place your eye at the top of this wyre, and look up the Lineaments of the Hemisphaer through the glass plate, and observe where the visual lines drawn from the severall points of the Hemisphaer to the eye cut the glass and what kind of lines and arches they do paint upon the glass and you shall see there that the semicircles of the Equator, the East Meridian, and the Ecliptick, will be depainted on the glass in straight lines; because they be great Circles, and pass through the eye-point of this projection) and the lines passing between your eye and the several degrees of any of them shall divide their Diameters upon the glass into such parts, as they are divided by the precept of the former Chapter. For the top of the wyre (here supposed to be the West point of the Horizon) is the true eye point from which the Diameters *A B* and *C D* are divided, and from which the whole projection of the Eastern Hemisphaer is made at one view upon the glass. But because this concave Hemisphaer with his wire or Axis erect, cannot easily be pictured on a flat, therefore to supply the want of a solid Scheme you may consider that the Axiree line *A B* is not onely the Diameter of the East Meridian, but a common Diameter to all the Meridians: and therefore if you take your ey point at *C* or *D*, and by your eye beam or a ruler laid from one of those points to all the degrees of the opposite semicircle, do divide the Axiree line, it shall be all one as if you had divided him from the top of the wire by the degrees of the East Meridian which passeth through the bottom of the concave Hemisphaer. For all great Circles

Circles of the Sphear and their Diameters likewise being equal, look how any one of their Diameters is divided, in like manner they shall all be divided, if the eye be alike situate to them.

CHAP. III.

*How to find the centers of the Meridians
five several wayes.*

THe centers of the Meridians and their semidiameters are thus found,

1. You have by the first Chap. three points given, by which they must be drawn (*viz.*) the two Poles, and a third point in the Equator) and how to bring these into a circle or arch, is shewed by *Euclid. 4. 9.* But I think this way incomedious for this purpose.

2 A better way is to get the centers by proffers, thus,

Let it be required to draw the twentieth Meridian whose points given are A 2 B. Having first extended infinitely the line C D, set one foot of your Compasses at adventure, in the line C D, whereabout you guess the center should be, and extending the other foot to A or B, carry it about at the same extent towards 2, and if it touch the point 2, you have taken the true center, and may draw the arch as is required, if your Compass over-reach, you must narrow it, and come nearer; if it reach short, widen your Compass, and seek your center further, till by tryal you light upon it: if one foot of your Compass stand in the line C D, and the other cut the middle point, and one of the extrem points A or B, it ought to cut the other also; if your plain be flat, and the line C D straight and square to the line A B: but if any of these have failed, you shall never bring the three points into an arch while the foot of your compass standeth in the line C D. Therefore in such case set one foot in A, and draw with the other foot a short arch crossing the line C D; then set the standing foot in B, and with the running foot cross the short arch last drawn: where these arches cross will be the center, by which you may draw an arch cutting A and B, and if it cut 2 also, you have your desire. But if this arch over reach 2, widen your Compass: if it

come short of 2 (the middle point) narrow your Compass, and try again in like manner till you can compass all the three points in the same arch.

3. A third way. I suppose you may know that every Meridian cuts the Equator twice, *viz.* in two opposite points distant 180 degr. one from another: as, for example, the Meridian which cutteth the Equator in 60 degr. of Right Ascension, cuts it again in the opposite degr. *viz.* 240. Now if you can find these two points in the Equator line C D, the center will be in the just middle betwixt them. One of these points is already given within the fundamental Circle; the other without, is thus found. Prolong your Equator infinitely beyond your plate both wayes, and divide the extension thereof by like reason as you divided his Diameter, *viz.* as by a Ruler laid from A to the severall deg. of the Quadrant B C, you divided the Semidiameter E C into 90 degr. so keeping still one end of your Ruler fixed at A, and carrying about the other end thereof to the severall degrees of the Quadrant C A, you may divide the excurrance of the line E C into 90 degr. more: and so E C and his excurrance or continuation will be half the Equator divided into his degr. and E D with his excurrance on the other side will be the other half divided by like reason. And thus the whole Equator is projected in one straight line, and divided into degr. also. Then having a point given within your fundamental circle through which the sixtieth Meridian must pass (*viz.* the 60 deg. of the Semidiameter E C or E D) number thence over the center to 180 deg. and there is the point where the other semicircle must cross, and the middle between those points is the center. But because the two points taken in the quadrant A C are very near together, especially towards A, and the Ruler also will cross the prolongation of the line E C very obliquely, you may therefore do better to divide this line into his degr. by a Scale of Tangents, for if upon the Equinoctial line D E C you prick down from E both wayes the Tangents of the half degr. in order from 0, to 90, those pricks shall be the whole degr. of the Equinoctial line in this Projection, to be numbred from E both wayes to 180 deg. where the Tangent becomes infinite. Thus taking A E for Radius, E D is the Tangent of 45 deg. by the structures: yet the arch or Diameter E D is a Quadrant or 90 deg. of the Equinoctial in this Projection, because the

the Tangents of the half deg. of the Quadrant E A I, measure out the whole degr. of the line E D, as was above-said.

4 If you consider well what hath been said, you will find (or you may take it here upon trust,) that for the 90 Meridians to be drawn between C and E, half the centers will be found in the opposite Semidiameter E D, and the other half without D in the said Semidiameter prolonged. And that every second division of the line E D from E toward D and forwards, shall be the centers of the Meridians which cut the Semidiameter C E. As for example, to draw every fifth Meridian from C to E, you take every tenth deg. from E toward D for the centers.

And further if you would not be at more trouble then needs, to divide the extension of the Diameter beyond the fundamental circle, you shall but do thus. Begin with the crookedest Meridians first, whose centers are within the fundamental Circle, and first pitching one foot of your Compass in the point 1, (near E) extend the other foot beyond the center to 2; there is the center from which you shall draw the first Meridian A 1 B: and also turning about your Compass you shall make a marke in the extension beyond D at 1, where the other Semicircle of this Meridian would cross the Equator. So for the next Meridian, in the line C E marked with 2, your center is beyond E at 4, and after you have drawn his arch A 2 B, marke with your compass his other crossing at 2 beyond D, and so with one labour you shall both draw the 45 crookeder Meridians, and also make the out lying division of the line E D prolonged: of which division every second or even number will be a center to some of the straighter Meridians. This is a very good and easie way: and this way Mr *Blagrove* alwaies used.

5 Or lastly. You may frame a decimal Scale of 1000 or 10000 parts, equal to the Semidiameter of the *Mater*; by which Scale with the help of the Cannon of Triangles, you may presently find the length of any S ne Tangent or Secant you shall desire. Now look what inclination any Meridian hath to your fundamental Circle (that is, what angle they make between them) the Secant of that inclination is the Semidiameter of that Meridian; and the Tangent of the same inclination is the distance of his center from E the center of the *Mater*. For example, the Meridian A 2 B his inclination is 20 deg. (for the angle C A 2 and likewise the arch C 2 which measures it is 20 degr. the S. cant of 20 degr is

10541.

10641. by the Cannon of Triangles (which every Mathematician ought to have at hand.) Take with your Compasses from your decimal Scale 10641. and setting one foot in A, with the other foot cross the Semidiameter E D; in that crossing is the center: or take with your Compasses 3639. the Tangent of 20 degr. and set it from E toward D, and it shall give you the same center at 4. For A E being Radius, E 4 is the Tangent, and A 4 the Secant of 20 deg. by the structure.

And if you like to work this way, it will help you much to have a short Cannon of Tangents and Secants of whole degr. of the Quadrant gathered into one page: which Cannon for your ease is here annexed.

A Table of Tangents and Secants to every degree of the Quadrant.

Degr.	Tan.	Secan.	gr.	Tan.	Secan.	Degr.	Tan.	Secan.
1	00174	010001	31	06008	011666	61	18040	020526
2	00349	010006	32	06248	011791	62	18807	021300
3	00524	010013	33	06494	011923	63	19626	022026
4	00699	010024	34	06745	012062	64	20503	022811
5	00874	010038	35	07002	012207	65	21445	023662
6	01051	010055	36	07265	012360	66	22460	024585
7	01227	010075	37	07535	012521	66-30	22998	025078
8	01405	010098	38	07812	012690	67	23558	025693
9	01583	010124	39	08097	012867	68	24750	026694
10	01763	010154	40	08390	013054	69	26050	027904
11	01943	010187	41	08692	013250	70	27474	029238
12	02125	010223	42	09004	013456	71	29042	030715
13	02308	010263	43	09325	013673	72	30776	032360
14	02493	010308	44	09656	013901	73	32708	034203
15	02679	010352	45	10000	014142	74	34874	036279
16	02867	010402	46	10355	014395	75	37320	038637
17	03057	010456	47	10723	014662	76	40107	041335
18	03249	010514	48	11106	014944	77	43314	044454
19	03443	010576	49	11503	015242	78	47046	048097
20	03639	010641	50	11917	015557	79	51445	052408
21	03838	010711	51	12348	015890	80	56712	057587
22	04040	010785	52	12799	016242	81	63137	063924
23	04244	010863	53	13270	016616	82	71153	071852
24	04452	010946	54	13763	017013	83	81445	082055
24-30	04663	011033	55	14281	017434	84	95143	095667
25	04877	011126	56	14825	017882	85	11430	114737
26	05095	011223	57	15398	018360	86	14300	143355
27	05317	011325	58	16003	018870	87	19081	191073
28	05543	011433	59	16643	019416	88	28636	286537
29	05773	011547	60	17320	020000	89	57289	572986
30						90		

CHAP. IIII.

To find the Centers of the Parallels, six several wayes.

THe first way, but the worst for our purpose, (as was said before for the Meridians) is by the fifth Proposition of the fourth book of *Euclid*; to find the Center of the Circle circumscribing the Triangle made by the three points given.

2 A better way is by profers. Take this upon trust: that as you found the Centers of all the Meridians in the Equator, so shall you find the Centers of all the Parallels in the Axtree line prolonged, and by making like profers as you were taught for the Centers of the Meridians, (Chap. 3.) you may quickly find the Centers of the Parallels.

3 A third way, You must consider that the Axtree line represents the East Meridian as well as the Axis of the world which is a common Diameter to all the Meridians. Also that every Parallel cuts the East Meridian (as it doth the rest) in two points Equidistant from the Equinoctial and two Equidistant also from the Poles. Therefore having one point already given in the Axtree line within the fundamental Circle where the Parallel shall cut, number the distance from this point to the next Pole, and number also the same distance again beyond the Pole in the Axtree-line prolonged, (being divided also as you were taught to divide the Equator line Chap. 3. and at the end of this number shall the Parallel cut the Axtree line again, And the middle between these two sections is the Center. For example, the 50th Parallel is 40 degr. distant from the Pole. Count therefore in the Axtree line prolonged 40 degr. beyond the Pole, and there is the utter end of this Parallel's Diameter; which if you part in two, the middle at G is the Center.

4 If from the point given, where the Parallel cuts the great Meridian, you raise a Tangent line, this Tangent shall cut the Axtree line in the Center of the Parallel. Example, The said 50th Parallel cuts the great Meridian at H, there I raise the Tangent H G perpendicular to the Radius E H. And this Tangent as you see cuts the Axtree line in G the Center of the Parallel.

5 Hence ariseth a fifth way. For it appears by this figure
C
that

that the Tangent of the Parallels distance from the Pole is equal to his Semidiameter: and that the Secant of his distance from the Pole is equal to the distance of his Center, from the Center of the great Meridian. For here EH is Radius, HB an arch of 40 degr. HG the Tangent thereof, and Semidiameter of the Parallel, EG the Secant thereof, and the distance of the Center of the Parallel from the Center of the Meridian. And all this is evident by the structure in the Scheme. Wherefore making EH Radius, take from your Scale or Sector, with your Compasses the Secant of the Parallels distance from the Pole, and set it from E in the Axtree line, and it shall end in the Center of the Parallel. Or take the Tangent of the Parallels distance from the Pole, and set it from the point of his Section with the Meridian toward the extension of the Axtree line, and where the end of it just toucheth the Axtree line, there is the Center.

6 For want of a Sector, or other fit Scales of Tangents and Secants you may do thus: Set one foot of your Compass in the Center E , and extend the other upon the Diameter of the Equator or Axtree line, to twice so many degr. as your Parallel is distant from the Pole. That distance is the very Tangent you seek. For example, for the 40th Parallel from the Pole, I number from E toward D 80 degr. to 8, now $E8$ is the Tangent of 40 degr. (though it contain just twice so many degr. of the Circle foreshortned in this projection, as hath been shewed Chap. 3. Sect. 3.) and so if you will have the Secant of 40 degr. take with your Compasses the length from 8 (where the Tangent ends) to A . and that is the Secant to be used as was taught in the last Section.

Thus have you wayes enough for finding the Centers of the Meridians and Parallels. And you may have occasion in the making of the Instrument to use most of them one time or other. However, the knowledge of them is both pleasant, and usefull for the right understanding of this and other Projections of the Sphear, as also for the examination of your work, when you shall chance to doubt of it.

CHAP.

CHAP. V,

*How to draw the straighter Meridians and Parallels,
whose Semidiameters are very long.*

IT may trouble you very much to draw those Meridians and Parallels, which lie near to the Diameters; because they be arches of great Circles, and require Compasses larger then you can well get, or manage when you have gotten them. Till you come to the 80th Meridian from the Limb, a Beam-compass of a yard long will reach, if your *Mater* be not above a foot Diameter, and a longer Beam you cannot well manage, for it will be apt to tremble with it's own weight, and draw double lines, though it be made very thick and massie. But the 89th Meridian will require a Beam-compass of almost ten yards long: For his Semidiameter will contain the Semidiameter of the great Meridian 57 times. Therefore to draw the 10 last Meridians and the 10 last Parallels, you may help your self one of these ways.

1. *Guido Ubaldus* hath devised an Instrument for this purpose, consisting of three rulers in form of an obtuse Triangle. The description and use thereof you may see in *Blagr. l. 4. c. 2. 3.* and in *Ubaldus* his book *De Theorica Astrolabij*. But though it be an Ingenious device, yet I have found by experience, that it is a ticklish Instrument, and hardly managed, for which reason I have hanged it by.

2 The Bow now commonly used, is an Instrument not so artificial, but more tractable and steddier then the former. It is made of too steel rulers, the shorter of them must be of good substance, as three quarters of an inch in height, and as much in breadth, that it may be stiff, and lie flat; the length must be somewhat more then the Diameter of your Instrument: The other may be an inch longer, of the same height but much narrower, that it may be bent out with screws into an arch of any Circle required; which ruler so bent, being laid to the three points given, you may by it draw the arch required, as easily as you draw a straight line by a straight ruler. The stiff ruler carries the screws, and it must have rivets, by which the bending ruler may be staid at both ends, while it is bent by the screws. See the figure.

CHAP. VI.

How to draw the Tropiques, and Polar Circles, and to finish the Mater.

BESIDES the 180 Parallels above mentioned, you have four more to draw before the *Mater* is finished, viz. the two *Tropiques*, and the two *Polar Circles*; of which the Northern is called the *Arctique*, and the other the *Antarctique* Circle. How to draw these you are sufficiently instructed Chap. 4. if you know but their Declination, for they be Parallels. The *Tropique* of *Cancer* declineth from the Equator toward the North Pole 23 degr. 30 min. and the *Tropique* of *Capricorn* declines as much toward the South Pole. The *Arctique* Circle declines Northward 66 degr. 30 min. and the *Antarctique* as much Southward. And these being drawn after the manner of the other Parallels, you have drawn all the lineaments of the *Mater*. And the better to adorn and distinguish them, you shall with your Graver hatch every fifteenth Meridian: for they are hour lines. The South arch of the great Meridian A C B, is the hour of Noon: and his North arch A D B, the hour of Midnight. These need not be hatched, being the Semicircles of the great Meridian, or fundamental Circle, which contains all but the Axtree line A E B, which is the hour line of the fixes, and the rest of the hour lines counted from him both waies, would be hatched on both sides, to shew like a ragged staff, for distinction sake. Also every fifth Meridian (not being a fifteenth) you shall make a pricked line, not punching it with a round point, lest you make your plate warp, but making many short strokes cross the line with your Graver, which will be more conspicuous. Every tenth Parallel also would be a ragged line, and the intermediate fiftths pricked lines: likewise the *Tropiques* and *Polar Circles* would be pricked lines. Also if your plate be large, you may set figures to the hour lines, and to every tenth Meridian at the Equator: but if your plate be small the divisions of the *Label* applied upon the Equator may supply the lack of them.

CHAP.

CHAP. VII.

Of the Reet, or Nets

HAVING shewed you what belongs to the Fabrique of the first part of this Instrument called the *Mater*: A few words more will instruct you how to make the *Reet*, whose lineaments are for the most part the same.

The *Reet* is a round plate of metal, or pastboard, like unto the *Mater*, but of less Diameter: it must be well planished and polished; and the thinner the better, if it hold working it would not be thicker then a shilling, being of a foot Diameter. It is called the *Reet* or *Kete*, that is the *Net*, because it must be pierced through, and made like unto a *Net* or *Letters*; that the lineaments of the *Mater* may be perceived through it. If we had a transparent metall, much labour might here be saved. A clear Lanthorn horn may serve for a small Instrument, but for large Instruments, it is best to have it either of fine pastboard, or, if you will go to the cost, of metal cancelled; as shall be taught.

1 For the delineation of the *Reet*, first draw your fundamental Circle equal to the fundamental Circle of the *Mater*, leaving a border or Limb without, of such breadth as may receive the graduations of the Circle, and figures set to them, which breadth may be three tenths of an inch, where the *Reet* is a foot in Diameter: draw likewise two Diameters A B, and C D, crossing one another in the Center E at right Angles, and dividing the Circle into his four Quadrants, which you shall subdivide again into 90 degr. apeece, as you did in the *Mater*.

2 You shall inscribe two arches, which shall represent the Semicircles of the *Ecliptique*, which shall meet at the points C and D of the Equator, and the middle points of these arches shall be found in the Diameter A B, thus. The Diameter A B being divided as before you were taught to divide the Diameters of the *Mater*, number from A toward the center E 23 degr. 30 min. and there make the point F, for φ : and likewise number from B toward E 23 degr. 30 min. and there set the point K, for \odot . then join the points C F D in one arch, and the points C K D in another arch (as is taught Chap. 3) and your *Ecliptique* is drawn. But now you must make him a narrow Limb inward toward the

C 3

C center,

Center, to receive the scale of his degr. and the characters of the Signes. And to divide him you shall do thus, Number in the Axtree line (A B, from F inwards 90 degr. there is the Pole of the arch C F D, to this Pole fasten one end of your ruler (having an ey-lid-hole in the edge for that purpose) and carrying about the other end over the several degr. of the Semicircle C A D, you shall cut the arch C F D into his correspondent degrees. As if you lay the ruler from C to 10 degr. in the *Limb* toward A, it shall cut the *Ecliptique* in ≈ 10 , and so of the rest. Likewise for the other Semicircle C K D, find his Pole 90 degr. from K toward F and A: and from that Pole by like reason, you shall divide the Semicircle C K D by the divisions of the Semicircle C B D. This is the best way.

Or you way divide the *Ecliptique* by a Table of Right Ascensions, thus. Lay your ruler from the Center E to 27 deg. 54 min. in the *Limb*, which is the Right Ascension of ≈ 0 . to be counted from D towards B, and the ruler shall at the same time cut the *Ecliptique* in ≈ 0 , to which that Right Ascension belongs, and so for any other deg. or you may defer the dividing of the *Ecliptique*, till you have finished and cut out the *Reet*: and then if you set the line C D of the *Reet*, in A B the Axtree line of the *Mater*, the *Ecliptique* will lie among the Meridians of the *Mater*, and shall be so divided by the Parallels of the *Mater*, as the Meridians are divided by them. But my advice is that you divide your *Ecliptique* the first way, and you may use this for proof of your work at last.

3 The rest of the lineaments of the *Reet* are the *Azimuths*, to be drawn as the Meridians of the *Mater*, and the *Almicanters*, to be drawn as the Parallels. Onely you shall need to draw but half the *Almicanters*, and the *Azimuths* but half way, leaving one half of your *Reet* viz. E C B D blank and void of them.

In drawing these *Azimuths* and *Almicanters* you shall be carefull to skip over the border of the *Ecliptique*, leaving it fair, that the graduations thereof with their figures set to every tenth degr. and the characters of the Signes may be more distinctly seen. Also you shall do well, if you make a border to the Axtree line on the Northside, that is toward D, and let this border be of the same breadth from A to B, the breadth not exceeding one fifth of an inch in a *Reet* of a foot Diameter; upon which border you may make a scale of degrees, setting figures in it to every tenth

Almi-

Almicanter. This will be a great strength and Ornament to your *Reet*.

Below the Horizon *CD* likewise, you shall make a *Limb* or border for the Horizon, to receive his graduations: this may be a quarter or three tenths of an inch broad, where the *Reet* is a foot in Diameter: and upon this border you shall set figures at every tenth *Azimuths*, and shall number them both wayes, from the Center and from the Meridian.

4 You shall inscribe so many of the fixed Stars as your *Reet* may well receive. Which to do you must know their Right Ascensions (or Culminations) and also their Declinations, for which purpose I have given you a Table of 110 of the more notable fixed Stars, (which may best be inserted in your *Reet*,) with their Right Ascensions and Declinations calculated to the year of our Lord 1671. which may serve for 40 years before and after without any considerable error.

To inscribe them you shall first number the Right Ascension of the Star from γ 0, that is from *D* upon the *Limb* of the *Reet* toward *B*, and at the end of that number fix your *Label*, (which by this time should be made and pinned on the Center,) then from the *Limb* count inwards upon the *Label* the Stars Declination, and at the end of that number make a prick in your *Reet* close to the edge of the *Label*, there is the Stars place. Then with your Graver you shall make there the shape of a Star, with 4, 5, or 6 points, according as the magnitude of the Star deserves: and let one point be longer then the rest; and let it point outward from the Center, if the Stars Declination be North, but inward toward the Center, if his Declination be South: and let the end of his long point (called *Apex*) be in the very true place of the Star. But if your *Label* be yet unmade, then take the measure of the Stars Declination with your Compasses upon any of the four Semidiameters of the *Reet*, (measuring it from the *Limb* inwards,) then lay a ruler from the Center to the Right Ascension of the Star and where the ruler cuts the *Limb* of the *Reet*; there set one foot of your Compasses, (opened as before) and with the other make a prick toward the Center, close to the edge of your ruler, and there is the Stars place in your *Reet*.

5 Lastly, you shall cut out all the spaces of this *Reet*, which may be spared; remembering alwaies that you leave uncut the borders of the *Ecliptique*, Horizon, and *Axuree* line, and be very care-

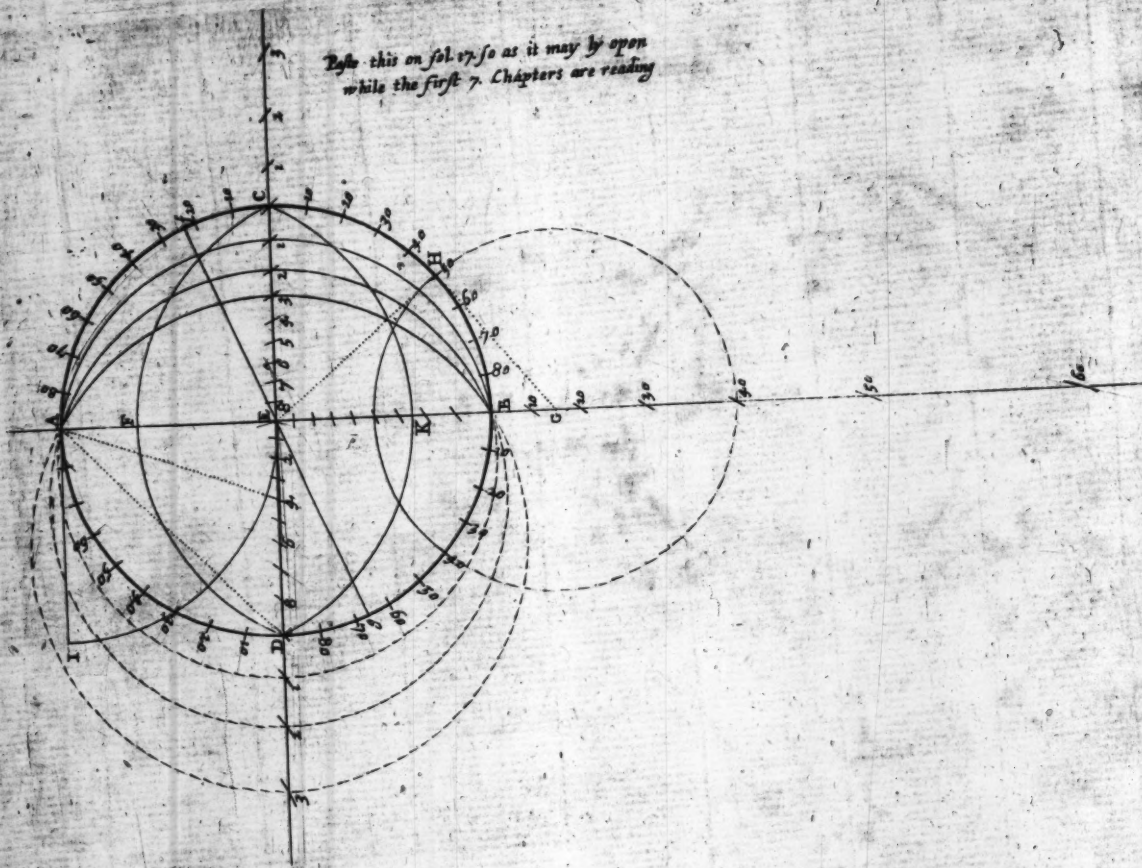
carefull that you cut not into the Center of your *Reet*, but leave breadth sufficient about the Center to hold the Center-pin, which must joyn *Mater Reet* and *Label* together. This remembred, you shall cut out two third parts of the spaces of the *Almicanters*, beginning from the Horizon *CD*, and cutting out the breadth of two degrees, after which you shall leave the breadth of one degree; and then cut out again the breadth of two degrees, and so forward. But for the greater strength and ornament of your *Reet*, and for ease in numbring the *Azimuths*, you shall at every 15th *Azimuth* leave a string of the breadth of one degree, whole from the Horizon to the Pole *A*, or at every thirtieth *Azimuth* leave such a string going quite through, and at every other fifteenth the string may be cut off when it comes within ten degr. of the Pole, because there the spaces of the *Azimuths* be very narrow and close together.

And where among those *Almicanters* and *Azimuths* you have any Star, you must contrive to leave him standing, and to set by him his name or some figure by which you may know him again. But you are to content your self with four Stars on this side the Horizon, because you will want convenient room. On the other side you may have more, and room also to writ their names upon strings or branches left for that purpose; which you may contrive into some voluntary letters-work, wherein you shall not much regard uniformity of the Quadrants, but to make the *Reet* as open as you can, provided you leave it of sufficient strength.

The cutting of this *Network* requires much labour and care, be sure you use no Punches nor Chisels, nor adventure to stamp your figures, lest you spoile all. But get your Gravers, Drills and Files, of several bignesses and fashions. and being to cut out any of the letters, lay your plate upon a flat board, or contrive to pinch it between two flat boards, as in a Vice, that it crumple not. The lower board were best have a small Auger hole, through which your Files may play: the upper board must come close to your work behind, but must not cover it. Then first make way for your Drill with a Graver: next with your Drill (set Perpendicular to the plate) bore two or three holes close together, then get in a small File, and file them all into one mortise or narrow window, to make way for bigger Files, and when you come near the line be sure your File be not slope but Perpendicular to the plate in working. And to guide your Files Perpendicular in
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2^{de} this on fol. 17. so as it may be open
 while the first 7. Chapters are reading



working you may make a long handle to your File, like an arrow shaft, and longer if you will: fasten a board with an hole besitting the handle of your File just over your work; put the shaft or handle of your File through that hole so far that it slip not out in working: and this hole shall so govern your File, that if you set it Perpendicular at first it must needs file Perpendicularly. This device I learnt from an excellent Artificer, M. *Matthew Hill*, of *Bedford*; who by this and such other ingenious devices did cut out two of these *Reets* so exactly and truely, as I think the like hath not been done in metall before.

To cut out the *Reet* in pastbord is much easier, if you be provided of sharp knives and chesills, fitted for your purpose.

A Table of the Right Ascensions and Declinations of 110 of the more notable fixed Stars; calculated from Tycho his Tables: rectified for the year of our Lord 1671.

	A. mi.	D. mi.	
Andromeda her Head,	357. 54.	27. 18. N.	2.
(Mirach) Girdle.	12. 49.	33. 55. N.	2.
Foot (Alamath)	25. 57.	40. 44. N.	2.
Perseus his side, Algenib.	44. 16.	48. 36. N.	2.
Mendusaes head, Algol.	41. 46.	39. 39. N.	3.
Henerichus right shoulder.	85. 53.	44. 56. N.	2.
Left shoulder, Alhaiot.	73. 07.	45. 37. N.	1.
Left elbow.	69. 29.	43. 15. N.	4.
The Kids.	69. 57.	40. 33. N.	4.
	70. 51.	40. 42. N.	4.
	160. 18.	58. 08. N.	2.
The great Wain.	160. 48.	63. 32. N.	2.
The Wheels.	173. 59.	55. 33. N.	2.
	179. 48.	58. 51. N.	2.
	189. 53.	57. 47. N.	2.
The Horses.	197. 37.	56. 41. N.	2.
	203. 37.	51. 00. N.	2.
The little rain, the Pole Star.	07. 53.	87. 34. N.	2.
Last wheel.	231. 14.	73. 15. N.	3.
Dragons tongue.	254. 36.	54. 55. N.	4.
		Head	

	Al.	mi.	D.	mi.	
<i>Head</i> { <i>first,</i>	260.	46.	52.	34.	N. 3.
{ <i>last, Ras Aben.</i>	267.	15.	51.	36.	N. 3.
<i>Tail</i>	167.	15.	71.	05.	N. 3.
<i>Bootes Arcturus.</i>	210.	13.	20.	58.	N. 1.
<i>Engonast's Head,</i>	254.	12.	14.	50.	N. 3.
<i>Ophiucus Head.</i>	259.	55.	12.	52.	N. 3.
<i>Lyra,</i>	276.	27.	38.	30.	N. 1.
<i>In Ariadnes brow, (Mumir)</i>	230.	12.	27.	51.	N. 2.
<i>The Swans bill,</i>	289.	23.	27.	18.	N. 3.
<i>The Eagles Heart,</i>	293.	41.	08.	03.	N. 2.
<i>Tail,</i>	282.	36.	13.	25.	N. 3.
<i>The Dolphins tail,</i>	304.	24.	10.	14.	N. 3.
<i>Pegasus his mouth, (Eniph)</i>	322.	03.	8.	24.	N. 3.
<i>Head,</i>	328.	24.	4.	38.	N. 4.
<i>Neck,</i>	336.	21.	9.	08.	N. 3.
<i>Right shoulder (Sheat.)</i>	341.	59.	26.	18.	N. 2.
<i>First in the wing, (Marcab)</i>	342.	07.	13.	28.	N. 2.
<i>Last in the wing.</i>	359.	08.	13.	22.	N. 2.
<i>The Rams head,</i>	27.	12.	21.	54.	N. 3.
<i>Horn,</i>	23.	54.	17.	40.	N. 4.
	24.	08.	19.	12.	N. 4.
<i>The Bulls North eye,</i>	62.	23.	18.	26.	N. 3.
<i>South eye, (Aldebaran)</i>	64.	17.	15.	48.	N. 1.
<i>Brightest of the Pleiades,</i>	52.	00.	23.	03.	N. 3.
<i>Gemini. Head of Apollo,</i>	108.	24.	32.	33.	N. 2.
<i>Head of Hercules,</i>	111.	19.	28.	46.	N. 2.
<i>The first foot,</i>	88.	48.	22.	33.	N. 4.
	90.	48.	22.	38.	N. 3.
<i>The third foot,</i>	94.	41.	16.	38.	N. 2.
<i>Cancer, Przepe,</i>	125.	22.	20.	48.	N. ne
<i>Leo, the Lions neck,</i>	150.	26.	21.	29.	N. 2.
<i>Heart, (Regulus,</i>	147.	43.	13.	33.	N. 1.
<i>Back,</i>	164.	08.	22.	20.	N. 2.
<i>Tail,</i>	173.	04.	16.	25.	N. 1.
<i>Virgo, Spica m., Azimech,</i>	196.	56.	9.	31.	S. 1.
<i>Libra, South ballance,</i>	218.	13.	14.	37.	S. 2.
<i>North ballance,</i>	224.	52.	8.	07.	S. 3.
<i>Scorpio, in his forehead the lowest,</i>	234.	50.	25.	06.	S. 3.
<i>Midst,</i>	235.	15.	21.	38.	S. 3.
					Highest

	Al.	mi.	D. mi.	
Highest,	236.	36.	18. 51. S.	3.
Heart, (Antares,)	242.	23.	25. 37. S.	1.
Sagittaries head, the midst,	281.	18.	22. 07. S.	4.
Capricorns horn, the highest,	299.	58.	13. 29. S.	3.
Tayl,	320.	29.	18. 02. S.	3.
	322.	15.	17. 32. S.	3.
Aquarius right shoulder,	327.	16.	1. 52. S.	3.
left shoulder,	318.	07.	6. 56 ¹ . S.	3.
Right leg, (Scheat,)	339.	22.	17. 31. S.	3.
End of the flood (Fomahaant,)	339.	46.	31. 17. S.	1.
The Whale, Mandibula,	41.	21.	2. 48. N.	2.
Mouth, the midst,	36.	36.	1. 50. N.	3.
Cheek,	35.	44.	1. 07. S.	3.
Belly, (Baren Kaitos)	23.	52.	11. 54. S.	3.
Tayl, (Northern,	0.	43.	10. 37. S.	3.
Southern	6.	45.	19. 48. S.	2.
Orion. Right shoulder, Bedalgieure	84.	23.	07. 18. N.	1.
Left shoulder Bellatrix,	76.	54.	06. 01. N.	2.
Girdle the first,	78.	52.	0. 35. S.	2.
Second,	79.	55.	1. 26. S.	2.
Third,	81.	04.	2. 09. S.	2.
Left foot, (Rigel)	74.	44.	8. 37. S.	1.
Right foot,	83.	03.	9. 49. S.	3.
The great Dogs month, Alhaber, Sirius,	97.	42.	16. 14 ¹ . S.	1.
Formost foot,	92.	08.	17. 49. S.	2.
The little dogs neck,	107.	22.	8. 54. N.	3.
Thigh, Procyon,	110.	34.	6. 03. N.	2.
Hydra, the heart, (Alphard)	137.	54.	7. 15. S.	2.
Corvus, in his beak, the first of the □,	177.	50.	22. 54. S.	4.
Second of the □,	179.	49.	15. 39. S.	3.
Third of the □,	183.	16.	14. 39. S.	3.
Fourth □,	184.	20.	21. 33. S.	3.

CHAP. VIII.

Of the Ring, or Limb of the Mater.

THe third part of this Instrument is the *Ring* or *Limb*, which is nothing else but the skirt of a Circular plate equal with the *Mater*, whose middle is cut out by a lesser concentric Circle. It is bounded with two Parallel Circles, the outmost must touch the edge of the *Mater* round the inner Circle or edge of this *Ring*: it must be a little less then the *Limb* of the *Reet*, that it may take hold of the *Reet* to keep it flat and safe from harms. This *Ring* had need be thicker then the *Reet*, but not so thick as the *Mater*; and for breadth, about $\frac{1}{2}$ part of the Diameter. It must be pinned or screwed on to the *Mater* with 6 or 8 pinnes or screws, that so you may take your plates asunder when need is to cleanse them from any stain or dust that may get between. Let the pins that carry the naile-screws be rivetted in the *Ring*, and thir heads so filed down and polished, that they be not seen to check the *Label*; and holes being made in the *Mater* for the pins to pass through, you shall have smal screws of what fashion you like best, to turn upon them on the backside; these screws would be made all of a length, and may serve as feet to bare up the Instrument about a third part of an inch from the ground, that it be not scratched and be readier to take up.

And that the *Reet* may turn more pleasantly under the *Ring*, and lie as near as may be in the same plain with the *Ring*, you shall abate half the thickneis of the upper edge of the *Reet*, about a barley-corn's breadth round about, so far as he shall run under the *Ring*: and likewise abate half the thickneis of the inner edge of the *Ring* on the lower side where he claps down the *Reet*, (which a good Turner knowes now to do;) or you may make a shift to do it with a beam-compass, if you make your running point like a narrow chesill.

Your *Ring* thus fitted to the *Mater*, you shall set one foot of your Compasses in the Center of the *Mater*: and with the other draw near the inner edge of the *Limb* a Circle about $\frac{3}{4}$ of an inch distant from the edge. Also opening your Compasses about $\frac{1}{2}$ of an inch more you shall draw another Parallel Circle: and
laying

laying your Ruler or *Label* from the Center to the several degrees of the fundamental Circle of the *Maser*, you shall draw short lines for every degree from the inner edge of the *Ring* to the first Circle, and every tenth degree you shall prolong to the second Circle, and let every fifth be drawn half way. Between these two Circles also you shall set figures to every tenth degree; numbring from the Equinoctial line *CD* to the Poles on both sides both wayes. Also without the second Circle you shall set great figures for the several Hours, setting *XII* at *C*, and thence proceeding in order to the right hand toward *B*, at 15 degrees set *I*. at 30 degr. set *II*, at 45 degr. set *III*, and so on, till you come to *D*, where you must set *XII*. Thence you shall proceed in the other Semicircle *DAC*, setting *I*, *II*, *III*, and so on in order, till you be come round. And remember that you write on the *Ring*, at *A* *Oriens*, at *C* *Meridies*: at *B* *Occidens*, and at *D* *Septentrio*,

CHAP. IX.

Of the Ephemeris or Calender, on the Ring.

IF there be space enough left upon the *Ring* without the Circles of the degrees and Hours, you may fill it up with the *Ephemeris* of the Sun in this manner:

The former Scale on the inner edge of the *Ring* shall serve you to this purpose for an *Ecliptique*; and you may set to him the Characters of the Signes, if you will, at every thirtieth degree; beginning at *Oriens* and there setting γ , and \odot at *Meridies*, and the rest in like order.

Then draw another Scale without this, upon the *Ring*, consisting of two spaces. In the inner space shall be the *Dayes* of the Year: in the outer space (which must be a little larger) shall be the *Names* of the months in their order,

And to divide this Scale rightly, you shall do thus. Go to some *Ephemeris* for the Leap Year that next comes, viz. 1660, (or rather for some Leap Year about 20 Years hence, that your Scale may serve without any *Prosthapheresis*, for 40 Years to come without sensible error, and beginning your year with *March*, look where the Sun was on the 29 of *February* at Noon; which you shall find to be \times 20 degr. 47 min. for the Year 1660. Therefore laying the *Label* or a Ruler from the center to \times 20 degr.

D 3.

47 min.

47 min. in the inner Scale, strike a long stroke through your outward Scale, and from thence begin your Year, writing from thence toward the right hand *March 1660*. Then lay the *Label* to \times 21 degr. 47 min. (which is the Suns place on the first day of *March* at noon the same year) and where it cuts the outer Scale, mark the first day of *March*, and so the rest in order. And to the first day of every moneth, you shall set his proper Letter which belongs to him in the *Calender*; as to the first of *March* you shall set *D*, and to the first of *April* *G*, &c. and when you have done *December*, you must take the Suns place for *January* and *February* out of the next years *Ephemeris*, viz. 1661, and note that the space for the last day of the year (*Febr. 28*) will fall out to be less by a fourth part then the rest, by reason that the Sun wants almost 6 hours to finish his Circle, which he finishes in dayes 365, 5 hours 48 minutes. And for this cause these Scales will serve you to find the Suns place at noon, for any day in a like year, that is every fourth year, accounted hence, either backwards or forwards; which year shall evermore be accounted to begin from *Febr. 29*, and may be accounted the first year after Leap year, because the Intercalation was *February 25* next before. Then for the year next following, viz. 1661, (beginning *March 1* and being second from the *Bissextile* or Leap year) these Scales shall give you the place of the Sun at six hours after noon, and the third year from *Bissextile* 1662 (beginning as before *March 1*) these Scales shall give you the Suns place 12 hours after noon, or the midnight following. And the fourth year 1663 being *Bissextile*, these Scales shew the place of the Sun at 18 hours after noon, the next year 1664, being the first after *Bissextile*, and beginning (as aforesaid) *March 1*, is the very same year for which your Scale is made and gon, for that year: your Scale shewes the Suns place at noon again.

But because the *Julian* years are bigger then the true Solar years by almost 12 mi. of time (that is, near a quarter of an hour) in which time the Sun moves 27 sec. 13 thirds 37 fourths, therefore when you have found the Suns place by the former Scale, any year after 1660, look how many years are passed since 1660 and so many times you must add 27 sec. 13 thirds 37 fourths, (that is almost half a minute) to the Suns place found: and for years past you must subtract as much, that you may find the Suns place exactly. This *Prosthapheresis* in 2 or 3 years is scarce considerable

in an Instrument, but in 10 years there will be 4. minutes 32. seconds, and in 20 years 9. minutes 5. seconds, to be added after 1660. and as much to be subtracted in like number of years preceding the year 1660. to which this Scale is supposed to be framed.

This *Ephemeris* or *Calender* M. *Blagrove* would have on the back-side, where hee would also have a *Ruler* with *Sights*, to take the *Altitude* of the *Sun* or *Stars*. But this will be found incommodious in many respects, both in the framing, and in the using; and therefore I advise that nothing be set on the back-side but the *Tables* of the *Prime*, *Epaſt*, and *Cycle* of the *Sun*, thereby to find the age of the *Moon*, her *Conjunctions* and *Oppositions*, and the *moveable Feaſts* for ever, Of which see *Chap. 11.*

CHAP. X.

Of the Label and Sights.

THe *Label* is a *Ruler* slit in the midst, and the half of it cut away to the Head, where it is pinned to turn upon the Center, and reaching to the outside of the Limb.

The *Fiducial* edge thereof, which pointeth upon the Center, must be graduated, like to the *semidiameters* of the *Maver* and *Reet*, into 90 degrees, to be numbred either inward or outward. The fashion of it may be understood by the figure without more words.

To this *Label* you may fit *Sights*, either fixed or moveable, as you like best, for observing *Altitudes* and *Azimuths*: but for taking *Azimuths* you had need have one tall Sight, at least half as long as the *Label*: and then it had need be moveable, to take off at pleasure.

For taking the *Altitude* of the *Sun*, I have made a pair of moveable *Sights*, to slip up and down upon the edge of the *Planisphear*; having on the backside springing plates of brass to pinch them close, and make them stick where you set them. These are commonly to be set at C and D the ends of the *Equinoctial* line. At A in the *Limb* and in the Circle next unto the inner edge which boundeth the strokes of the severall degrees, you shall drill a small hole, through which you may put
a thred

a thred to hang a plummet on. The Sun then shining through the Sights placed at C and D, the plumb-line shall shew his Altitude in the semicircle B C A, you beginning to number from B, and observing where the plumb-line crosseth the Circle in which the hole for hanging the plumb-line was made. And here you must remember that because the plumb-line falleth not from the Center of the *Planisphear*, but from a point in the circumference about A, therefore the space of two degrees must be taken but one degree, so that if the Plumb-line fall 20 degr. below B toward C, the Suns *Altitude* is 10, degrees as you may see demonstrated, *Euclid*. 3. 20. and *Pitisc. Trigonem.* 1. 53. And thus you may observe the Suns *Altitude* neer the Horizon, as exactly as by a *Quadrant*, whose semidiameter were equal to the diameter of your *Planisphear*. But if the *Altitude* exceed 30 or 40. degrees then will the Plumb-line cut the limb too slope and have too much play to your trouble : For remedy whereof you shall remove the Sight at D towards A some degrees : as for example 60 degrees, by which means you shall abate the Suns *Altitude* 30 degrees, which 30 degrees must be added to the *Altitude* observed: as for example, the Sights are placed one at C, the other 60 degrees above D toward A, and the Plumb-line cuts 10 degrees from B towards C, I say, then is the Sun 5 degrees high and 30 degrees more, in all 35 degrees: in like manner you may place the Sight at any other number of degrees, from D toward A, as you shall find most convenient for the present *Altitude*; remembring always that how many degrees soever you remove the Sight, half so many are to be added to the *Altitude* found. But if your *Reet* happen to run so far under the *Limb*, that you cannot make a center-hole for the Plumber through the *Limb* and *Mater*, without hindring the *Reets* motion, then may you have a small plate of sheet brass, in fashion of an Arm or Tongue, in the point whereof you shall have a Center-hole drilled, and this plate shall be so joyned with a sluice or screw about the *Limb* near A, that the Center-hole made in this plate may lie close to the point where the Center should have been boared in the *Limb* in the line A B: and thus you may put it on, and take it off, at pleasure, that it hinder not the motion of the *Reet* or *Label*. Of the fashion of the Sights see more Booke 4. 2.

CHAP. XI.

Of the perpetual Calender, on the back-side.

ON the back-side of your *Planisphear* you may set the *Calender* following, which consisteth of three *Tables* gathered round. The longest would be set outermost. The first is the *Table of the Cycle of the Sun*, that is of the *Sundays Letter*. This is here placed in the middle. It is a *Cycle* of 28. years, in which time the *Dominical Letter* runs all his changes, (caused by the one odd day above 52 weeks) in every *Common year*, and two odd days which run over the even weeks in the *Leap years*. To find the beginning of this *Cycle*, add to the year of our *Lord* 9. (because the first year of our *Lord*, as we commonly account, was the 10 of this *Cycle*) and divide the sum by 28. the remainder is the year of the *Cycle* running; and if nothing remain, then it is the 28. or last year. So you shall find that the *Cycle* now running shall end with the *Julian year* 1671. as in the *Table*; and shall begin again with the year of our *Lord* 1672. Thus may you renew the *Table* when it is expired; or make this very *Table* serve you for ever.

Example.

Enter this *Table* with the year of our *Lord* 1656. now running; and you shall find over against this year in the next space inwards 13. shewing you that it is the 13 year of the *Suns Cycle*; (so shall the 28 year forward viz. 1684 be again the 13th year of the *Cycle* next coming.)

In the next space within, you have the *Dominical Letters* F and E, (because it is *Leap year*) F shall be the *Dominical Letter* till you come past the *Intercalary day*, which is the day following the 24th of *February*: and for the rest of this year the *Dominical Letter* shall be E; (for the *Letters* always change backwards) also you shall note here that the day inserted in every 4th year is not *February* 29, but *February* 25. for *February* 24, (being 6 Cal. *Martij*) is repeated again in the *Leap year*: and they write again *February* 25. 6 Cal. *Martij*: and the 25th of *February* in the *Leap year* is marked with the same letter F,

E

wherewith

wherewith the 24th of *February* hapneth always to be marked. Hence the *Leap year* is called *Annus Bissextilis*: and note that by the *Eclesiasticall Law* *S. Marthias day*, which is *February* 24th in common years, in the *Bissextile* years is to be observed on *February* 25. Nevertheless in our *Secular Law* not the 24th and 25th of *February*. but the 28th and 29th in the *Leap year* are ordained to be one day in the account of Law: as by *Statutum de Anno Bissextili*, made in 21 year *Henry* 3. may appear.

The second Table is of the *Cycle of the Moon*, consisting of the *Prime* or *Golden Number*, and the *Epaet*. This Table contains 19 years, which is the *Annus Metonicus*: in which space of time *Meton* an *Astronomer* about 430 years before *Christ*, observed the *Moon* to finish all her variations. So that every 19 year the mean conjunctions or changes should happen upon the same days of the moneth, that they did happen upon 19 years before; onely an hour and half sooner. Yet because every 19 years contain not the same number of *Leap years*, but sometime there come five *Leap years* in 19 years, and sometimes but four, therefore there may happen in this Period of *Meton* an error of an whole day, besides the hour and half above mentioned. For remedy whereof *Calippus*, about the 330 year before *Christ*, devised to quadruple this period of *Meton*, making *Periodus Calippica* of 76 years, which contains just 19 quaternions of years; so containing always the same number of *Leap years* and days. This period is therefore more perfect then *Metons*: for after this period of 76 years, the *Moon* runneth over the same course for her conjunctions and oppositions; changing in the same year of the period always, upon the same day of the moneth, save onely that shee changeth sooner by six hours in the latter period then in the former.

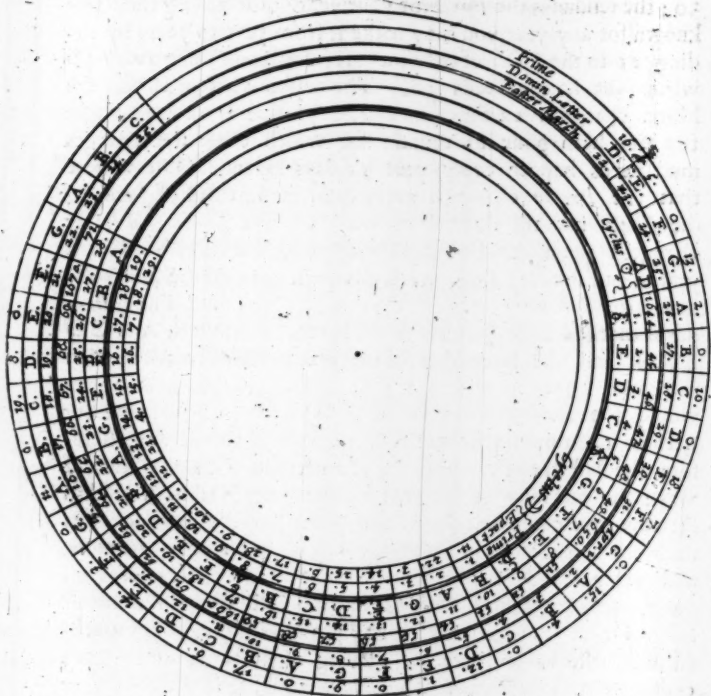
But the Church still retaineth the period of *Meton*, called the *Prime*, or *Golden number*; because it used to be set in *Golden letters* in the *Kalender*, in a certain artificiall order throughout every moneth, to guide you to the day of the Moons *Priming* or *Changing*: so may you find it in red letters, thus, Set to the *Kalender* printed in large folio with the *Book of common Prayer*, in the time of the late *Queen Elizabeth*. To find the year of the *Prime*, add to the year of our Lord 1, and divide the sum by 19. the remainder is the year of the *Prime*, or if nothing remain it is the 19th or last year. Thus you may find the present year

year 1656, to be the fourth year of the *Prime*, and so you find it in the Table. The *Cycle* or *Period* now running, ends with 1671. and begins again with the year following.

The *Epaet* or *Concurrent* is set against the *Prime* in the next space inwards: and finisheth his *Cycle* in the same time. It was devised to find more readily the day of the change, and age of the Moon. The way to find it is this. Multiply the *Golden number* serving for your year by 11, and divide the product by 30; the residue is the *Epaet* for your year. Or having the *Epaet* known for any year, you may make it from year to year, by adding 11 to the *Epaet* of the year foregoing, and casting away 30 when the sum exceeds 30. The reason whereof is, that the Moon changeth 12 times in 354. days, that is 11 days before the Sun hath gone his round: for which cause the changes must needs happen every year 11 days sooner. Observe here that the *Prime* changeth every year the first day of *January*; the *Epaet* not till the first of *March*. The *Dominical letter* changeth upon the first of *January* going one letter backward yearly; and in every *Leap year* it changeth again on the Lords day next after *February 24*. The reason whereof is this: The *Calendar* is marked throughout with the letters of the week A B C D E F G, and the same day of the year is always marked with the same letter, now if the year contained even weeks then would the *Dominical letter* be always one and the same: but because a common year contains 52 weeks and one day, therefore the last day of the year must be marked with A, as the first was; the first day of the year following again is marked with A: now put case the last of *December* marked A, be *Sunday* in the year 1654. the day following viz. *January 1*, is *Munday*, and yet marked A; and the first *Sunday* in 1655 must needs fall on *January 7* marked with G: and so G became *Dominical letter* for 1655. as A was for 1654. and as those 2 days marked with the same letter A, coming together at every years end cause a change of the *Dominical letter*, so in the *Leap year* the Intercalary day *February the 25*, being marked with F, always as the 24th is, the coming together of those two dayes marked with one letter, causeth a second change of the *Dominical letter* for that year by like reason.

The third Table is a Table to find *Easter* for ever. This is placed outmost because it is the longest. It was very falsely

ordered in *M. Blagraves* book; and so it is in *Groftons Tables*, from whence I suppose he transcribed it. I have set it right and straight, and taken what care I could that the *Printer* or *Graver* do not put the ranks into the same disorder in which I found them, both in *Blagrave*, and in *Groftons Tables*, printed 8 years before him.



CHAP. XII.

Some cautions to be Observed in the making of the Instrument.

THough I have taught the making of the *Mater* first as being the base and principal part of the *Instrument*; yet I shall advise you first to draw and cut out the *Reet*, and fit the *Label* to it, leaving it sufficient length to reach to the out-side of the *Mater*. And then having your *Ring* ready fitted to screw on to the *Mater* you shall drill the centers of the *Mater*, *Reet*, and *Label*, with the same drill; and fasten them together with a *Center-pin* well fitted to the bore: this *Center-pin* must not be too big: let it be square at the head to stick in the backside of the *Mater*, that it turn not; and let the other end have a male screw, upon which you shall turn a female screw, to draw the plates together; so that they be neither too loose nor stick too hard. Then take a great needle, or such a round point of hardned steel, and bearing it up into some corner of the *Reet* close to the inside of his *Limb*, turn about both *Reet* and Needle upon the *Mater*, so that the Needle may trace out the great *Meridian* of the *Mater*, and so the principall Circles of the *Mater* and *Reet* shall be sure to be Concentric, and to agree in all postures of the *Reet*: whereas if you draw the *Meridian* of the *Mater* before you have bored the Center, and fitted on the *Reet*, you shall hardly happen to bore so true, but you shall find the Circles to be a little Eccentric and interfering one with another. And to avoid the like Eccentricity in the Circles of the *Ring*, it were best to have a sorry Beam Compass made onely for this purpose, and fitted to your Center pin to draw them by: yet if those be drawn from the Center of the *Mater* unbored, there will be no perceivable error, if you devide them from the *Limb* of the *Reet* by the *Label* when all is pinned together. These things done, quarter the *Meridian* of the *Mater* with two cross *Diameters*, and divide them as is above directed; remembring to apply your *Reet* to the *Mater* often, to see how the divisions of the *Diameter* agree, and how the *Meridians* and *Parallels* which you are drawing on the *Mater* agree with the *Azimuths* and *Almicanters* of the *Reet*. And thus by comparing your plates often, and examining the lineaments of the one by the other, as you draw them, you shall avoid many slips and mistakes, and proceed in your work with more confidence and contentment.

The end of the first Book.

E 3

The

The second Book.
 Of the several Projections of the
S P H E A R;
 which are represented by this
P L A N I S P H E A R.

The Preface.

THe Sphear may be Projected fitly upon the Plain of any great Circle: but the Projection will be of little use for resolving Questions in Astronomie, unless it be made upon one of these fowre, the Meridian, the Equator, the Azimuth of the Nonagesimus gradus, or the Horizon. This Planisphear is fitted therefore to represent all those four Projections, and especially the two former.

C H A P. I.

*Of the Planisphear in the Meridional Projection, representing the Eastern or Western Hemispheres:
 And of his three Modes or postures.*

WHat M. Blagrove Book 2. Chap. 15. 16. calleth the first and second distinction of the Jewel, I call the first and second Meridional and Equinoctial Projection of the Planisphear, for which change of termes I hope the Judicious Reader will not blame me. The Meridional Projection is the Eastern or Western Hemisphere projected

projected upon the plain of the Meridian of your place, which is the great and cheif Meridian in every Country, passing through the *Zenith* and *Nadir* of the place, as well as through the Poles of the World. The eye in this Projection is supposed to be placed in the East or West point of the Horizon. The lineaments which belong to this Projection are the innermost Scale of the *Ring*, and all the lineaments of the *Mater* and *Reet*, except only the *Zodiack* of the *Reet*, and the Stars. Here the outmost Circle both of the *Mater* and *Reet* represents the great Meridian of your place, and the Scale upon the inside of the *Ring* divided into 360 degrees serveth to divide the said Meridian: for the *Label* laid upon any degree of the Scale of the *Ring* cutteth the same degree in the Meridian Circle; because it is concentrick thereto.

This Meridian also standeth for *Colurus Solstitiorum*, (so they call that Meridian which passeth through the beginning of *Cancer* and *Capricorn*) for though all the Meridians in 24. hours space do successively come into the Meridian of your place (which is the Noon Circle passing over your head North and South) and the *Sphear* may be divided into Eastern and Western *Hemisphear* by any of these Meridians, when they become Vertical, yet the *Sphear* is then in the best posture to be divided for our purpose into East and West, when *Cancer* is Southing, *Capricorn* at midnight, and \cap \circ rising full East, and γ \circ setting full West.

In this Meridian at A, or *Oriens* is the North Pole, and the South Pole at B, or *Occidens*: for the words *Oriens* and *Occidens* are there placed to serve the Equinoctial Projection. The Concurrent Circles meeting in the Poles A and B are Meridians. Those Meridians are 180 in number, and divide the Equator CD into 360. degrees, because every one of them cutteth it twice, that is once in each *Hemisphear*. By these are numbred the Right Ascensions of the Stars and Planets, and the hours and minutes of Day and Night: for every 15 of these Meridians numbred from the *Limb* is an hour Circle, as hath been shewed (Book 1.6.) they are numbred from D to C, that is, from *Septentrio* to *Meridies* 1.2.3. &c. for the Morning hours, and back again from C to D, in like manner for the Afternoon: the A xeltree line A B falling out to be the six a clock line both ways. By those Meridians also are numbred the Longitudes of Towns and Countries in *Geography*.

The Circles or Semicircles crossing these Meridians are the
Parallels

Parallels of Declination: they are lesser Circles whose propriety it is to divide the *Sphear* into unequal parts. In the midst of them lies the Equator C D, being here a straight line, and cutting the Axtree-line A B at Right Angles in the Center E: the Parallels are greatest near the Equator, and from thence they lessen toward the Poles, they are 180 in number i.e. 90 on each side the Equator, save that the two extreame Parallels are reduced to two points in the Poles. By these Parallels are numbred the Declinations of the Stars in *Astronomie*, and the Latitudes of Towns and Countries in *Geography*.

And this name and use have the Circles of the *Mater* always in the Meridional Projection. The *Ecliptick* always standeth for it self, when it is used, which is onely in the first Mode of this Projection. But the Circles of the *Reet* have divers names and uses, in the divers Modes of this Projection, which here follow.

1 *The first mode of the Meridional Projection.*

The point A of the *Reet* in which the Concurrent Arches meet, is called the *Vertex* of the *Reet*. Set the *Vertex* of the *Reet* to the Latitude of your place, so shall the *Vertex* be *Zenith*, and the Concurrent Arches there meeting shall be *Azimuths*, called also *Vertical Circles*, and *Circles of Position*, passing from *Zenith* to *Nadir*, and dividing the Horizon into 360 degr. as the Meridians on the *Mater* pass from Pole to Pole; and divide the Equinoctial. The Semicircles crossing these *Azimuths* shall be *Almicanters* or *Circles of Altitude*. The Diameter crossing the Axtree of the *Reet* at Right Angles shall be the *Horizon* or *Finiter*, whose Graduations are set to him in a border below the Center, and from him are the *Almicanters* reckoned upward to the *Zenith*. The *Azimuths* may be reckoned from the North or South Semicircles of the Meridian, or from the Axtree-line of the *Reet*, which is the East or West *Azimuth*, commonly called the *Prime Vertical*. When I bid you set the *Vertex* of the *Reet* to the Latitude of your place; you must first know what your Latitude is. It is the nearest distance of your place from the Terrestrial Equinoctial, numbred in degrees and minutes of a great Circle. The Latitude of London is 51 degr. 32 min. North. The Latitude of *Elton* or *Norhampton*, is 52 degr. 15 minutes, or very near, And how to get the Latitude of those

or any other place shall be shewed Book 4. 11. The Latitude had, number the degrees thereof upon the *Ring* from C or *Meridies* (where the Equator cutteth the Meridian) toward A or *Oriens*, which in this Projection is the North Pole, because we in England have North Latitude. At the end of this number see for *London* 51. degrees 32. minutes, from the Equator Northward, set the Vertex of the *Reet*, so this Vertex representeth the Zenith, or point in the Heaven which is just over your head, in which point all the Azimuths meet, and through which also passeth the Meridian of your place, which here is represented by the outmost Circle of the *Mater*, or the innermost Circle of the *Ring*. Now is the upper Semicircle of your Meridian divided into four notable parts. From the Zenith Southward to the Equator is the Latitude 51. degrees 32 minutes, from thence to the Horizon is the complement of the Latitude 38. degrees 28. minutes, making up a Quadrant: againe from the Zenith Northerly to the Pole, is the complement of Latitude 38. degr. 28. minutes, as before: and from thence to the North of the Horizon is the Elevation of the Pole above your Horizon: which is always equall to the Latitude of your place: for where in a right *Sphear* the Poles ly in the Horizon, and have ^{no} Elevation, there the Equator passeth through the Zenith, and if you go from such a Country Northward till the Pole be Elevated one degree, the Equator shall there decline from your Zenith one degree Southward, because the Equator keeps always the distance of 90 degrees from the Poles. And this distance of the Zenith of your place from the Equator is called by Geographers *Latitude*, and is always equal to the Elevation of your Pole. So that it is all one whether you set the Vertex 51. degrees 32. min. above the Equator, or set the North point of the Horizon 51. degrees 32. minutes below the North Pole.

Now the Vertex of the *Reet* set to the Latitude, and consequently the Pole mounted to his due Elevation, your *Plani-sphear* is in a right mode and posture speedily to resolve all questions concerning the Diurnall motion; as the Suns longitude, Declination, Right Ascension, the Ascensionall differences, with the Semidiurnall Arch or length of the day, the Suns Altitude, Azimuth, and Amplitude; the hour and minute of the day, the beginnings endings and duration of twilight, and such like; and that with so great facility, that having onely the Longitude of

the Sun (with the Ephemeris on the *Ring* shall give you for asking) and therewith either the *Altitude* *Azimuth* or *Houre*, one of them: you may see all the rest at the first view without changing the posture of your Instrument; as shall appear in the fourth book.

2 *The second Mode of the Meridional Projection.*

Set the Zenith, or Vertex of the *Reet* to the North Pole of the *Ecliptick*, (or which is all one) set the Horizon line of the *Reet* in the *Ecliptick* line of the *Mater*, so the *Azimuth* shall in this posture become Circles of Longitude, and the *Almicanters* Circles of Latitude: And in this Mode your *Planisphaer* is fitted to resolve all Questions of the Longitude, Latitude, Right Ascension, and Declination, of the Stars.

3 *The third Mode of the Meridional Projection.*

Number the *Altitude* of *Culmen Cali*, (that is the Southing point of the *Ecliptick*) in the *Ring*, from the North Pole toward *Meridies*, if the Ascendant be a North Signe, or toward *Septentrio*, if the Ascendant be a South Signe. To the end of this numeration palce the Finiter. Reckon also upon the Finiter from the Center toward *Septentrio* the *Amplitude* of the Ascendant; the Meridian cutting there gives you the arch of the *Ecliptick* from the Ascendant to the Midheaven: and his match taken so many degrees on the other side the Center gives the other arch of the *Ecliptick* from the Midheaven to the Descendant. The rest of the Meridians and the Parallels are in this Mode of no use. The *Almicanters* and *Azimuth* of the *Reet* here shew you the *Altitude* and *Azimuth* of every degree of the *Ecliptick* at one view.

CHAP: II:

Of the Equinoctial Projection: shewing the Northern or Southern Hemisphaers.

THe Equinoctial Projection representeth the Northern or Southern Hemisphaer projected upon the plain of the Equator. Here the *Limb* or outmost Circles of the *Mater* and *Reet* are Equator. The eye-point

is the North or South Pole, which you will, by turns. Which Poles are here expressed on the Center of the Equator, because the Sphear is pictured on a plain or flat. The Axtree line of the Mater A B is *Colurus Equinoctiorum*, the Diameter C D crossing him is *Colurus Solstitiorum*. But contrary on the Reet the Axtree is *Colurus Solstitiorum* and the Finiter *Colurus Equinoctiorum*. The *Colurus Solstitiorum* on the Mater is also the Meridian of your place, and therefore is marked with *Septentrio*, and *Meridies*; and the ends of the Axtree with *Oriens*, and *Occidens*. The rest of the Meridians being all straight lines meeting in the Poles or Center, are easily supplied by the Label: and so may the Parallels also, being Concentrick with the Equator. For if you lay the Label on the 15. degree in the Limb from *Meridies* toward *Occidens*, the fiduciall edge of the Label there designeth the 15 Meridian, or the One a clock line: the North Quadrant of the said Meridian proceeding from the Center (now the North Pole) outward to the Limb or Equinoctial, and the South Quadrant returning in the same line from the Equinoctial to the Center: (now the South Pole :) and if you remove the Label 180. degrees from One a clock of the day, there it shall designe One a clock at night, made by the other Semicircle of the same Meridian, which joyneth with his match in the Center without any angle, that is, into the same straight line: and so of the rest.

And for the Parallels, if you set the point of your Compass or a needles point in the 23. degree $\frac{1}{2}$ of the Label, and turn about the Label with the point, it shall describe a Circle which will serve for both the Tropicks: and so may you make any other of the parallels. I do not advise you to draw the Meridians and Parallels in this form, least you cumber your Instrument, but I shew you how you may represent any of them in a moment, when occasion requireth.

The Meridians of the Mater, (that were so called in the Meridional Projection) are here turned into the severall Horizons of the World. And the Parallels here serve only to graduate those Horizons. Out of these Horizons choose your own Horizon, and distinguish him if you will that you may readily find him when you shall looke for him.

Your Horizon is thus inquired. Because the Elevation of the Pole at Northampton is 52. degrees 15. minutes, therefore

from the Center (now North Pole) number in the Meridian line Northward 53. degrees 15. minutes, and there cutteth the North Semicircle of our Horizon, or there you may Imagine him between the 52 and 53 Horizons, and the Southern Semicircle thereof lies 52 degrees 15 minutes on the other side the Center towards *Meridies*. This may seeme strange that the North and South points of the Horizon, which in the *Sphear* are unequally distant from the North Pole, viz. the one but 51. degrees 15. minutes, and the other 127. degrees 45. minutes, (the supplement thereof) should be equally distant in this Projection. But the reason is because the Center is both North and South Pole here at pleasure, and the Northern and Southern *Hemispheres* are both here represented by turns. Carry this in your head, and then lay the *Eabel* upon the South part of the Meridian, and number thereon from the Center (now North Pole) outward to the Equator at the *Limb* 90. degrees, thence number backward toward the Center (now the South Pole) the Elevation of the Equator (which is always complement of the Elevation of the Pole, and is here 37. degrees 45. minutes) there is the Southern point of the Horizon, and is distant from the Center (now South Pole) onely 52 degrees 15 minutes, but from the Center being North Pole 127. degrees 45. minutes, and from the Northern point of the Horizon before found just 180. degrees, as it is in the *Sphear*. Having found the North arch of your Horizon 52. degr. 15. min. behind the Center; count as many degrees and minutes forward in the Meridian before the Center toward *Meridies*, and the arch crossing there shall be his match to make up the whole Circle; and so may you find your whole Horizon upon the *Mater* whatsoever your Latitude be.

Here you must remember, that Stars which have Northern Declination rise and set upon the Northern arch of the Horizon; and those which have Southern declination upon the Southern arch. Remember also, that many Stars between the Tropicks which have Northern Latitude, have nevertheless Southern Declination, and contrary many which have Southern Latitude have Northern Declination.

The lineaments of the *Reet* serving you in this Projection, are onely the Ecliptick, and the fixed Stars, the Alimicanters and Azimuths here are of no use. The Meridians and Parallels

are supplied by the *Label*, for the *Reet* as well as for the *Mater*.

And whereas the *Ecliptick* here seemes to be irregular, seeing the *Solstitial* points of *Cancer* and *Capricorn* are not distant 180 degrees, as they should be, you must imagine that the Southern arch of the *Ecliptick* is Projected by the eye placed in the North Pole, and for the Northern arch the eyes place in the South Pole: and the Center serveth for both the Poles alike, as hath been shewed: number therefore as you were taught for the *Horizon* in this Projection. For the reason of the draught of the *Horizon* and of the *Ecliptick* in this Projection is the same.

CHAP. III.

Of the Nonagesimal Projection, shewing the Eastern and Western parts of the Sphear, being divided by the Azimuth of the Nonagesimus gradus.

Number in the *Limb* from the *Equinoctial* line toward the Pole the *Altitude* of the *Nonagesimus gradus*, (which is the highest degree of the *Ecliptick*) and thereto set the *Finitor*, turning the *Almicanters* either to the North or to the South, as your work proposed shall require.

Now is the *Finitor* *Ecliptick*, his point at the *Limb* is *Nonagesimus gradus*. The Center of the *Plansphear* is *Ascendant* and *Descendant*, the East and west points of the *Horizon* are here distant from the Center as much as the *Amplitude* of the *Ascendant* cometh to, to be counted from the Center upon the *Equinoctial* line of the *Mater*, which here stands for *Horizon*: the *Meridians* and *Parallels* of the *Mater* are here *Azimuths* and *Almicanters*, but the *Azimuths* must be numbered from the East point of the *Horizon*. The *Azimuths* and *Almicanters* of the *Reet*, are here *Circles of Longitude* and *Parallels of Latitude*. Here are no *Meridians* nor *Parallels* of *declination* in this Projection, onely the great *Meridian* of your place is to be found here, because he is an *Azimuth* as well as a *Meridian*, for he passeth through the *Zenith* as well as through the *Poles* of the *World*, and this *Meridian* is always distant from the *Limb* (or *Azimuth* of the *Nonagesimus gradus*) as much as the *Ascendant*

dant is distant from the East point of the Horizon: for the Amplitude of the Ascendant and the Azimuth of the *Nonagesimus gradus* are always equall, and as the Meridian cutteth the Horizon 90. deg. Westward, from the East point, so doth the Azimuth of the *Nonagesimus gradus* always cut the Horizon 90. degrees Westward from the Ascendant.

This Projection is of excellent use, for getting the Altitude and Azimuth of any or all the degrees of the Ecliptick at once, also for getting the Longitude and Latitude of Planets, Comets, or Stars unknown, by their Altitude and Azimuth Observed.

CHAP. III.

Of the Horizontal Projection, representing the upper and lower Hemispheres.

Here the *Limb* must be reputed Horizon, and the Center of the *Planisphere* the Zenith of your place. Then may you by one of the Azimuths of the *Reet* represent the Ecliptick in any of his postures, (whatsoever degree be Ascending) and by the *Label* you may presently find the Altitude and Azimuth of every degree thereof. Likewise may you here represent the plain of any Declining-inclining Dial, by some one of the Azimuths: and the Meridian of the Plain by one of the Meridians: by the help whereof you may resolve divers Problemes in Dialling, as shall appear in due place,

The end of the Second Book.

The Third Book.

Of the Resolution of all Spherical Triangles,
by the

PLANISPHEAR.

CHAP. I.

Of the kinds and parts of Spherical Triangles.

IT is to be known, that 1. Spheri. Triang. are $\left\{ \begin{array}{l} \text{Rectangular} \\ \text{Obliquangular.} \end{array} \right.$

2 A Rectangular Triangle is that which hath one or more Right Angles.

3 A Triangle that hath three right Angles hath alwaies his three sides Quadrants.

4 A Triangle that hath two right angles hath the sides opposite to those angles Quadrants, and the third side is the measure of the third angle. So that of those Triangles which have more Right angles, seldome ariseth any question. But the Right angled Triangle with one Right and two Acute angles, is that which comes most commonly to be resolved.

5 A Right angle is that which containeth 90 degrees, or openeth to one quarter of the circumference of any Circle described from the angular point,

6 All Spherical Triangles not Rectangled are called Oblique-angled. And if they have one angle greater then a Right angle, they be called Obtuse-angled, otherwise they be Acute-angled.

7 In rectangled Triangles the sides including the Right angle be called Legs, the side subtending it is called Subtense or *Hypotenuse*.

8 Either Leg of a rectangled Triangle may be made Basis, (if you will imagine him to lie level) and then the other leg shall be called *Cathetus* or Perpendicular.

9 In Oblique angled Triangles, the sides comprehending the angle given or sought, are called *Legs*, and the third side the *Base*.

10. In every Spherical Triangle there be (beside the Area or space contained) six containing parts *viz.* three sides, and three angles: of those six there must be three alwaies known or given to find out the rest.

CHAP. II.

Of the 16 Cases of Rectangled Triangles. And how they may be reduced to five Problemes.

IN the Rectangular Spherical Triangle there be five parts onely come into the Question; the three sides, and two acute angles: because the third (being right) is alwaies known. Of these five parts any two being given the rest may be found.

There be 16 Cases or *Problemes* about Spherical Triangles, six for finding the *Legs*; four for the *Hypotenusa*; and six for the *Angles*. See *Gellibrand. Trigonom. Britan.* But we may here reduce them all to 5 *Problemes*, because our *Planisphaer* resolveth alwaies two of them at once. For by two parts given you shall presently get two of the three that are unknown: and if you do but turn the Triangle, you may presently have the third also: as shall appear in this book.

The Rectangular Triangle in question shall be marked throughout this book with *A B C* in this maner: so that the *Base* shall be marked and called *B A*, the *Cathetus*, or Perpendicular *Leg C A*, and the *Hypotenusa* *B C*.



The right angle *A*, the angle at the *Base B*, the angle at the *Cathetus C*. And note that in the 4 first *Problemes* *B A* shall be alwaies set upon the Equinoctial line of the *Mater*, *C A* in a *Meridian*, *B C* on the *Label*, and *B* alwaies at the *Center*; as you shall find in the four next Chapters.

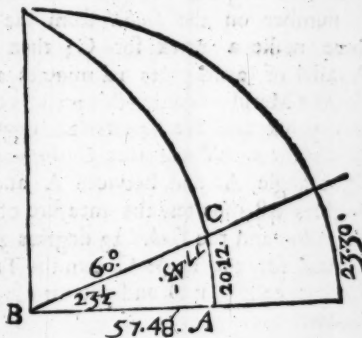
CHAP. III. PROBL. I.

The Legs given, to find the rest.

S Et B at the Center, B A, on the Equinoctial line of the Mater, C A, on that Meridian which crosseth at A; then lay the *Label* to C, and your Triangle is made. Example.

Let B A be 57. degr. 48. min. C A 20. degr. 12. min.

I number in the Equinoctial line from the Center toward Meridies the length of B A to 57. degrees 48. minutes, and there I imagine stands A. Now because this Base endeth between the 57 and 58 Meridians, but nearer to the 58, I must imagine a Meridian passing between them in his due distance



which shall cut off your Base in his due length of 57 degrees $\frac{1}{2}$, and in that imagined Meridian I number upwards from the Equator, by help of the Parallels, the length of the Cathetus C A 20. degr. 12. minutes; at the top of this Cathetus is the place of C, whereto I set the *Label*, and the Triangle is made upon the Planisphere, in such form as the figure here sheweth.

Now may you number B C the *Hypotenuse* upon the *Label*, and find it 60. degrees, the angle B hath his measure on the *Limb* between the Equator, and the *Label* 23 degrees $\frac{1}{2}$.

Lastly to find the angle C do but turn the Triangle, setting C A on the Equinoctial, and B A on a Meridian, (according to the 1. 8.) and laying the *Label* to B you shall find B C 60. degrees as before, and the measure of the angle C between the Equator and the *Label* may be reckoned on the *Limb* 77. degr. 43. min.

Note here that in this and all other like cases, in stead of the *Label* you may better use one of the Semidiameters of the *Reet*; for they have the same graduation, and lie closer to the *Mater*.

CHAP. III. PROBL. II.

A Leg and the Hypotenusa given to find the rest.

S Et the *Hypotenusa* *BC* on the *Label* from the Center: the given *Leg* (to be marked *CA*) in one of the *Meridians*. Example. In the former Triangle, where the *Hypotenusa* was 60. degrees, the *Cathetus* 20. degrees 12. minutes: I number on the *Label* from the Center 60 degrees, and there make a prick for *C*; then I turn this prick to the Parallel of 20. degrees 12. minutes, and the Triangle is made. For the *Meridian* cutting this prick is *Cathetus*, and hath betwixt this prick and the *Equator* 20. degrees 12. minutes, as the *Parallels* shew. Where this *Cathetus* cuts the *Equator* stands the right angle *A*, and between *A* and the Center lies *BA*, 57. degrees 48. minutes: the measure of *B* is on the limb between *Meridies* and the *Label* 23. degrees 30. minutes.

And for the angle *C* turn the Triangle. Set *C* now at the Center, calling it *B*, and you may find this angle as you did his fellow.

CHAP. V. PROBL. III.

The Hypotenusa and an Angle given, to find the rest.

S Et the *Hypotenusa* on the *Label*, the Angle given at the Center. Example. In the former Triangle the *Hypotenusa* was 60. degrees, and the greater angle 77. 43. I number in the *Limb* from *Meridies* toward *Oriens* 77. degrees 43. minutes, and there I set the *Label*, then I look the 60. degree of the *Label* numbred from the Center, at that 60 degree is *C* where the *Hypotenusa* and *Cathetus* meet. Here therefore the *Meridian* that cuts the *Label* in 60 degrees makes the *Cathetus*: I follow him down to the *Equator* and find his length 57 degrees 48 minutes, and from the point where he cuts the *Equator* I go straight to the Center, and find 20 degrees 12 minutes the length of *BA*.

Lastly for the angle *C* turn the Triangle, setting *C* at the Center, and calling it *B*; and you shall find *C* as chap. 3. For
whereas

whereas your *Hypotenusa* is 60, and your *Cathetus* 20 degrees 12 minutes, lay the 60 degree of the *Label* upon the 20 Parallel, and the *Label* shall cut in the *Limb* 23 degrees 30 minutes, the measure of the angle C.

CHAP. VI. PROBL. IIII.

A Leg and an Angle given to find the rest.

IF the *Leg* be conterminat or adjoyning to the angle given, then make the given *Leg Base*, letting it upon the *Equator*; and move the *Label* from the *Equator* toward the *Pole*, so many degr. as the given angle B comes to. Then mark what *Meridian* cuts the end of the *Base*, that *Meridian* makes the *Cathetus*: follow him till he crosseth the *Label*, in that crossing is the angle C of your Triangle, from whence you reckon the length of the *Cathetus* to the *Equinoctial*, and the length of the *Hypotenusa* next way from C to the Center.

And now having all the sides, to get the angle C you shall turn the Triangle, and get him as in the 3 Chapter.

But if the *Leg* be opposite to the Angle given, make the given *Leg Cathetus*, that the angle given may be at the Center.

Example. In the former Triangle I have given the less angle 23 degrees $\frac{1}{2}$, and the *Leg* opposite thereto 20. degr. 12. min. I open therefore the *Label* from the *Equator* to 23 deg. 30. min. on the *Limb*, and mark where he cutteth the 20 $\frac{1}{2}$ Parallel, for there is the angle C of the Triangle; thence you shall have a *Meridian* for the *Cathetus* going to the *Equator*, whose length is 20 degrees 12. minutes: thence in the *Equator* to the Center is the *Base* 57. degrees 47. minutes; and thence in the *Label* to C again, is the *Hypotenusa* 60 degrees.

And now having all the sides, to get the angle C, you shall turn the Triangle, and get him as in the 3 Chapter.

CHAP. VII. PROBL. V.

The Angles given to find the Sides.

THIS should have been the third Probleme, considering what is given. But because the way of resolving this

case differeth from all the former, therefore I have reserved it to the last place.

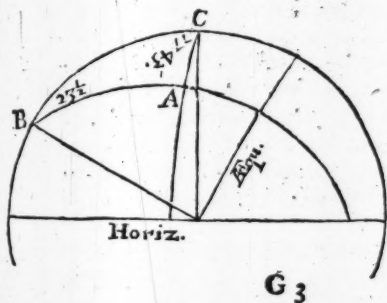
In plain Triangles this case is insoluble. But in Spherical Triangles it may be resolved on the Planisphaer, two wayes.

1. The first way hath *M. Elagave* 5, 24. He sets B C on the *Limb* between the Pole of the *Mater* and the Vertex of the *Rect*, B A and C A one on a Meridian, and the other on an *Azimuth* crossing one another at a Right angle within the *Limb*. Which to do you must work thus. Example. In the former Triangle, the Angles are given A 90, B 23, degr. 30, min. C 77, degr. 43, min. Now first I will guess that the *Hypotenusa* is 40 degrees, and setting the *Zenith* 40 degrees from the Pole, that arch of the *Limb* between Pole and *Zenith* I take for my *Hypotenusa*, yet unknown. At the Pole shall be B, and at the *Zenith* C. Then because B is $23\frac{1}{2}$ I take the twentieth-third Meridian from my *Hypotenusa* which is on the *Limb*, and between that and the 24th I imagin a Meridian which shall make B A of my Triangle. Also because the Angle at C is 77, degr. 43, min. I take an imaginary *Azimuth* near the 78th, numbred from my *Hypotenusa*, which is on the *Limb*, and that *Azimuth* shall make C A of my Triangle. Now have I the Angles B and C, and three arches, of which all the sides of my Triangle shall be made: but whether B A and C A cross at Right Angles I know not, and therefore I know not yet certainly the length of any side. Now to make the Angle at A a Right Angle, mark where your *Azimuth* (which you have taken for C A) cuts the *Finiter*, and from that point number in the *Finiter* toward the Center to 90 degrees, and there is the Pole of your *Azimuth*; (*viz.* 12 degrees 17 minutes from the *Limb*) make a prick with ink at that Pole, and then look whether your Meridian $23\frac{1}{2}$ (which you took for B A) cut this Pole, which yet he doth not as you will find. Therefore turn the *Rect* till the said Meridian do cut this Pole of the said *Azimuth*, and then you may be sure that Meridian and *Azimuth*, (wherever they cross,) do make Right Angles. (By *Pittsc Trigonom.* 1, 57) Therefore now have you all the Angles set on the Planisphaer, and thereby all the sides found, *viz.* B C in the *Limb* 60, degr. B A in the Meridian 57 degrees 48 minutes. C A in the *Azimuth* 20 degrees 12 minutes, as they ought to be.

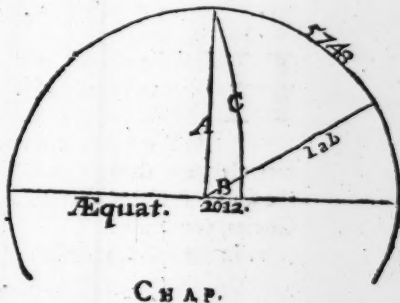
2. The second way *M. Oughtred* useth: It is this. For the
rectangled

rectangled Triangle whose three Angles be given, you shall frame another oblique Triangle, whose sides shall be equal to the Angles of the first Triangle. And so the Angles of the second Triangle to be found on the Planisphaer shall be equal to the sides of the first Triangle, which are inquired. The Triangle which serveth for an Example throughout this Book hath his Angles A 90 degrees, C 77 degrees 43 minutes, B 23 degrees 30 minutes. Here to find the sides, for the Angle A, I take half the Axis of the *Mater* from the Center to the Pole, and that shall be a side of 90 degrees. For the lesser Angle B, I reckon upon the *Label* from the Center a side of 23 degrees 30 minutes, and at the end thereof make a prick, on the *Label*. I turn this prick upon the Parallel from the Pole 77 degrees 43 minutes, and the Meridian there Crossing shall be the third side of this Triangle. Follow this Meridian to the Equator, and from his cutting there to the Center is the measure of the lesser Angle of this second Triangle, which is equal to the lesser Leg of the first Triangle, 20 degr. 12 minutes: likewise the arch of the *Limb* from the Pole to the *Label*, is the measure of the middle Angle of the second Triangle, which is equal to the middle side, that is, to the greater Leg of the first Triangle 57 degrees 48 minutes. And now having found the Legs of the first Rectangled Triangle you may by the first Probleme find the *Hypotenusa* to be 60 degrees. The Rectangled Triangle used in the first way, and the oblique *Quadrantal* Triangle used in this second way, shall appear in such formes on the Planisphaer as these figures following do exprefs.

The first Way.



The second VVay.



CHAP. VIII.

How to represent and resolve the Cases of the four first Problemes of Spherical Triangles, divers other wayes.

ONe way hath been shewn for representing any Rectangled Spherical Triangle upon the Planispher, by the Label, Equator-line, and a Meridian, and thereupon to find out the sides and Angles of any such Triangle.

Now for *Variety* sake, and for the exercise of Learners in the knowledge of the Sphear, and because the same Angle sometimes may be more distinctly represented in one part of the Planispher then in another, I have thought good to set down six other wayes, by which the four first Cases of Spherical Rectangled Triangles may be pictured on the Planispher, and resolved.

There be three places in the Planispher where the Angle B may be placed, whether he be given, or sought.

1. At the Center, and there his quantity is measured by the Label or any Semidiameter of the *Reet*, moving upon the *Ring*, thus was B placed in the former Chapters, and shall be once more in the first *Variety*.

2. At either of the Poles of the *Mater*, where by the Meridians that issue thence you may number the quantity of any Angle from 0, to 180.

3. At the *Zenith* or *Vertex* of the *Reet*, where the quantity of the Angle may be numbred by the *Azimuths* in like manner.

CHAP. IX.

The first Variety.

Here the angle B shall be at the Center as before; B A on the Finiter, C A in an *Azimuth*. B C in the Axis of the *Mater*. So shall you have your Triangle pictured in the same form and quantity that he had in the former chapters, though other lines be here used. And to resolve the four first Cases of Rectangled Spherical Triangles with these Circles, you shall,

1. In the first Case where B A and C A are given, Number B
A from

A from the Center upon the Finiter; where it ends, you shall meet an *Azimuth* upon which you shall number C A toward the *Zenith*; in the top of C A make a prick with ink for C, and then turn that prick to touch the Axis of the *Mater*. Thus have you all the sides in view, and the measure of the angle B you shall find upon the *Limb*, between the Pole and the Finiter. And for C you must turn the Triangle as before hath been taught.

2. In the second Case. B C and C A given, Number B C in the Axis from the Center, and at his end for C make a prick; Then for C A count to what *Almicantar* he will rise from the Finiter, and turn the *Reet* till that *Almicantar* cut the prick C in the Axis; and the *Azimuth* there crossing the Axis and *Almicantar* in C shall make C A. And between that *Azimuth* and the Center shall be B A on the Finiter. B shall be measured as before. C shall be found as before.

3. In the third Case B C and B given, Set the Finiter as much from the Pole as the angle B comes to. Then number B C in the Axis from the Center B to C. Thence turn down in the next *Azimuth* to the Finiter and you make C A. Thence turn to the Center, and you close the Triangle with B A. C shall be found as before.

4. In the fourth Case, if B and B A be given, Set the Finiter to the angle B. as in the third case in this chap. and from the Center upon the Finiter number B A. from A go up an *Azimuth* to the Axis, where C shall stand. From thence go to the Center, and you have compassed your Triangle, and all is shown by the view, but the angle C, which may be found as before. But if B and C A be given, set the Finiter to the angle, as in the third Case of this chap, then count in what *Almicantar* C A will end, and follow this *Almicantar* to the Axis, where they meet is the point C. And the *Azimuth* that cutteth there shall cut the Finiter in the place of A.

CHAP. X.

The second and third Varieties.

SET B at one of the Poles of the *Mater* where the Meridians meet; B A on the *Limb* either way B C in a Meridian C A on the *Label*. One Example of the third Case shall suffice. B and B C are given. B is 77 degrees 43 minutes; Number therefore the Meridians from the *Limb* till you come past 77 and almost to 78, and there imagin a Meridian to be drawn for the *Hypotenusa* of your Triangle; That Meridian maketh an angle of 77 degrees 43 minutes with the *Limb*, as the *Hypotenusa* of your Triangle doth with the Base. And because the *Hypotenusa* B C is 60, therefore the 60th Parallel reckoned from the Pole shall determin his length, and cut him off in the point C. Prick the point C (that is, the crossing of the 77 43 Meridian with the 60th Parallel from the Pole) and to that prick lay the *Label*: so that part of the *Label* which lieth between the prick and the *Limb* shall be C A, and the arch of the *Limb* between the Pole and the *Label* shall be B A of the Triangle. So shall all be known but C, which also may be found if you turn the Triangle as before.

Or thirdly, using only the *Reet* and *Label*, Set B at the *Zenith*; B A on the *Limb* of the *Reet*; A C in the *Label*; B C in an *Azimuth*, and you shall make the same Triangle on the *Reet*, that you made last on the *Mater*.

CHAP. XI.

The fourth Variety.

SET B at the *Zenith* of the *Reet*. B A upon the *Limb* from the *Zenith* to one of the Poles of the *Mater*. C A in the *Axtree-line* of the *Mater*, B C in an *Azimuth*,

CHAP. XII.

The fifth Variety.

S Et B at one of the Poles of the *Mater*, B A upon the *Limb* between the Pole and *Zenith*, C A in the Axis of the *Reet*, B C in a Meridian.

Note here, that if you set the Triangle upon the Planisphere either of those two last wayes, you shall find him to be set both wayes, and that you haue your Triangle twice found, or two Triangles, each of them representing the Triangle in Question, one is toward the right hand, and the other toward the left : And they are both comprehended between the Axletrees of the *Mater* and *Reet*; and the arch of the *Limb* which lies between the two Axletrees is Base to them both.

CHAP. XIII.

The sixth Variety.

S Et the *Zenith* line of the *Reet* in the Equinoctial line of the *Mater*, Then set B at the *Zenith* B A upon the Equinoctial line inwards from the *Limb*, C A in a Meridian, B C in an *Azimuth*.

Thus have you various wayes for describing and resolving any rectangular Spherical Triangle upon your Planisphere. If in trying one way you find the points of your Triangle too much shadowed with the *Reet*, or that the sides cross one another too obliquely, that you can hardly find the point of the angle, then may you trie another way, and you shall likely find that fault amended.

These three last Chapters you shall easily understand, if you understand the former Chapters of this Book. And therefore I thought it needless to use any further exemplification,

CHAP. XIV.

*Of the Solution of Oblique angled Spherical Triangles:
And generally of all Spherical Triangles.*

THese six Chapters following might well have been placed before the second Chapter. For howsoever they best serve Oblique angled Triangles, yet are the Rules general, and may serve very well for the solution of all *Spherical Triangles* whatsoever. But I like this order well enough, and I think the Reader will have no cause to dislike it.

There be twelve Cases of Oblique-angled *Spherical Triangles*. But for the *Planisphere* they are here reduced to six. And they be all (unless I may except the last) as easily resolved upon the *Planisphere* as the five Cases of Rectangled Triangles.

Here note that for Oblique-angled Triangles, in all the Cases following, one side shall evermore be set upon the *Limb* between one of the Poles of the *Mater* and the *Zenith*, of the *Reet*, and the other two sides shall be made, one by a Meridian, and the other by an *Azimuth*; at the meeting whereof is the Angle C, which only may remain unknown after any Question resolved, and may be presently found by turning the Triangle, as before is hapned in the Rectangled Triangles.

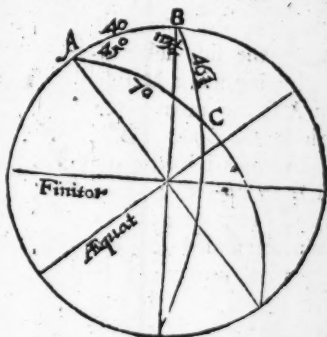
PROB. I. *Three Sides given, to find the Angles.*

SET one Side, (which you will) upon the *Limb*, between the Pole and *Zenith*, count the second side from the Pole by the Parallels, and count the third side from the *Zenith* by the *Almicanters*: and know that where the last Parallel cuts the last *Almicanter*, there is the point of the third Angle C: the Meridian that passeth from this point to the Pole is the side AC: the *Azimuth* that passeth from the same point to the *Zenith* is the side BC: and the third side AB is on the *Limb* between the Pole and *Zenith*. Now may you count the Angles at the Pole and *Zenith* and B: and for the third Angle C, turn the Triangle laying one of the other sides in the *Limb* between the Pole and *Zenith*, and you shall find that Angle also, as you did his fellows. Note that whereas I called the sides of Rectangled Triangles

gles B A. C A, and B C, that is *Basis*, *Cathetus*, and *Hypotenusa*, I choose here in Oblique-angled Triangles. to transpose the letters of the two first sides for distinction sake, calling them A B, and and A C, and the third side indifferently either B C or C B.

Example. Let 40 degrees 70 degrees and 46 degrees $\frac{1}{2}$ be Sides of a Triangle, whose Angles are sought. Now because I would first get the Angles joyning to the side 40 degrees, I mark that side A B, and set A B upon the *Limb*, A at the Pole, and B at the *Zenith*; which I remove 40 degrees from the Pole, according to the length of the side A B. Then because A C is 70 deg. I hold one finger (or a pin) upon the 70 Parallel from the Pole, and because B C is 46 $\frac{1}{2}$ I hold another finger on the 46 $\frac{1}{2}$ *Almicantar* counted from the *Zenith*, and look where this *Almicantar* crosseth the said 70 Parallel, there is C of my Triangle: The Meridian that comes from the Pole to C is the long side of my Triangle A C; I count then from the side A B on the *Limb* how many Meridians lie between A B and A C, and I find that A C is just the 45 Meridian, therefore I say the Angle A at the Pole is 45 degrees. The *Azimuth* that comes from the *Zenith* to C is here the middle side of my Triangle, being in length 46 $\frac{1}{2}$ I count from the side A B of my Triangle on the *Limb* how many *Azimuths* there are to this, and I find that this is the 114 *Azimuth* almost, therefore the Angle B at the *Zenith* is almost 114 degrees (exactly 113. 30. minutes.)

Now to find the Angle C, I turn the Triangle, and set B C, 46 degrees $\frac{1}{2}$ on the *Limb* (changing the letters into A B) And where the 40 Parallel crosseth the 70 *Almicantar*, there I meet with the 39 *Azimuth*, which shews me that the third Angle formerly called C, and now since the Triangle turned marked B is 39 degrees (exactly 38 deg 51. minutes.)



CHAP. XV. PROB. 2.

Two Sides and an Angle comprehended given, to find the rest.

S Et the Angle given at the Pole. and set one of the given sides in the *Limb* between the Pole and *Zenith*, the other given side you shall reckon on that Meridian which is distant from the *Limb* as much as the given Angle cometh to, at the end thereof there shall meet you an *Azimuth* which shall make the third side of your Triangle.

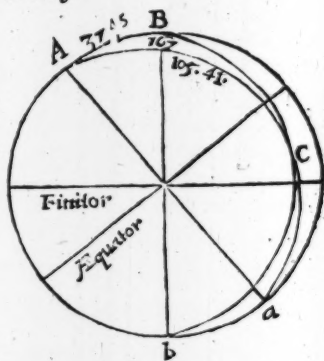
Example. In the former Triangle having A B 40. A C 70 and the Angle comprehended at A 45 degrees, I set A B on the *Limb* from Pole to *Zenith*, then because the Angle A is 45 degrees I take the 45 Meridian reckoned from A B, and thereof I take 70 degrees (counting from A the Pole) for my side A C: at C in the 70 degree of this Meridian there crosseth an *Azimuth* which makes my third side; this *Azimuth* is the $113\frac{1}{2}$ being numbered from A B, therefore the Angle at B is $113\frac{1}{2}$, and I finde between B and C in this *Azimuth* $46\frac{1}{2}$ for the length of the side B C: onely C is now unknown, which you may also find by turning the Triangle.

CHAP. XVI. PROB. 3.

Two Sides and an Angle opposite to one of them given, to find the rest.

S Et the given Angle at the *Zenith* B, the side subtending it in a Meridian A C, the other given side on the *Limb* A B.

Example. I have given A B 37 degrees 45 min. A C 105 degrees 41 minutes: and B 167 degrees 09 minutes: I set the *Zenith* B 37 degrees 45 minutes from the Pole A, then because B



is 167 degrees 9 minutes, I count the *Azimuths* from the side A B to 167 degrees, and farther 9 minutes, and I know that the *Azimuth* there imagined to pass (set between 167, and 168) shall make the side of my Triangle B C; but yet the length of B C I know not; and I want still a Meridian for the side A C opposite to the angle given. Now because A C his length is given (105 degrees 41 minutes, though the Angle A be yet unknown) I take the Parallel 105 degrees 41 minutes, numbred from the Pole A, and where this Parallel crosseth the 167 *Azimuth*, there I am sure must be the Angle C: and the Meridian passing from C. to the Pole is the side A C 105 degrees 41 minutes: this Meridian lieth between the 12 and 13 number from A B, and sheweth the Angle A to be 12 degrees 26 minutes: the side B C, I may count 68 degrees $\frac{1}{2}$ by help of the *Almicantars*. Now have I three sides and two Angles, which are more then enough to find the Angle C, when the Triangle is turned.

Note that you may place the known Angle at the Pole as well as at the *Zenith*, and it may be needfull so to do when the Angle C of your Triangle would otherwise fall under the *Limb* of the *Zodiacque*.

Note also that the Angle C may sometime fall under the *Finiter*, where the *Azimuths* faile. As if you had set the Angle 167 degrees at the Pole, the opposite side 105 degrees 41 minutes had been set in an *Azimuth*, and C had been beyond the *Finiter*: your remedie in this case is to set *Nadir* in the place of *Zenith*, so shall C fall among the *Azimuths* just as you would have him. Example. Set 37 degrees 45 minutes between the Pole and *Nadir* (a b) count the Angle given at the Nadir b 167 degrees 9 minutes, and his supplement 12 degrees 51 minutes, for A C count a C the supplement thereof, and you shall find b C 111 $\frac{1}{2}$, whose supplement is B C 68 $\frac{1}{2}$.

Note thirdly, that if the angle given in this chapter be acute, then if you place the known Angle at the *Zenith*, the Parallel may cross the *Azimuth* twice; or if you place the known Angle at the Pole, the *Almicanter* taken to find out the opposite side, may cross the Meridian twice; and so it may be doubtfull in which intersection the Angle C shall be found: That you may discover, if you examine which agrees best with the other parts of the Triangle being turned; or if you reduce this Triangle to

two Right-angled Triangles, by letting fall a Perpendicular. Of which see the last Chapter.

CHAP. XVII PROB. 4.

Two Angles and the Side comprehended between them being given, to find the rest.

S Et the side given between the Pole and *Zenith* on the *Limb*, then count one Angle among the Meridians, the other among the *Azimuths*, and where the Meridian and *Azimuth* bounding the said Angles meet, there is the point of the Angle C, and all is known but the Angle C, which you may find also, if you turn the Triangle.

Example. In the 14th Chap. The Angle A was 45° B $113\frac{1}{2}^\circ$ the side A B comprehended 40° . Having let the *Zenith* 40° from the Pole, I seek the 45° th Meridian from A B, and the $113\frac{1}{2}^\circ$ *Azimuth* from A B, and where they cross is C. Now may I number A C by the Parallels 70° and B C by the *Almicantars* $46\frac{1}{2}^\circ$. C may now be found by any of the 3 former Problemes, if you turn the Triangle, and let C at the Pole, or at the *Zenith*.

CHAP. XVIII PROB. 5.

Two Angles and a Side opposite to one of them given, to find the rest.

S Et the Angles given, as A, and B, at the Pole and *Zenith*; the known side, as B C in an *Azimuth*; Count among the Meridians the Angle opposite to the known side, and having found the Meridian that boundeth him, lay a finger or a bodkin point thereon; then count the other Angle among the *Azimuths*, and when you come to the *Azimuth* that boundeth him, because that *Azimuth* maketh the known side of your Triangle, you shall number his length from the *Zenith*, and at the end thereof make a prick, then turn about the *Reet* till this prick in the *Azimuth* touch the Meridian before found; and then is your Triangle formed on the *Plantshear*, and all is known: but the Angle C to be found as in the former Chapters.

Example. Let be given A 45° degrees B $113\frac{1}{2}^\circ$ B C $46\frac{1}{2}^\circ$. I count

count from A B to the 45th Meridian, upon which I lay my finger, that he get not away, for he must make my side A C, then I look the $113\frac{1}{2}$ Azimuth (from A B) to stand for the given side: and because his length given is $46\frac{1}{2}$ therefore in this $113\frac{1}{2}$ Azimuth at $46\frac{1}{2}$ below the Zenith I make a prick: then I turn the Reet till this prick touch the 45th Meridian, there at that touch must C stand; thence to the Pole is the side A C 70, and on the Limb I have the side A B 40. C is to be had by turning the Triangle, as in every of the former Problems.

CHAP. XIX PROB. 6.

Three Angles given to find the Sides.

THIS Case comes very seldome in use. Yet that our Method of Trigonometry by the Planisphaer may be compleat, and that no Probleme that is soluble may be left here unresolved, I shall shew the solution of this Probleme also. Mr *Blagrove*, it seemes, never attempted this, contenting himself that he had found the way to resolve this Probleme in Rectangled Triangles, which also he had once given over as impossible. *Blagr. Book 5, 24.*

For resolving this Probleme it is to be known that if you go to the Poles of the 3 great Circles wherof your Triangle is made, these Poles shall be the angular points of a second Triangle; and the two lesser sides of this second Triangle shall be equal to the two lesser Angles of your first Triangle; the greatest side of the second Triangle shall be the supplement of the greatest Angle of the first Triangle (that is, shall have as many degrees and minutes as the greatest Angle of the first Triangle wanted of 180 degr.) see *Pitiscus Trigonometry Lib. 1. Prop. 61.*

This second Triangle therefore (all whose sides are known from the Angles of the first) you shall resolve by the first Probleme of Oblique angled Spherical Triangles. Chap. 14. And having by that Probleme found the Angles of this second Triangle, „ know that the 2 lesser Angles of the second Triangle shall „ be severally and respectively equal to the two lesser sides „ of the first Triangle. (and the least Angle to the least side, „ the middle Angle to the middle side) and the greatest Angle „ of this second Triangle being subtracted out of 180 degr. „ shall

„ shall leave you the greatest side of your first Triangle.

Example. If the Angles be given $113\frac{1}{2}$ degr. 45 degr. and 38 degr. 51 minutes, and the sides be enquired. Draw by aime a rude Scheam of this first

Triangle, writing in the Angle A 45 degr. in B $113\frac{1}{2}$ in C 38 degr. 51 minutes, supposing these sides yet unknown: then draw under this by aime also, a

Scheam of the second Triangle, setting his Base Parallel with the Base of the first, and making the Base of the second shorter then the Base of the first. Set also B at the Vertical Angle, and A C at the Base; as in the first Triangle.

Then say, Because A in the first Triangle is 45 degr. therefore in the second Triangle B C (subtendeth A) shall be 45 degr. And because C in the first Triangle is 38 degr. 51 min. therefore in the second Triangle the side A B (which subtendeth C) shall be 38 degr. 51 min. And because B the greatest Angle in the first Triangle, is $113\frac{1}{2}$ therefore in the second Triangle the side A C (which subtendeth B) shall be the supplement thereof, viz. $66\frac{1}{2}$. Write now upon the sides of this second Triangle the quantities of the sides. so is your second Triangle ready to be resolved by the first Probleme of Oblique-angled Triangles. whereby you shall find the Angles of the second Triangle, as I have expressed them in the Scheam. A $46, 26$ min. C 40 , B 110 degrees.

Now lastly, I say the Angles of the second Triangle thus found, give me the sides of the first Triangle, which I seek, in this manner.

In the second Triangle.

A is $46. 26$.

C is $40. 00$.

B is $110. 00$.

Therefore

In the first Triangle.

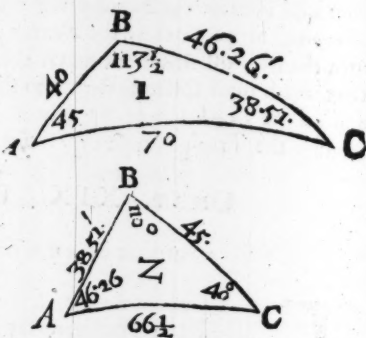
B C is $46. 26$.

A B $40. 00$.

A C $70. 00$. Supplement

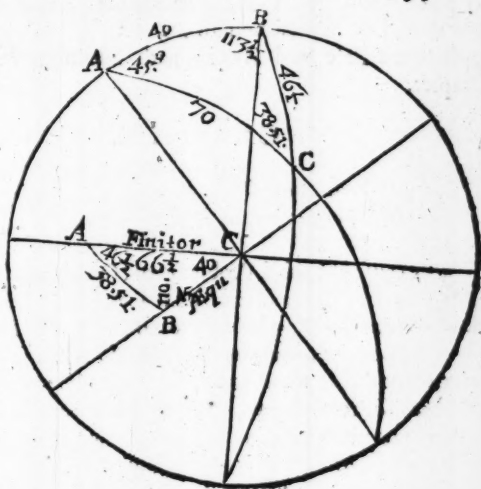
of 110 degrees. And thus by all the Angles given, we have found out all the sides, which was required.

Now would you see where this second Triangle dwells in the Plane-



Planisphere, by whose help we have found out the sides of the first? That I will now shew you; because many may be as glad to know it as I was when I first found it. Having then the Angles of your first Triangle given, and his sides also now found; place him as in the 14 Chap. A B, 40 in the *Limb*, A C 70 in the 45th Meridian. B C 46 degr. 26 min. in the 113½ *Azimuth*. Then

you shall
say, Because
the Center
of the Pla-
nisphere is
the Pole of
the arch A
B, therefore
at the Cen-
ter shall
stand the
Angle C,
which A B
subtendeth:
Next fol-
low the
113¹/₂ Azi-
muth (which



maketh B C of your Triangle) to the Finiter, and from the point where he toucheth the Finiter you shall number in the Finiter to the Center $23\frac{1}{2}$, and number on $66\frac{1}{2}$ more beyond the Center to make up 90, and there is the Pole of the arch B C. Therefore there shall stand the Angle A, which B C subtendeth. Then follow the 45th Meridian to the Equator, and thence count in the Equator 45 degr. to the Center; and 45 degr. more beyond, which make 90: there is the Pole of the arch or side A C. Therefore there shall stand the Angle B which A C subtendeth. Here you see your second Triangle made by the Poles of the first adjoining to the Center of the *Planisphere* under the Finiter: onely the side A B is wanting: To get that, prick A and B with ink on the *Matr*, if your *Planisphere* be metal; and when they be drie (if you can have patience to tarry so long,) turn about the *Reet* till some one *Azimuth* or other do cut both these pricks,

I

which

which here the 48th or 49th from the *Limb* will make a shift to do (if your *Zodiac* do not obscure one of the pricks) and in this *Azimuth* you may number between the pricks 38, 51. for the length of the side A B. Thus I have shewed you how all the sides and the Angle (C) of the second Triangle (made between the Poles of the first Triangle) may be found in his proper place where he dwells in the Sphear, below the Finiter; and how to find both these and all the rest, by hoising up this Triangle to the Pole and *Zenith*, hath also been shewed in this Chapter.

CHAP. XX.

How to reduce an Oblique angled Triangle to two Rect-angled Triangles, by letting fall a Perpendicular.

BEcause the third Probleme of Oblique angled Triangles cannot be resolved by the Canon of Sines and Tangents without letting fall a Perpendicular, and because in that case the crossing at the Angle C is oft so Oblique that you cannot define the Angular point certainly, and because in the *Method* for resolving the third Probleme one of the sides of the Triangle hapneth some times to make two interfections with the Parallels or *Almicanters*, and there may be doubt which of these interfections is to be taken for the Angle C. Although I there shewed another way to resolve that doubt, yet I will shew you also how to resolve it, and to remedie the inconveniences aforesaid, by letting fall a Perpendicular. And it shall suffice to shew you this in one example, which if you mark and be acquainted with the four first Problemes of Rectangled Spherical Triangles, you shall be able to do it in any other needfull case whatsoever. Take therefore the Triangle of Chap. 16. where we had given A B 37.45 minutes, A C 105. 41. minutes. B 167. 9 min. you must observe that the Perpendicular ought to fall from the end of a known side, and to subtend some known Angle, which here cannot be, because both the Angles at the Base A C are unknown.

Continue therefore the sides A C and B C to Semicircles, and you shall have a second Triangle N P C. in which N P is equal to A B. N C is supplement of B C. P C supplement of A C: N supplement of B. C is common to both Triangles.

Here

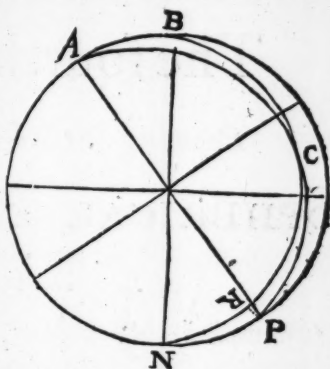
Here then in the second Triangle N P C, let the Perpendicular fall from P upon the Base N C, so have you two Rect-angled Triangles, P R N, and P R C.

In the Triangle P R N you have (beside the Right Angle R) the Angle N 12. 51 minutes, (supplement of B) and the Hypotenusa N P 37. 45 minutes; and so may

find all the rest of this Triangle, by the third Probleme of Rect-angular Spherical Triangles, viz. P R 7. 49 min. $\frac{1}{2}$ N P R 79, 49 min. and R N 37 degrees, which had,

In the Triangle P R C, by the second Probleme of Rect-angular Spherical Triangles you may find R C 70 degrees (which added to R N maketh N C 111 $\frac{1}{2}$, whose supplement is C B 68 $\frac{1}{2}$ C 8 degr. $\frac{1}{2}$, C P R 88 degr. which added to N P R maketh the whole Angle C P N 167. 47. which being subducted out of 180 degr. leaveth the supplement thereof C A B 12. 13 min. as I find it by my Planisphæar; and by exact calculation it may be 12 26 minutes.

Thus have you a perfect Method of resolving all Spherical Triangles by the Planisphæar.



The end of the Third Book,

The fourth Book.

Shewing the Solution of the

SPHERICAL PROBLEMES,

Both

Astronomical, Astrological, and Geographical,

by the

PLANISPHEAR.

CHAP. I. The Preface.

THe best method (in my judgement) for setting down the Problemes of the Sphear is, to set them in such order, that the former may be Præcognita to the latter, and the latter presuppose the knowledge of the former. This most Authors have used. But this method here aimed at, perhaps is not alwaies kept exactly. Because where one Triangle serves to resolve divers Problemes, I was willing to make an end with him sometime before I meddled with another, for avoiding the multiplicity of Chapters, and repetition of the same Schemes.

THere be in the Sphear five famous Triangles, by the knowledge whereof most *Astronomical Problemes* are resolved, insomuch that if you be but well versed in the general Problemes of *Trygonometry* set down in the former Book, and have acquaintance with these five Triangles in the Sphear, you will be able to resolve most of the following Problemes without any further help.

Of

Of those five Triangles three are Rectangled, which shall be here denominated from their *Hypotenusa's*.

1. The *Ecliptical* Triangle, whose *Hypotenusa* is an arch of the *Ecliptick*, his *Legs* are arches of the *Equator*, and a *Meridian*: he serveth especially for *Questions* of the *Suns* Longitude, Right *Ascension*, and *Declination*, with some others, See this Ch. 6 &c.

2. The *Horizontal* Triangle, whose sides, are arches of the *Horizon*, *Equator*, and a *Meridian*. He serveth especially for *Questions* of the *Suns* Amplitude, *Ascensional* difference, and *Declination*, and of the *Latitude* of your place. See this Chapter 14.

3. The *Azimuthal* or *Parallactical* Triangle, whose sides are arches of an *Azimuth*, the *Ecliptick*, and a *Circle* of Longitude: he serveth especially to find the *Moons* *Parallaxes* in *Altitude*, *Longitude*, and *Latitude*. See this Chap. 64.

4. The other two are *Oblique angled*. One I use to call the *Complemental* Triangle, because all his sides be complements, viz. the Complement of *Latitude*, of *Declination*, and of *Altitude*. He serveth chiefly to find the *Altitude*, *Azimuth*, and *Hour*. See this Chap. 24.

5. The last, I use to call the *Polar* Triangle, because one side of him is evermore the distance of the *Poles* of the *World*, and of the *Ecliptick* (23 degrees $\frac{1}{2}$) his other sides are a *Meridian*, and a *Circle* of Longitude. He serveth chiefly to find the *Longitude* and *Latitude*, the *Right Ascension* and *Declination* of the *Stars*. See this Chap. 34.

CHAP. II.

How to find the Altitude of the Sun or Stars, by Observation, with the Planispheric. Also what fashion is best for Sight.

THe *Planispheric* may here supply the office of a *Quadrant*, (which is the fittest and most common Instrument for taking *Altitudes*) For the *Planispheric* is divided into 4 *Quadrants*, and if you hang a *plumb-line* at the *Center*, it may serve any of them. Set your *Sights* to one of the *Semidiameters* of the *Mater*, and turn him so to the *Sun* that the *Sun* may shine through the *Sights*; then shall the *plumb-line* (if

it hang Parrallel to the *Planisphear*, neither bearing upon it, nor hanging off from it) shew in the lowest Quadrant of the *Limb* the degrees of Altitude. But because the Quadrants may be smal, I have shewed you a way how to make them serve your turn as well as if they were of double Semidiameter, Book 1. 10. whither I refer you.

My Sights for the Sun and Moon I have devised to make thus.

Let them be about an inch square for a *Planisphear* of a foot Diameter: And in the middle of that sight next you (which must be a thin plate) let a very smal hole be drilled quite through: in the middle of the Sight next the Sun, bore an hole as big as a Pease, or bigger, whose Center must answer the smal hole in the other Sight, then cross the Center of the hole in the Sight next the Sun with an hair, or fine thrid, so that the thrid may run level or Parrallel with the *Horizon*, when you use the Sights. When you turn the Sights toward the Sun, and the shadow of the thrid fall, upon the smal hole of the lower Sight, you shall see or hold a white paper about a span behind the lower Sight, upon which paper you shall perceive a smal Image of the Suns body, and likewise of the thrid cutting through the midst of him very distinctly. And here you shall observe that the image of the thrid moveth upon the image of the Sun in the paper, contrary to the motion of the shadow of the thrid upon the lower Sight, for when the shadow of the thrid toucheth the bottom of the Sight-hole, the image of the thrid shall touch the top of the Suns image on the paper, and contrarily. But when the shadow of the thrid cutteth the middle of the Sight-hole, then shall the image of the thrid always cut the middle of the image of the Sun upon the paper exactly and clearly. Also you shall observe that though the Diameter of the Sun be always more then 30 min. yet the Diameter of the image cannot be observed here to be much above 20 min. as you may measure by the min. of the Quadrant which the plumb-line passeth over, while the image of the thrid passeth over the image of the Sun: whither the Diameter of the Suns image on the paper be diminished by reason of the thickness of the plate through which the beams pass, or because the image on the paper is smal, the beginning and end of the Obscuration by the image of the thrid, cannot be precisely observed, for the present, I leave to Optical men to enquire: Also what is the reason why the image of the thrid moveth contrary

to the motion of his shadow, is a question of some difficulty: My resolution is, because that image is a species which passeth through the Sight-hole with the species of the Suns body: For when the shadow of the thrid falleth upon the lower part of the Sight-hole, then certainly the upper part of the Suns body is above the obscuration of the thrid, and the lower edge is Eclipsed at the Sight-hole. Now the wayes of the Suns body thus Eclipsed on the lower side, passing through the Sight-hole, must needs be there decussated, so that the wayes or beames comming from the lower part of the Sun shall make the higher part of the image on the paper, and contrarily; as appeareth when an Eclipse of the Sun is obvierved by a *Telescope*, or by a smal hole, letting the beames into a dark room: For the reason here and there is the same. I have used those Sights for the Sun and Moon almost these 20 years past, and (for ought I could ever read or hear) they are of my own invention, and I have not met with any device more commodious to me for this purpose.

For the Moon, you must set your eye to the lowest Sight-hole, and let the thrid cut the middle of her body. For the Stars, if your eye cannot discern them by the thrid, you must behold them by the edges of the Sights both above and below. Or if you would observe the Stars Altitude by some larger Instrument, I advise that the Sight next your eye be a broad plate 4 or 5 inches square, in the middle whereof you shall cut a window whose length may be near 2 inches, and his breadth or height about an inch or more, so that your eye may be well shadowed, and yet have free scope through the window to find the Star. Let the upper Sight be a Cylinder or ruler set Parrallel to the lower Sight, and his breadth be equal to the window almost, but narrower by a few minutes as 2 min. or 4 min. when you looking through this window can see the Star appear alike on both sides, the upper Sight, then is your Instrument right set, and the plumb-line shall shew you his Altitude as before. Note that for all curious observation of the Sun or Stars, your Instrument must be supported with a Tripod, or like device, that it may be steady, and that the apparent Altitudes of the Sun and Moon must be corrected according to the Table of Parrallax and Refraction. The fixed Stars have Refraction, but no Parrallax sensible. The quantity of the Parrallax is to be added, and the quantity of the Refraction to be subtracted alwayes from the apparent Altitude found, so shall you have the true Altitude.

of

Here followeth an Abridgement of *Lansbergius Tables* of Refraction and Parrallax of the Sun, as much as this Instrument may need, for the rest go to *Lansbergius* or *Tycho Brahe's Tables* at large, where you shall find the Moons Parrallax in the Horizon, to be sometimes 51 minutes, sometimes 1 deg. 7 min. at 70 degrees of Altitude, between 18 deg. 24 min. Here Refraction is as the Sun.

Alt. $^{\circ}$	Parall. mi. sec.	Ref. mi. sec.
0	2 18	34 00
5	2 18	14 00
10	2 16	8 15
15	2 13	6 00
20	2 10	4 33
25	2 05	3 12
30	2 00	1 51
35	1 53	0 54
40	1 46	
45	1 38	
50	1 29	
55	1 19	
60	1 09	
65	58	
70	47	

CHAP. III.

To finde a Meridian line.

S Trike a straight line upon a Table or any *Horizontal* plain : and lay your *Planisphear* so that one of the Diameters of the *Mae*r may lie in that line. Then take the Suns Altitude : the Altitude would be taken at least 2 hours (the more the better) before noon: and note, that if you take it between 29 and 30 degrees you shall be troubled neither with Parrallax nor Refraction, because the Suns Refraction and Parrallax be equall at the Altitude 29 degrees 26 minutes. The Altitude taken, you shall immediately lay your *Planisphear* in the posture aforesaid ; and turning the *Label* to the Sun, make a prick in the *Limb* where the *Label* cutteth : And when the Sun comes to the same Altitude after-noon, your *Planisphear* laid as before, turn your *Label* to the Sun, and where he cuts make a second prick in the *Limb*. Then divide equally the Arch of the *Limb* comprehended between the pricks : and to the middle thereof lay the *Label*, and it shall point full North and South. Look then through your Sights; and if you see any Steeple, Pinacles. Chimney, Tree, or such mark, at a good distance in the line of Vision, you may note him for a South-mark, or for want thereof set up a smaller mark neerer hand. But note also that this may best be done when the Sun is in or neer the Summer Tropick, for neer the Equator he chargeth his Declination so fast. that it may cause you an error of a few minutes, unless you make allowance for it.

Note

Note, that all lines Parallel to your Meridians are Meridians.

2. Another way.

Having taken the Altitude of the Sun, or a Star, at a good distance from the Meridian; presently lay your *Planispher* flat, and turn the *Label* to the Sun, or Star, as before. Then by the Altitude taken, get the *Azimuth*; (by chap. 24 or 27 of this book.) Then remove your *Label* (Eastward; if the Sun or Star were Westward from the Meridian; or Westward if the Sun or Star be in the East Hemispher;) so many degrees as the *Azimuth* cometh to, and your *Label* shall be in the Meridian.

3. A third way.

When the great *Wain* is seen under *Cynosura*, (the Pole Star) observe with your eye the distance of the *Thill-horse*, called *Alioth*, from the next wheel of the *Wain*. and setting that distance (by a line) in 5 parts, observe by a plumb-line when *Alioth* drawes neer to be in the same Perpendicular with the Pole Star. For when he wanteth but one of those 5 parts to come into the Perpendicular, then is the *Pole-star* in the Meridian over the *Pole* in our age: at other times of the night, the *Pole-star* may be 4 degrees wide, and in one hour neer the Meridian he changeth his *Azimuth* above one degree.

4. A fourth way.

Because the distance of the *Pole-star* from the *Pole* is now 2 degrees 30 minutes, and the *Pole* is in the circle or line which passeth from the *Pole-star* neer *Alioth*, as before; you may by guess cut off from that line 2 degrees 30 min. and in that Section you have the *Pole* at any time. This way may be used abroad in the fields, where you cannot stand upon exactness; and herein you shall miss very little, if you accustom your self to observe the distances of the Stars about the *Pole*.

CHAP. IIII.

To Observe the Azimuth of the Sun or Stars.

Lay your *Planispher* upon an *Horizontal* plain or Level, and his Meridian on the Meridian line of your Place, found by the last Chapter. Then turn your *Label* that the Sun may cast the shadow of one Sight upon the other, or directly towards it, or till the shadow of a plumb line

cut both the Sights alike, then doth the *Label* shew the *Azimuth* in the *Limb*. For the Stars, you must so direct the Sights by your eye, that their edges may touch the Visuall line that comes from the Star to your eye: and if your long Sight prove too short, turn him toward your eye, and inlightning the shorter Sight by a candle held behind you, mark where the edge of the long Sight cuts both the edge of the short Sight, and the Star; for there is your *Label* in the *Azimuth* of the Star, which you may count on the *Limb*.

Note that if you seek the *Azimuth* to get the hour, you shall find it most easily when the Sun or Stars are neer the *Horizon*: and then you shall not be troubled with their Refraction. But there is most use of observing *Azimuths* neer the Meridian, because there the *Azimuth* changeth apace, the Altitude very slowly: Yet if you may choose, choose to take Altitudes rather then *Azimuths* (so you come not within 2 or 3 hours of the Meridian) because the Sights serve all Altitudes with like facility, and you may sooner have a true plumb line any where, then a true *Horizon* all plain, and a true Meridian line.

C A A P. V.

To find the Suns Longitude.

THe Longitude of the Sun is the arch of his distance from $\gamma \circ$ in the *Ecliptick*: or it is the angle made at the Pole of the *Ecliptick* comprehended between the circle of Longitude passing through $\gamma \circ$, and another Circle of Longitude passing through the center of the Sun: for the said arch of the *Ecliptick* is always the proper measure of this Angle. And because the Suns center never hath Latitude, therefore for the Sun you shall enquire the arch; but contrarily, for the Stars which have Latitude, you shall require the Angle: and they be both (as was said) of one measure.

The Suns Longitude (Arch or Angle) is presently found by the *Ephemeris* upon the *Limb* of your *Planisphaer*, for if you lay the *Label* upon the day of the Moneth, it shall cut the degree of the Signe also in which the Sun is, and that is his Longitude: in doing whereof, you shall observe the cautions given Lib. 1. 8. to which I refer you,

Note

Note here, that the Longitude of a place in *Geographie* is the Angle at the Pole of the World, comprehended between the first Meridian (passing by the hither side of *S. Michals Island*, which is the neerest of the *Azores*) and the Meridian of the Place: and this Angle hath his measure in the *Equator*.

CHAP. VI.

The Suns Longitude, Declination, Right Ascension, any one of them given, to find the rest in the first Projection.

WHat the Suns Longitude is, hath been shewed chap. 5. His Declination is his distance from the neerest point of the *Equator*; and therefore is alwaies measured in an Arch of that Meridian which hapneth to pass through the center of the Sun, and always cuts the *Equator* at right Angles, as do all the Meridians.

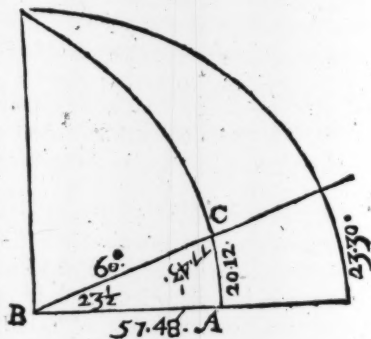
The Right Ascension of the Sun is the angle at the Pole of the World comprehended between that Side of the *Colurus Equinoctiorum* which cuts the intersection of the *Ecliptick* with the *Equator* in γ o, and the arch of another Meridian which passeth through the center of the Sun. And note, that this angle may increas above 180 degrees, even to 360 degrees, though every angle, properly so called be les then 180 degrees, and never more then 90 degrees comes into the Triangle: for if you number backwards or forwards from either of the Equinoctiall points, you shall have like arches of Right Ascension answering to like arches of Longitude and Declination; so that having found the Right Ascension in any one Quadrant, or the complement thereof, you shall find the whole Right Ascension from γ o by adding one, two, or three whole Quadrants to the Right Ascension found, or to the complement thereof, as by the view of your Planisphaer you shall presently know how to do better then by more words. Otherwise thus. The Right Ascension of the Sun is an arch of the *Equator* comprehended between the *Vernal Equinox* and that point of the *Equator* which riseth with the Sun in a right Horizon. A right Horizon is where the *Equator* passeth through the *Zenith*, and maketh right angles with the Horizon, and consequently, where the Poles have no Elevation: For from that posture of the Sphear in which the

Equator riseth upright, is the term of Right Ascension borrowed: I would, if I might, call it rather Equation; because it is numbred on the Equator, and serves for the Equation of naturall days, and may as easily be found in any Sphear as in a right Sphear, since the Horizon of a right Sphear limits the Right Ascension only because that Horizon falls in with a Meridian, and the Meridians do limit it in all parts and postures of the Equator, without any respect to the Horizon at all. But the old term hath so long injured, that I beleve it will not be changed without better Authority.

The Ecciptical Triangle.

These definitions premised, you shall know that these three arches, viz. of Longitude in the *Ecciptick*, of Right Ascension in the Equator, and of Declination in a Meridian, do make up a notable Rectangled-Triangle in the Sphear, like unto that which was made the common Example, in all the five Problemes of Rectangled-Triangles. Book 3, 3. &c.

For there B C is the Longitude (in π o) 60, degr. C A the Declination 20 degr. 12 min. B A the Right Ascension 57 degr. 48 min. A is known a right angle, B is known, the angle of the Suns greatest Declination, which for our age is 23 degr. 30 min. Now if but one of the Sides be given, you may find the other two by the Problemes of Rectangled Spherical Triangles;



But to see your Triangle, and resolve him in his proper lines, Go to the *Mater* of your Planisphaer, and take him there in the first Projection. There number 60 the Suns Longitude in the *Ecciptick* line of the *Mater* from the Center outward. Where 60 endeth, there is C of your Triangle, and the Meridian that meets you there is C A the arch of Declination; follow him to the Equator, and you shall find by his graduation he is 20 degr. 12 min. Long. thence turn in the Equator to the Center, and you make B A the Right Ascension 57 degr. 48 min. so have you the

the true picture of your Triangle in his proper place. Observe your Triangle now, and you may see A is a right angle, for at such angle all the Meridians cut the Equator. B is $23\frac{1}{2}$, for such an angle the *Ecliptick* dayly maketh with the Equator, as the arch in the *Limb* comprehended between them shewes. Now take for given any of the three Sides, and you have the rest. Take the Longitude for given (and be it 60 degr. as before, or 70 degr. or what you will) and you may find the Declination, and Right Ascension as before. Let the Right Ascension be given; then setting a needles point in the end thereof A, you may thence in a Meridian trace out the Declination C A to the *Ecliptick*, and the Longitude B C thence to the Center, every Side being divided into his whole parts or degrees. If the Declination be given, say, Because the 20th Parrallel almost must cut off C A (the arch of Declination) in C, therefore I follow the Parrallel $20\frac{1}{2}$ to the place where he cutteth the *Ecliptick*, and there comes the Meridian that serves my turn; and I may go down by him to the Equator, (as you would go down a ladder counting the rounds or degrees as you go) and so on, round my Triangle, and I need no more. For observe it when you will in the use of this Planispher, if you can find the way to go round your Triangle, you have all the Sides measured to your hand, and evermore one Angle also, most commonly two, and the angle C onely left unknown.

But admit the Sun be in Ω O, then is his Longitude 120 degrees, and he is come back from the *Solstice* in your Planispher as many degr. as he wanted of it before. Here the Triangle is equal to the former, and resolved in like manner. The Declination is the same as before: But the arches of Longitude and Right Ascension in the Triangle are supplementes of the true Longitude and Right Ascension; shewing what the Sun wants of the Longitude and Right Ascension 180, in Ω O. wherefore subtract the Base of the Triangle 57 degr. 48 min. from a Semicircle, or 180 degr. and you shall leave 122 degr. 12 min. the Right Ascension of Ω O. or number in the Equator from the Center the way in which the Right Ascension hath increased, that is first to the *Limb* (which here is *Colurus Solstitiorum*) 90 degr. then back again to A the Right angle of your Triangle, and you have 32 degr. 12 min. to be added thereto. The Sum is 122 degr. 12 min. the Right Ascension, as before: If you observe this Example,

you will easily perceive, that when the Sun is past $\triangle O$. the Triangle will be on the other side the Center, and between \triangle and γ you must add to the Right Ascension and Longitude found within the Triangle 180 degr. and in the last Quadrant between γ and γ (where the Right Ascension again increaseth inwards) you must add 270 degr. to the complement of Right Ascension found in the Triangle, and take the sum, or else subtract the Right Ascension found in the Triangle from 360 degr. and take the residue for the Right Ascension.

CHAP. VII.

To do the same in the second Projection, more easily.

IN the second Projection where the Center is the Pole of the World, and the *Limb* Equator, you shall find the *Ecliptick*, fairly drawn upon the *Reet* and distinguished into his quarters and degrees. Remember now from the former chap. that the *Ecliptick*, Equator, and a Meridian, must make your Triangle; and know that the *Label* supplieth the place of the Meridians.

If the Longitude or Right Ascension be given, lay the *Label* on the degree given (in the *Ecliptick* for Longitude, or in the *Limb* of the *Reet* for Right Ascension) and your Triangle is made, and you may presently see your desire.

If the Declination be given, consider in what quarter of the *Ecliptick* the Sun is, then number the Declination given upon the *Label* inwards, and where the numbring ends make a prick on your *Label*, then move the *Label* into the quarter where the Sun is, and lay the prick on the *Ecliptick* there, and your Triangle is made, wherein you may see the Longitude and Right Ascension desired. This needeth no Example.

CHAP. VIII.

To find the Angle at the Sun, made between the Ecliptick and Meridian.

THIS is the angle C of the former Triangle, and is the only part which cannot be found in the former posture of the

the Triangle, neither in chap. 6 nor 7, but is easily had by conversion of the Triangle, as you may remember out of the third Book.

Take the Triangle of chap. 6, and make the *Cartetus* Base, for this turn: and by the 1 or 2 Problemes of Rectangled Triangles, you may find this angle to be 77 degr. 43 min.

CHAP. IX.

To find the said angle of the *Ecliptick*, with the *Meridian*, by the *Longitude*, *Declination*, or *Right Ascension*, divers other wayes.

IN the Meridional Projection do thus.

If you have the *Longitude* given, count the distance of the Sun in that *Longitude* from the next *Equinoctial* point, and count so many degrees in the *Arctick* Circle from the *Limb* inwards: to the end of this numbring, lay the *Label*, and between the *Label* and *Equator* you have upon the *Limb* the lesser angle made between the *Ecliptick* and *Meridian*; the greater angle is the supplement thereof. Also between the *Arctick* Circle and the *Limb* you may find the *Declination* on the *Label*, which is more then was required.

If you have the *Declination* given, count it on the *Label* inwards, and make a prick where the number ends, then turn this prick upon the *Arctick* Circle, and the *Label* sheweth the lesser angle in the *Limb*, as before.

Example. I would know what angle the *Meridian* that curteth the Sun in 89 degr. maketh with the *Ecliptick*. I number therefore in the *Arctick* Circle from the *Limb* inwards 39 deg. and to the 39th degr. I lay the *Label*, and it sheweth in the *Limb* the angle sought 71 degr. 20 min. and in the *Label* the *Declination* of 89 degr. viz. 14.32 minutes: this is a good way. But that the *Label* at this 39th degr. curteth the Pole of the *Ecliptick* (as Mr. *Blagrove* saith Book 3, 40.) is not true: either Mr. *Blagrove* or the Printer here mistakes. For the Pole of the *Ecliptick* lies 14.24 minutes nearer the *Axletree*, as you shall find in the next rule.

2. Another way. Mark what is the *Right Ascension* of the point proposed, being counted from the next *Equinoctial* point (as of

89 degr. the Right Ascension is 36.36 min.) count so many degrees in the *Arctick* circle from the Axeltree: at the end of this number is the Pole of the *Ecliptick*. Lay the *Label* to him, and you shall make a Quadrantal Triangle, whose Sides shall be equal to the Angles of the former Triangle, which was made of the Longitude, Declination, and Right Ascension, of the point proposed: for the Right Angle you have a Radius or Quadrant of the Axis: for the Angle of the greatest Declination between the Equator and *Ecliptick* $23\frac{1}{2}$, you have the arch of a Meridian between the Pole of the Equator and the Pole of the *Ecliptick*: for the angle sought, you have the arch of the *Label*, between the Pole of the *Ecliptick* and the Center 71.20 minutes; as before: the least angle of this Quadrantal Triangle is at the Center, and you shall find his measure in the *Limb* 14.32 minutes: that is the measure of the least Side of the former Triangle, viz. the Declination of the point proposed.

Here you see, If the Declination had been given, you should have set it in the *Limb*, between the Pole and the *Label*, and so had you made the same Quadrantal Triangle, and might have found on the *Label* between the *Arctick* Circle and the Center the measure of the angle sought: and likewise in the *Arctick* Circle between the *Label* and the Axtree-line the Right Ascension, though it be more then was required. The reason hereof you may learn from Book 3. 7.

CHAP. X.

To find the point of the Ecliptick in which the Longitude and Right Ascension have greatest difference.

Move the *Label* on the Polar circle till you find the degrees of the *Label* between the Polar circle and the *Limb* to be equal to the degr. of the *Limb* between the *Label* and the Pole, so have you a Rectangled æquicrural Triangle made by the *Limb*, *Label*, and the Meridian $46\frac{1}{4}$; like to that in the second Variety, Book 3. 10.

Here the angle B at the Pole between the $46\frac{1}{4}$ Meridian and the *Limb*, is equal to the Longitude of the point sought $46\frac{1}{4}$, and either Leg is equal to the Declination thereof $16\frac{1}{4}$: Therefore I conclude, that when the Sun is $46\frac{1}{4}$ in Longitude, (that is in $\approx 16\frac{1}{4}$) then

then his Longitude hath furthest out run the Right Ascension. Subtract now the Right Ascension of \propto $16^{\circ} \frac{1}{2}$, which is $43^{\circ} \frac{3}{4}$ out of the Longitude $46^{\circ} \frac{1}{2}$; there remains $2^{\circ} \frac{1}{2}$; which being converted into Time, is 10 min. the greatest inequality of Ascension in a Right Sphaer.

C H A P. II.

To find the Latitude of your Place, or the Elevation of the Pole above your Horizon, by the Meridional Altitude, and Declination of the Sun. Meridional Projection.

Geographers call the distance of a place from the nearest point of the Equator upon Earth, the *Latitude of that Place*, as the Latitude of London is 51° deg. 32 min. from the Equator Northward: the Latitude of *S^t Thomas Island* upon the coast of *Africk* is 0° deg. 0 min. because the middle of that Island lyeth under the Equator. And because the Latitude of your Place, and the Elevation of the Pole above your Horizon, are alwaies equal, therefore the Elevation of the Pole is oft called *Latitude of the Place*, or *Latitude* simply: and so for brevity sake we shall often call it. But when we speak of the Latitude of the Moon or Stars, you must understand Astronomers thereby mean their distance from the nearest point of the Ecliptick.

To find the Latitude of your Place, get the Suns Declination, by the 6 or 7th. and his Meridian Altitude by the second of this Book: Then find the parallel of the Suns Declination, North or South as the Declination is, and where it toucheth the *Limb* (here Meridian) there is the point where you observed the Sun at Noon; set the South end of the Finiter so many degr. below this point as the Meridian Altitude had, then is your Finiter set to your Latitude, and you shall find the measure of it between the Equator and the *Zenith*, (which is properly the Latitude) and the same measure shall you find between the North point of the Finiter and the North Pole, where it is more properly called the *Elevation of the Pole*.

Example. June 20 1651. I observed the Meridian Altitude of the Sun, here at *Edon*, four miles Eastward from *Norhampton*, 60° deg. 59 min. the Longitude of the Sun was then \propto 8° deg. 19 min. $\frac{1}{2}$; his Declination 23° deg. 14 min. Northward, There-
L fore

fore having found in the *Limb* the point where the Parallel 23 degr. 14 min. toucheth above the Equator, I put the South end of the Finner 60 degr. 59 min. below that point, toward the South Pole, which done, I see the North Pole Elevated above the Finner 52 degr. 15 min. and the *Zenith* of my Horizon likewise to be removed from the Equator Northward 52 degr. 15 min. which is the Latitude of *Elton*.

Note that you may best observe the Latitude when the Sun is near the *Summer Tropick*; for then you shall not be troubled with Refraction; and then the Declination varyeth slowly; which varyeth almost one minute every hour near the Equinoctial.

CHAP. XII.

To do the same by the Meridian Altitudes of the Stars about the Poles.

MAny of the Stars near the Northern Pole may be seen with us twice in the Meridian in one Winters Night: that is, one while above the Pole, and 12 hours after again below the Pole. As for Example, the Pole-star, called *Abrucabe*, about *December* 18 will be in the Meridian above the Pole at 6 of the clock at Night, and at 6 next morning he will be in the Meridian below the Pole.

Observe both the Meridian Altitudes, and add them together, half that sum is the Elevation of the Pole. Example. I observed at *Elton* the greatest Altitude of the Pole-star to be 54 deg. 45 min. and his least Altitude 49 degr. 45 min. the sum is 104 deg. 30 min. the half 52 degr. 15 min. the Latitude of *Elton*: and here I have gotten also the Pole-stars distance from the Pole, and consequently his Declination which is the complement thereof, for the Latitude being subducted from the greater Altitude leaves the Stars distance from the Pole 2 degr. 30 min. and consequently shewes his Declination to be 87 degr. 30 min. which is 39 min. more then *Gemma Frisius* observed it, *Anno Dom.* 1547. for in our age the Pole-star approacheth about 1 min. nearer the Pole in every 3 years.

Note that these Stars which are distant from the Pole less then the Latitude, and more then the complement thereof, have their

less Meridian Altitude in the North part of the Meridian, and their greater Meridian Altitude in the Southern part of the Meridian beyond the *Zenith*. Wherefore for them you shall take the complement of their greater Altitude, and add it to the North Quadrant of the Meridian, and if to that sum you add the lesser Altitude, the half thereof shall be your Latitude. But the nearer any Star is to the Pole, the fitter for this purpose, and therefore none better then *Alrucabe*, who is the nearest of all.

CHAP. XIII.

To find the Declination of the Sun or Stars, by their Meridian Altitude, and the Elevation of the Pole.

THis is done by the first, made of the Meridional Projection, where having set your Finiter to the Elevation of the Pole, or your *Zenith* to the Latitude, (for as hath been shewed Chap. XI. all comes to one, and in doing either, you do both) and having observed the Meridian Altitude of the Sun or Star, number the Altitude observed upon the *Limb* of the *Reet* on the South or North side of the Pole, according as the Star was observed to be, and there shall meet you on the *Mater* his Parallel of Declination.

Example. I observed the Suns Meridian Altitude at *Elton*, 20 deg. I look therefore where the 20th *Almicanter* toucheth the *Limb*, (the Finiter first set to the Latitude) and there meets at the *Limb* the $17\frac{3}{4}$ Parallel below the Equator: wherefore I say, the Sun declineth 17 degr. 45 min. Southward. Again, I observed the Star *Alhaiot* in the North part of the Meridian 6 degr. 42 min. high, I go to that *Almicanter* in the North quarter of the *Reet* under the Pole, and there meeteth at the *Limb* the Parallel 45 min. $\frac{1}{2}$ of North Declination.

CHAP. XIV.

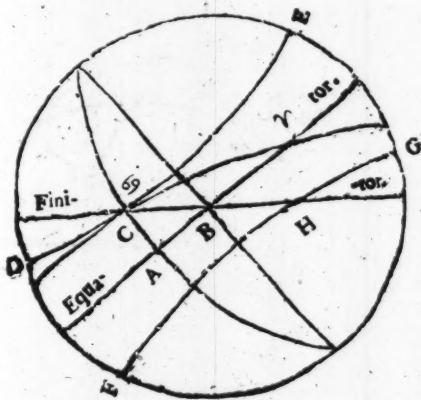
To find the Oblique Ascension and Descension, and the Ascensional difference of the Sun or any Star: by his Declination, and the Latitude of the Place, Two severall wayes, in the Horizontal Triangle.

THe Oblique Ascension is the arch of the Equator which riseth with the Sun or any Star in an Oblique Sphear, that is, a Sphear wherein the Equator maketh an Oblique Angle with the Horizon. This arch beginneth alwayes from the Vernal Equinox, but we seek the latter term or end thereof. To find this by Calculation, we use to find first the Ascensional difference, that is the difference of the Right and Oblique Ascension, or the arch of the Equator comprehended between the latter termes of the arches of the Right Ascension and Oblique Ascension of the Star, this difference for North Stars, we subtract from the Right Ascension, and the remainder is the Oblique Ascension; but for South Stars we add it to the Right Ascension to make the Oblique Ascension: and for Oblique Descension or Setting, contrarily, we add the Ascensional difference for North Stars, and subtract it for South: you shall see all plain in the Meridional Projection of the Planispher, and the first Mode thereof, where the Finiter is set to the Latitude.

Example. I would know the Oblique Ascension of the Sun in \odot and the Ascensional difference. The Declination of the Sun in \odot is 23 degr. 30 min. our Latitude 52 degr. 15 min. I go to the North Parallel 23 degr. $\frac{1}{2}$, which is the *Tropic* of Cancer, on the *Mater*, and following him to the Finiter, there I turn in the Meridian which cutteth there, and go down to the Equator under the Horizon, and make a prick here; I say, is the Right Ascension of the Sun in Cancer 03 ; for the same Meridian cutteth both these, and therefore both these points would rise at once in a Right Sphear, where the Meridians by turns successively, become Horizon: but counting how many degrees are between this prick and the rising point of the Equator, I find 34 degr. 10 min. this is the arch of Ascensional difference, which being subtracted out of the Right Ascension of \odot (which by Chap. 6 is 90 degr.) there remaineth the Oblique Ascension 55 degr.

degr. 50 min. And the meaning is, that whereas the Sun being in ☉ in a Right Sphear, riseth with the 90th degree of the Equator, in our Latitude, he riseth with the 55 degr. 50 min. of the Equator: the difference of these Ascensions is 34 degr. 10 min. add this difference to the Right Ascension of ☉, and it maketh 124 degr. 10 min. the Oblique Descension, for the 124th degree of the Equator setteth with ☉, and the point of the Suns Right Ascension shall in North Signes Set before him as much as it Riseth after him, and in South Signes shall Set after him, as much as it Riseth before him. This you may see plainly by the view of this Projection; if you imagine it one while to be the Eastern Hemisphear, and another while the Western Hemisphear, at your pleasure.

The Horizontal Triangle.

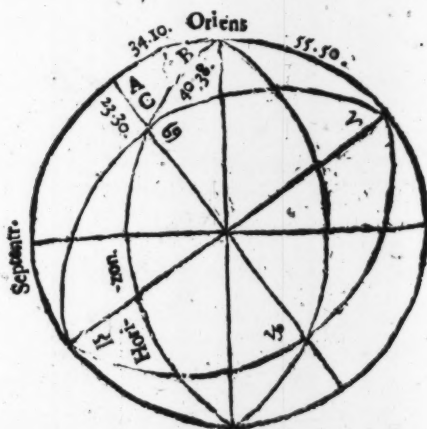


Take in the Scheme of the Horizontal Triangle annexed, so many Circles of your *Planisphear* as you shall use for this purpose, and moreover see here how the *Ecliptick* should lie in your *Planisphear* when ☉ is rising, which the *Planisphear* in this posture cannot express.

- ☉ Is the arch of the Suns Longitude 90 degr.
- ☉ A Is the arch of the Suns Right Ascension 90 degr.
- ☉ B Is the arch of the Oblique Ascension 55 degr. 50 min.
- B A Is the Ascensional difference 34 degr. 10 min.
- A B C, I cal the *Horizontal Triangle*.

The same way serveth for the Stars, for the Stars Parallel of Declination followed to the Finiter, shall bring you to C of the Triangle, as the Suns did; and then you know what to do.

A second way and more easie and pleasant, is by the Equinoctial Projection. Place the Sun or Star upon the East part of your Horizon, (in the North-east quarter, if the Declination be North; but in the South-east quarter, if the Declination be South; as you had direction, Book 2, 2.) and the degrees of the *Limb* by which γ 0 is gone past *Oriens*, or the six a clock line of the *Mater*, are the degrees of Oblique Ascension, subduct this out of the Right Ascension, if the Star be North, or out of this subduct the Right Ascension, if the Star be South, and the remainder is the Ascensional difference. But this subduction is made to your hand in the *Planisphaer*.



Take the former Example. The Latitude here is 52 degr. 15 min. the Suns Declination in \odot 0, is 23 degr. 30 min. as before. Now See in this second figure of the Horizontal Triangle A B C, how the Circles lie in the *Planisphaer*, set \odot 0 on the North-east part of the Horizon at C, and you have before your eyes.

γ \odot the Suns Longitude.

90 degr.

γ A the Suns Right Ascension.

90 degr.

γ B the Suns Oblique Ascension.

55 degr. 50 min.

B A the Ascensional difference.

34 degr. 10 min.

C H A P.

CHAP. XV.

The Ascensional difference, Declination, and Amplitude, of the Sun or a Star, and the Latitude of the Place, any two of them given, to find the rest.

The Amplitude or Ortive Latitude is the arch of the Horizon between the rising-point of a Star and the full East point. This is the *Hypotenusa* of the Horizontal Triangle, expressed in both the Schemes of the former Chapt. Now I told you Book 3. 2. that if any two parts of a Rectangled Triangle be given with the Right angle, the rest may be easily found; observe then your Triangle A B C in the first Scheme of the former Chapter, and likewise in the Meridional Projection of your *Planisphere*, you shall see the very same. For the Finiter being set to the Latitude, C shall be where the *Tropick* of Cancer cuts the Finiter: the arch of the Meridian between C and the Equator is C A and the Declination: thence in the Equator to the center is A B the Base, and the Ascensional Difference B C in the Horizon is the Amplitude; B is the complement of Latitude; A is 90^o degr. C is unknown, and we need it not, else, if you have read the third Book, I hope you can find him.

Here are six Cases.

1. Admit now that the Declination and Amplitude be given, put the term of the Amplitude (I mean the point where it ends, counting from the Center) upon the Parallel of the Declination, and your Triangle is formed, and thereby the Ascensional difference and the complement of Latitude are discovered.

2. Or if the Declination and Ascensional difference be given, number the Ascensional difference from the Center downwards in the Equator: Then go up in a Meridian as many degrees as the Declination comes to, and to the point where you end (which is C) set the Finiter, so he is placed to your Latitude, and the Amplitude also is shewn.

3. Or if the Declination and Latitude be given, the Finiter being set to the Latitude, follow the Parallel of Declination to the Finiter

Finiter there is C, thence go down by a Meridian to A in the Equator, thence in the Equator to B at the Center, thence turn by the Finiter to C, and you have compassed your Triangle, and therefore have all known but C.

4. If the Latitude and Ascensional difference be given, the Finiter being set to the Latitude, count from the Center in the Equator to the end of the Ascensional difference, there is A: Go up thence in a Meridian to the Finiter; there is C: Go thence in the Finiter to the Center: there is B.

5. If the Latitude and Amplitude be given, the Finiter being set to the Latitude, count from the Center (B) in the Finiter to the end of the Amplitude (where shall be C) go down thence in a Meridian to the Equator, (where is A) thence in the Equator return to the Center B.

6. If the Amplitude and Ascensional difference be given, prick the end of the Amplitude numbred in the Finiter from the Center, and prick the end of the Ascensional difference, numbred in the Equator from the Center: then turn about the Reet till some one of the Meridians cut both these pricks, and that shall make up the Triangle.

Note, that for South Stars, or the Sun in South Signes, this Triangle lies on the South-side the center, and above the Finiter; but for North Signes it lies North of the center, and below the Finiter.

CHAP. XVI.

To do the same in the Equinoctial Projection.

Here serves the second figure of the Horizontal Triangle in Chap. 14. where B A is the Ascensional difference; C A the Declination, B C the Amplitude, B complement of the Latitude.

If the Latitude and Declination be given, number the Declination on the Label inwards, and at the end make a prick, turn this prick to the Horizon of the Mater, and so shall the outward arch of the Label, be C A, the shorter arch of that Horizon B C, and an arch of the Limb B A of your Triangle.

If the Latitude and Amplitude be given, do as in this Example. I observed *Sirius* to rise $27\frac{1}{4}$ from the East South-ward
my

my Latitude is $52^{\circ} 4'$. I go to the $52^{\circ} 4'$ Meridian on the *Mater*, reckoned from the Center on the South-side, because the Star is Southern, as his rising shewes. This $52^{\circ} 4'$ Meridian being my Horizon (as Book 2.2.) I number in him the Amplitude of *Sirius*, from *Oriens* toward *Meridies* $27^{\circ} 1'$, and thereto I lay the *Label*; and I see my Horizon cuts the *Label* in $16^{\circ} 1'$, that is C A the South Declination of *Sirius*: and between the *Label* and *Oriens* in the *Limb*, I have B A $22^{\circ} 1'$, his Ascensional difference. If you can do these two, you may resolve the four other Cases of this Chapter with like facility. View but the Scheme in the Book, and in your Planisphere, and that alone will instruct you.

CHAP. XVII.

To find the Semi-diurnal and Semi-nocturnal Arches of the Sun or Stars: the time of their Rising and Setting: and the length of their Day and Night: by Declination, and the Latitude of the Place.

S Et the Finiter to the Latitude, (as in the first Mode of the Meridional Projection,) Then seek the Parallel of the Declination of the Sun or Star, North, or South, as it hapneth to be. That Parallel shall be divided by the Finiter into two arches: the arch above the Finiter is the *Semi-diurnal* arch, in which you may count the time of Rising and Setting, and the Length of the Day: that below is the *Semi-nocturnal* arch, in which you may reckon the length of the Night; or if your Question be of a Star, the time he spends under the Horizon.

Example. In the first Scheme of the 14th Chapter, D E is the *Tropic of Cancer*, that is the $23^{\circ} 1'$ Parallel of North Declination: C E is the *Semi-diurnal* arch: C D the *Semi-nocturnal*. And you shall find in the Meridional Projection of your Planisphere those arches are divided by the Meridians; and the arch C E containeth $124^{\circ} 10'$, which turned into houres and minutes, (accounting every degree 4 minutes of Time, and every 15 degrees an houre,) is 8 houres 16 min. 40 sec. half the length of our longest Day, and the arch C D containeth $55^{\circ} 50'$, that is, three houres 43 min. 20 sec. half the length of our short-

est Night: therefore at three hours 43 min. after midnight the Sun Riset in the *Tropicke*, and sets so much before midnight, that is, at eight hours 16 min. 40 sec. and so may you find your desire in any other Parallel.

Example. 2. I observe that *Fomahant* his Meridian Altitude is but 6. 30 min. therefore by Chap. 13 he declineth Southward 31 $\frac{1}{2}$. I would know how long he shines with us; and I presently see in the Meridional Projection of my Planisphere, that his Parallel hath but 38 degr. above the Horizon; that is, he will set two hours 32 min. after he is South; and the whole time he shines in our Horizon, is five hours four minutes.

Example. 3. *Lyra* her Declination is 38. 30 min. North; and I see his Parallel comes within 45 min. of the Horizon, in the North part of the Meridian, but never toucheth it: therefore I conclude that *Lyra* never sets with us at all.

CHAP. XVIII.

To find the same, in the Equinoctial Projection.

TURN about the *Reet* till the Suns place in the *Ecliptick*, or the point of the Star, touch your proper Horizon: and that on the North side, if the Declination be North, or on the South side, if it be South. Lay the *Label* to the Sun or Star in the Horizon, and between the *Label* and *Meridies* upon the *Limb* you shall have the *Semi-diurnal* arch, both in degrees, and in hours and minutes. And you shall observe that those Stars whose Declination is greater then the complement of your Latitude (as *Lyra*'s was in the last Chap.) will never touch the Horizon at all. For Stars of such Declination, if they be North, never set; and if they be South, never rise at our Town.

But what shall I do if the Star be not in my *Reet*? Then will I number his Right Ascension on the *Limb* of the *Reet*, and having thereto laid the *Label*, I will number his Declination upon the *Label* from the *Limb* inwards, and where it ends make a prick by the edge of the *Label*, in the *Reet*, for him: for there is the place of the Star: but if the Stars place happen to be in a window of the *Reet*, where the *Reet* is perforated, then I will make the prick upon the *Labels* edge at the Stars Declination, and

and turn that prick to the Horizon. I may pinch the *Label* close with the *Reet*, and turn both together, which will be the handfomer way, but if I move the *Labels* prick alone to the Horizon, it is sufficient for this Probleme, which needeth no more words.

CHAP. XIX.

To find the beginning and end of Twilight, by the Suns Declination, and the Latitude of the Place.

S Et the Planispher in the first Mode of the Meridional Projection; then turn the Planispher that the *Zenith* may be downwards, and the *Almicanters* mostly below the Horizon. Then goto the 18th *Almicanter* below the Horizon: and wheresoever the Parallel of the Suns Declination doth cut that *Almicanter*, there is the beginning and end of Twilight: and because every Parallel is divided by the Meridians into 12 hours, or 180 degr. (every 15 degr. being one hour) therefore you may easily count how far the point where Twilight begins, is distant from Midnight, or from Noon, or from Sun-rise, or Sun-set in the Horizon.

Example. In our Latitude 52 degr. 15 min. my Planispher set as aforesaid, I find that where the 18th *Almicanter* cutteth the Equator under the Horizon, there cutteth also in the same intersection the 30th Meridian, or second Hour Circle from the Axis and Center; by which I gather, that when the Sun is in the Equator, the twilight begins two hours before 6 or Sun-rising, and ends likewise at 8 of the clock at Night, the Sun then setting, (as you may see) at 6. Likewise where the Winter *Tropick* cuts the 18th *Almicanter*, there cuts also the first Meridian from the Axis South-ward; shewing that in the depth of Winter Twilight begins 4 minutes after 6 in the morning, and lasteth till 5 hours 56 minutes after-noon. Likewise I see that about the beginning of π where the Sun declineth North-wards about 20 degrees, the Twilight lasts till mid-night, and that from that time till the Sun comes to \mathcal{N} (that is, from May 11 to July 11, or thereabouts,) we have no dark night at all, unless the Skie be Cloudy, for in all that time the Sun is never found above 18 degrees under the Horizon.

CHAP. XX.

To find the time of the Cosmical Rising and Setting of the Stars, by their Declination and Right Ascension, and the Latitude of the Place.

A Star is said to rise *Cosmically* when he riseth at the same instant with the Sun.

To find it, use the Equinoctial Projection: Turn the Star (being found in your *Reet*) to the East part of your Horizon, and look what degree of the *Ecliptick* cutteth the same East part of your Horizon; for when the Sun comes to that degree, the Star and Sun shall rise both together. If the Star be not in your *Reet*, put him in wick ink, as you put in the rest, Book 17. if his place light upon a window, or hole of the *Reet*, prick him on the edge of the *Label*, and hold *Reet* and *Label* close together, while you turn him to the Horizon.

Example. *Sirius* I have among 40 other principal Stars in my *Reet*, and would advise you not to be without him, for he is a little Sun in a Winters Night, to tell you how the time passeth; he is called by the *Latines* both *Canis*, and *Canicula*; for they had no name for the little *Dog*, but called him by the Greek name *Procyon*, as *Pliny* witnesseth *Lib. 18 Chap. 28*: yet I have seen a late Writer, who takes upon him to teach the *Colledge* of *Physicians* both *Physick* and *Astrologie*, before he hath well learned either of them: who in his *Obtrecations* upon the *Pharmacopœa Lond.* in the Chapter of *Vinum Scilliticum Gale- ni*, betrayes his ignorance herein, as elsewhere in 100 other things, which I could shew; for in that very Chapter pag. 147 of his fourth Impression, in 24 short lines he commits 5 absurd errors. 1. He makes it doubtfull whether *Canis* be to be taken for *Sirius*, or *Procyon*. 2. He goeth about to teach *Galen* where *Squills* grow; and that there is no hilly ground near the Sea. 3. He supposeth that the *Acronyca* rising of the *Dog* (which hapneth in the depth of Winter) is a fitter time to gather *Squills*, then the *Heliacal* rising, which hapneth near unto the *Cosmical*, in the heat of Summer. 4. He either supposeth that *Squills* grow in the Parallel of *London*, or that by the rising of the *Dog* at *London* men should gather *Squills* in *Greece* or *Spain*. 5. He

5. He tells the *Colledge* that both the *Dogs* are between the Equator and the South Pole, which indeed is newes, if it were true. Let the ingenuous Reader pardon this digression, and I proceed.

This *Sirius* I brought to our Horizon, (the 52 $\frac{1}{2}$) and found that there riseth with him in the *Ecliptick* Δ 18 $\frac{1}{2}$: in like manner, with *Procyon* riseth Δ 6 $\frac{1}{2}$: therefore *Sirius* riseth *Cosmically* with us *August* 1: and *Procyon* 12 dayes sooner. But in *Greece* and *Spain*, in the Latitude 38 degr. *Sirius* riseth with Δ 4 $\frac{1}{2}$, that is a fortnight sooner.

A Star is said to Set *Cosmically*, when the Sun riseth at his setting. Place the Star therefore on the West part of your Horizon: then look what degree of the *Ecliptique* riseth in the East part; for when the Sun comes to that degree, the Star shall set *Cosmically*.

Example. I brought *Sirius* to the South-west part of our Horizon, where he useth to set. And in the South-east part I saw m 23 degrees in the *Ecliptique* rising: therefore when the Sun is in m 23. (which is about *November*, 5. then shall *Sirius* set *Cosmically*. But at *Athens* in Lat. 37 $\frac{1}{4}$.

His *Cosmicall* (Rising is \odot in Δ 4. *July* 17
Setting is \odot in γ 9. *Nov.* 20

The *Pleiades* in our Lat *Cosmically* (Rise. \odot in δ 12 $\frac{1}{2}$ *Apr.* 22.
Set \odot in m 29 $\frac{1}{2}$ *Nov.* 11.

At *Athens* *Cosmically*. (Rise \odot in δ 19 $\frac{1}{2}$ *April* 30.
Set \odot in m 27 $\frac{1}{2}$ *Novem.* 9.

Arcturus in our Lat. *Cosmically*. (Ri. \odot in ϵ 0 *Sep.* 13.
Set. \odot in ζ 4 *June* 15.

At *Athens* *Cosmically*. (Rise \odot in ϵ 10 $\frac{1}{2}$ *Sept.* 23.
Set \odot in π 6. *May* 17.

CHAP. XXI.

To find the time when any Star riseth or setteth Acronically, by his Declination, and Right Ascension, and the Latitude of the Place.

When a Star Riseth just at Sun-setting, he is said to rise *Acronically*. To find the time, turn the Star to the East part of the Horizon in the Equinoctial Projection

jection, and mark what degree of the Ecliptique descendeth in the West: for when the Sun comes to that degree, the Star shall rise *Acronically*.

Example. When *Sirius* toucheth the South East Quatter of our Horizon, I see \approx 18. setting. Therefore when the Sun is in \approx 18, *Sirius* riseth *Acronically*.

A Star setteth *Acronically*, when he setteth with the Sun. To find the time, place the Star setting, in the West-part of the Horizon, and see what degree of the Ecliptique setteth with him: for when the Sun is in that degree, the Star shall set *Acronically*. Thus in our Latitude.

Sirius Acronically. { Riseth \odot in \approx 18. Jan. 27.
Seteth \odot in \approx 23. May 3.

At Athens *Sirius Acronically.* { Ri. \odot in \approx 4. Jan. 13.
Set. \odot in \approx 9. May 20.

Pleiades Acronically. { Riseth \odot in \approx 13. Octo. 26.
Seteth \odot in \approx 29 $\frac{1}{2}$ May 10.

At Athens *Pleiades Acronically.* { Riseth \odot in \approx 19 $\frac{1}{2}$ Nov. 1.
Seteth \odot in \approx 27 $\frac{1}{2}$ May 8.

Arcturus Acronically. { Riseth \odot in \approx 10. March 10.
Seteth \odot in \approx 4 Dec. 15.

At Athens *Arcturus Acronically.* { Riseth \odot in \approx 10 $\frac{1}{2}$ Mar. 20.
Seteth \odot in \approx 6. Nov. 18.

CHAP. XXII.

To find when a Star riseth or setteth *Heliacally*.

A Star riseth *Heliacally* when he getteth out of the beames of the Sun, and beginneth to be seen in the East a little before Sun rise. And a Star is said to set *Heliacally* when he getteth into the beames of the Sun, and beginneth to be least in the evening by reason of the Suns approach to him. Those Stars which you see nearest the East Horizon in the Morning Twilight are *Heliacall* Risers; and those which you see nearest the West part of the Horizon, in the evening Twilight are *Heliacall* Setters. For this no exact rule can be given, for all men have not like quickness of sight, nor all Stars like brightness, nor all Climates, Countries and Dayes of the Year the same clearness of Air. And the Moon oft times augment

menteth the Twilight, when she is within a few dayes of the Change, and keepeth the Stars longer Combust. Commonly about twenty dayes before their *Acronicall* setting they come within the Sun beames, and so set *Heliacally*, and they appear again, (that is, rise *Heliacally*) about twenty dayes after their *Cosmicall* rising. But if they be great Stars, the Air clear, your sight good, the angle made between the *Ecliptique* and the Horizon great, they may appear sooner: and later in the contrary Cases. According to this rule the *Pleiades* set *Heliacally*, now at *Aithens* ☉ in 8 7. and rise *Heliacally* ☉ in 11 9. so they should be Combust there 32 dayes; but because they be Stars of less Magnitude, we may perhaps allow them 40 dayes as *Hesiod* did in his time, in the beginning of his Second book of Weeks and Dayes. *Ἀδ δὲ τοι νύκτας το ἤματι ταραχόσι κακὸν οἶον.*

CHAP. XXIII.

To find the Age when any Astrologer lived, and what time of the Solar year the Seasons hapned in his Country, by knowing his Latitude, and the Rising of any Star in his time.

THe old *Grecians*, and after them the *Latines*, before *Julius Caesar* especially, designed the Seasons of the Year by the rising and setting of some notable Stars. *Hesiod* begins his second book of Weeks and Dayes: with this *Georgical Canon*.

Πλειάδων Ἀπλάγαντων ἑκαταλομήνων
Ἄρχει δ' ἄμωσιν, ἀετοῖο δ' ἀνατομῆων. That is, when the *Pleiades* rise, begin to Mow, and to Plow when they set; And in the same Book *Vers.* 182. he saith

Εὖτ' ἂν δ' ἰξήκοιτο μὲν τρυγὰς ἡλίωιο
Χαμῖνι ἑκατέσσῃ Ζεὺς ἡμάδα, δὴ ῥα τέτ' ἀσῆς.
Ἀρχὴ δ' ὅτε, περὶ πτόν ἱερὸν ῥέον ὠκεανοῖο
Πρῶτον παμφάνων, ἀνατέλλειαι ἀκρονόφαιον.
Τὸν δὲ μετ' ἰερὸν Πανδρονὸς ἄρτο χιλιδῶν.
Ἔς θά σ' ἀνδράπης, ἕξ θ' ῥέας ἰσαμόμοιο. That is, 60 dayes after the Winter *Tropique* *Arcturus* riseth *Acronically*, and then appears the Swallow, the Spring being then new begun.

These and the like rules were the Husband-mans Almanack.

by which they measured the Solar Year, and the return of the Seasons. For in their Civill Year, consisting of Lunar Moneths, by reason of an intercalary Moneth which was added every third Year, and somewhat oftner, the Seasons could happen upon the same day of the moneth yearly, but sometimes 2 or 3 weeks sooner or later, as our moveable Feasts do. The rising and setting of the fixed Stars keep the same distance Yearly, from the Equinoctial and Solstitiall points, for a mans age near enough; but longer those rules cannot last without some perceivable error: for in 100. years the Stars go forward in Longitude, according to *Tycho*, 1 degree 25 minutes, by reason whereof the risings and settings of the Stars happen later in the Year, about a day and half every 100 years in the same Latitude.

Now if you would note in what Age a Star had such a rising or setting, in such a Latitude, as for Example. In what age *Arcturus* rose 60 dayes after mid-winter in the Latitude of *Asera* in *Bæotia* near *Athens*, whose Latitude is 37° , and consequently how long since *Hesiod* lived, in whose dayes *Arcturus* had such rising, you shall reason thus: 60. dayes after the Winter *Tropicke* the Sun is in $\propto 1$ degree by the *Ephemeris* for in those 60 dayes near his *Perigium* he goeth about 61 degrees. I am therefore to seek when *Arcturus* did rise at *Athens* with the opposite degree of the *Ecliptique*, $\propto 1$ degree (the Sun is in $\propto 1$ degree, then setting over against it.) I seek the Longitude and Latitude of *Arcturus*, and find in *Tycho's* Tables that *Anno Domini*. 1600. *Arcturus* had Longitude ≈ 18 . 39 minutes, Latitude B. 31.02 . minutes: then I will suppose that *Hesiod* lived 830. years before Christ (for there some *Chronologers* place him, but without any good proof that I find) that is, 2430 years before *Anno Domini*. 1600. in which space of time *Arcturus* must have increased his Longitude by *Tycho's* *Hypothesis* 34 degrees 25 minutes, which being subducted out of the Longitude which *Arcturus* had *Anno Domini*. 1600. leaves his Longitude for the year before Christ 830. $\propto 14$. degree 14. minutes, his Latitude was then and ever 31.02 minutes. Now from this Longitude and Latitude, I get his Right Ascension, and Declination, by Chap. 34. of this Book, where I find Ascension 180. degrees, Declination North 34 . degrees 15 minutes: those had, I place *Arcturus* in my *Reet* according to that Right Ascension and Declination (as was taught Book 1 7. and Book 4.

18.) and by Chapter 21. I find m 4 rising with him; and at the same time \times 4. setting in the same Horizon of *Athens*. But I ought to find \times 1 degree. setting in *Hesiods* time. Therefore I will suppose again that *Hesiod* lived 1120 years before Christ: and proceeding as upon the former supposition, I find that then m 29. degrees did set at his *Acronical* rising: but I ought to find \times 1 degree rising. And seeing it is hereby found, that in 300 years his *Acronical* setting varies 5. degrees, or dayes; I take the proportional part of that time, and say that in the year 1010. before Christ, *Arcturus* did set *Acronically* 60. dayes after the Winter *Tropicque*: and then lived *Hesiod*, or soon after. For being an *Astrologer* himself (as *Pliny* tells us *Lib.* 18. 25. saying, *Huius quaq; nomine extat Astrologia*.) it is likely he would not use an antiquated rule. *Arcturus* therefore rose *Acronically* at *Athens* in *Hesiods* time, \odot in \times 1 degree, that is, about Febr. 9. of our *Julian* year, as it now goeth: then the Swallow, used to come to *Athens*: but in our Age he riseth *Acronically* at *Athens* \odot in \times 10 $\frac{1}{2}$ that is, Mar. 20. and at *Ellen*, or *Northampton*, \odot \times 0. that is, Mar. 10.

By this you may see that the old *Astrological* Rules concerning the rising and setting of the Stars, left us by *Hesiod*, *Cato*, *Aratus*, *Varro*, *Palladius*, *Virgil*, *Ovid*, *Pliny*, *Columella*, *Ptolemy*, and other Ancient Authors cannot serve for our Age, nor for every Latitude; and the best use we can make of them, is to find the Age when they lived.

Pliny, *Lib.* 18. 26. saith, that in *Casars* Calender *octavo* Calend. Martij was *Hirundinis adventus* & *postero die Arcturi exoritur Vesperitimus*. Which agrees not to *Casars* time.

Alto *Lib.* 2. 47. he saith, *Ardentissimo aëstatis tempore, excrimur Canicula, sedus Sole primens partem Leonis ingrediente, qui dies est 15. ante Calend. Augusti* (that is, July 18,) *Rome* is in Latitude 42. degrees, *Pliny* lived about 70. years after Christ; then was *Canicula* (that is *Sirius*) in Π 17. degrees Latitude, $39 \frac{1}{2}$ Right Ascension, $79 \frac{1}{2}$ Declination, South, $16 \frac{2}{3}$, and did rise at *Rome* *Cosmically*, *decimo quinto* Calend. *Augusti*, or July 18. as thus far he reports truly: but the Sun was not then in \Re 1 deg. as *Pliny* saith but in \odot 23 degrees: for the Sun entred \Re in his time not *decimo quinto* Calend. *Augusti*, but *octavo* Calend. *Augusti*. The Sun in those dayes entering the several Signes mostly on the 5 day of the several moneths, as in our Age a-

about the 11th day, as *Astronomers* well know. *Pliny* seemes to have taken his *Astrologie* upon trust. And I cannot devise what should lead him to suppose, that howsoever the *Equinoxes* and *Solstices* in his time happed *octavo Calend.* (as he denyeth not) yet the Sun entred into a new Signe about the Ides of every Moneth, and that the Equinoctial and Solstitial points were in *Octavis partibus signorum*, as if the Sun came not to the Equinoctial till he came to the 8th degree of *Aries*. See *Pliny* Book 18. Chapter 25, 26, 27, 28. He seemeth to distrust the *Julian Calender*, and to adhear more to the account used by *Varro de Rerusticâ Lib. 1. 27.* but either he understood neither of them well, or I do not well understand him.

Now *Sirius* riseth in our Horizon with δ 18 $\frac{1}{2}$, about *August 1*, in the Declination of the heat, who in *Plinies* time rose *ardentissimo ætatis tempore*. And our Dog-dayes, if we follow the Dogs rising, will be every age colder and colder, and at length fall in Winter. It were better to reduce them to the Suns entrance into *Leo*, or to *Cancer*, 23, rather as they were in *Plinies* time: and to count the *ardentissimum tempus* a fortnight before and a fortnight after: for *Sirius* was not by the Ancients supposed the cause of the sultry heat of Summer, but a concomitant signe of that Season, whereof the Suns continuance in the North-Signes was the cause.

Would you know also when they began to Plow and to Mow in *Greece* in *Hesiods* Time? He saith, when the *Pleiades* rise, begin to Mow, and to Plow when they set. The *Pleiades* (I mean the brightest of them) 1010. years before Christ, were in γ 17. 25. minutes, Latitude 4 degrees North. Declination therefore by Chapter 34) 11 degrees, Right Ascension 14 $\frac{1}{2}$ degrees; therefore they rose Cosmically at *Athens* or *Asra*, (*Hesiods* birth Place) \odot in γ 10 $\frac{1}{3}$, that is, as our *Julian* year now goeth, about *March 20*. The *Heliacall* rising is about 20. dayes after the *Cosmicall* (Chapter 22.) that is about *April 9*. Therefore either *March 20*. at the *Cosmical* rising, or *April 9*. at the *Heliacall* rising, they began to Mow, and I think he means the *Cosmicall*; the *Acronical* rising was there in his Age \odot in α 10. $\frac{1}{3}$ about *Sep. 23*. which is too late beyond reason. Now that they should begin Mowing in *Greece* within 10. dayes after the Equinoctial is not strange, seeing the first fruits of ripe Corn were offered at *Jerusalem* yearly at *Easter*; which fell ordinarily 15. dayes

dayes after the Equinoctial, or thereabout. *Duet.* 16. And in Egypt - cum falce arva visunt Paulo ante Calendas Apriles, *moſſis autem peragitur Maio*, saith *Pliny* 18. 18. viz. Harvest began in Egypt a little before April, and April then began 8. dayes after the Equinoctial onely.

The Cosmical setting of the *Plaiades* at Athens, in *Hesiods* time 1010. years before Christ was \odot in \approx 18. degrees Octob. 1. then began they to Plow and Sow: the Egyptians began November *monſe incipiente* *Pliny* 18. 18. But if *Hesiod* were now alive at *Aſcra* he would find the *Plaiades* riſe Cosmically, with \propto 19 $\frac{1}{2}$ April 30. and ſet Cosmically \odot in m 27 $\frac{1}{2}$ Nov. 9. ſo much are his *Georgique* rules now antiquated, and ſerve for little elſe but to ſhew how many Ages ago he lived; and how the Seaſons hapned in his Age.

CHAP. XXIV.

The Latitude of your Place, the Declination, Altitude, Azimuth, and Hour of the Sun or Stars, any three of theſe being given, ſo find the other two.

S Et your Planisſpear in the firſt Mode of the Meridional ^{The Comple-} Projection, and you ſhall find all theſe five in one Ob-^{mental Trian-}lique-angled Triangle; which I uſe to call the Comple-^{gle.}mental Triangle; becauſe it conſiſts of three Sides, which are all Complements. (Others may call it as they pleaſe.)

A B in the *Limbe* between the Pole and Zenith, Complement of Latitude.

A C in a Meridian, Complement of the Declination, or the Supplement of that Complement.

B C in an *Azimuth*, Complement of the Altitude.

A at the Pole is the Angle of *Horary* diſtance from the Meridian, whoſe full meaſure is in the Equinoctial line; but becauſe every Parallel is divided by the Meridians into 180. degrees as the Equator is, and every 5th. and 15th. Meridian plainly diſtinguiſhed from the reſt in the *Fabrique* of this Inſtrument, therefore you may eaſily count the angle of the Hour in any Parallel.

B at the Zenith, is the angle of the *Azimuth*, accounted from the North part of the Meridian: his full meaſure is in the Finiterline of the *Reet*; but you may number it in any *Almicantier* be-

cause every 5th. and 15th. *Azimuths* are distinguished on the *Reet*, as the Meridians are on the *Mater*.

C the place of the Sun or Star, in the meeting of the Meridian and *Azimuth*, is the third angle, which commonly is neither known nor enquired; but it may be found when you please, by turning the Triangle, as hath been often shewed.

Now if you be versed in the 8 last Chapters of the third Book, you may easily find any of the requisites of this Chapter without any more direction. Nevertheless for the Learners sake, I shall exemplifie this general Probleme, in the 4 next Chapters, and also further in the 31, 32, and 33. Chapters hereafter following. See the Scheam Chap. 26.

CHAP. XXV.

To find the Altitude and Azimuth of the Sun or Stars, at any time proposed; the Latitude and Declination being known.

Y Our Planispheric set in the first Mode of the Meridional Projection, as in the former Chapter, go to the Parallel of the Declination of the Sun or Star, and follow him through all the Meridians from the *Finiter* to the *Limb*; (which is the Meridian of your Place;) and thence back again to the *Finiter*, and you shall find at the first sight what *Almicantar* and *Azimuth* cross the Parallel in any point proposed: and so have you the Altitude and *Azimuth* thereof.

Example. *June 10* the Sun was in the *Tropique* of *Cancer*, and so makes his diurnal revolution in the $23\frac{1}{2}$ Parallel of Declination; I follow this Parallel, the *Tropique*, from the Horizon upwards, and having gone 4 degrees, I meet the ragged arch or hour line of 4. (which is the 120th. Meridian from the South) there crosseth the second *Almicantar*, and the three and fiftieth *Azimuth* from the North; whereby I learn that at 4. in the Morning, *June 10*, the Sun is 2 degrees high; and in *Azimuth* from the North 53. Thence going on 15 degrees, I come to the hour circle of 5. where cutteth the 10th. *Almicantar* almost, and *Azimuth* 64 degrees, and better: going 15 degrees further I come to the Axtree-line, which is the hour circle of 6, and there I find the Suns Altitude 18 degrees, and his *Azimuth* from the North 75 degrees, &c. And look what Altitudes and *Azimuths* I find at 4, 5, 6. &c, in the Morning, the same I find at the

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the afternoon hours, that have like distance from Noon : because the Eastern and Western Hemispheres are alike, and the same lines serve them both.

Thus you may do in any other Parallel, and for any Star, as well as the Sun ; having his Declination given. And so you may make Tables of the Suns Altitude and *Azimuth*, at every hour, and quarter of an hour, if you please, for every day throughout the year: and that as fast as you can write them, without changing the posture of the Planisphere at all.

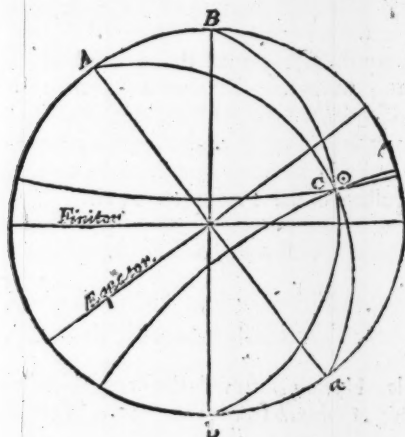
CHAP. XXVI.

The Latitude, Altitude, and Azimuth given, to find the Declination, and the Hour.

Example. Having observed the Suns Altitude 13° , and his *Azimuth* from the South Westward $28\frac{1}{2}$ in our Latitude $52\frac{1}{4}$. my Planisphere set in the same manner as Chapter 25. I sought out the 13th. *Almicantar* at the *Limb* of my *Reet*, and followed him inwards till I came between *Azimuth* 28, and 29. there I met the 30th. Meridian, and the $20\frac{1}{4}$ Parallel of Declination, by which I gathered that it was 2 of the clock after noon, and that the Sun declined Southward 20° .

Note here, that the hour of a Star thus found, is not the hour of the Night, unless the Star happen to be opposite to the Sun ; but it is the time the Star lacketh to come to the South, or the time of his course from the South.

CHAP.



CHAP. XXVII.

The Latitude, Declination, and Altitude, given, to find the Hour, and Azimuth.

Here the three sides of the Complemental Triangle are given, and the angles A and B sought.

Example, *March* the 10 in the Morning the Sun being in the Equinoctial, I observed his Altitude 32 degrees: the *Finitor* being set to my Latitude $52\frac{1}{4}$. as before, I went to the 32. *Almicantar* in the *Rect*, and where I found him crossing the Equinoctial line of the *Mater*, there I conclude was the place of the Sun at the time of my observation; and the angle C of my Triangle: there the $30\frac{1}{2}$ Meridian passing, shewed me that the angle A at the Pole was $30\frac{1}{2}$; or, that it wanted half a degree, that is 2 minutes of time, of ten of the clock: and there also the *Azimuth* $36\frac{2}{3}$ from the South (or from the North $143\frac{1}{3}$) shewed me that the angle B at the Zenith is $143\frac{1}{3}$, the *Azimuth* from the North, and his supplement $36\frac{2}{3}$, the *Azimuth* from the South.

CHAP.

CHAP. XXVIII.

The Declination, Altitude, and Azimuth of the Sun given, to find the Hour, and Latitude.

IN the Meridional Projection, look in the *Reet* where the *Almicantar* for the Altitude given, and the *Azimuth* given do cross; and turn the point of the *Reet* where they cross to the Parallel of the Suns Declination upon the *Mater*: the Meridian that cutteth there sheweth the hour, and between the Finiter and the Pole, or between the Equator and the *Zenith*, you have the Latitude in the *Limb*.

CHAP. XXIX.

To find the Hour of the Night, by the Northing, or Southing, Rising or Setting of any Star.

USe for this the Equinoctial Projection. And if the Star be in your *Reet*, turn him to the North or South of the Meridian line, or to the East or West part of the Horizon in your Planispher, as you see him in the Heaven. Then turn the *Label* to the Suns place in the *Ecliptick* of the *Reet*, and it shall shew the hour in the *Limb*: but if the Star be not in the *Reet*, you shall supply him by the shift used Chap. 18.

Example. *March* 10th, I saw *Sirius* setting in the South-West; and having turned him to the same place in my Planispher, I laid the *Label* to γ^0 . which was the Suns place for that day; and it cut in the *Limb* 11. hours 3 minutes past noon.

Again, *December* 1. Seeing *Lucida Pleiadum* in the Meridian, I turned the Star till he touched the Meridian line of the *Mater*; then laying the *Label* to τ 19. the place of the Sun, I found it was 10. hours 17. minutes at Night.

The same Night I saw *Ras Aben*, or the brightest in the *Dragons head* under the Pole, in the North part of the Meridian; wherefore I placed him on the Meridian line between the Center and *Septentrio*: and the *Label* laid to τ 19. shewed me it was 12. 36. minutes; that is more then half an hour past Mid-night.

CHAP.

CHAP. XXX.

The time of Day or Night given, to find in what Coast any Star is: and how much he is distant from the Horizon, or Meridian.

Lay the Suns place to the hour given, in the Equinoctial Projection, then may you presently see all the Stars of the *Reet* in what Coast they are, whether under the Horizon or above, and how many hours they lack, or are past either the Horizon or Meridian.

Example. Sitting within dores at seven of the clock on *Christmas* day at Night, I desired to know what Stars were rising, and what near the Meridian, wherefore laying \sphericalangle 14. to 7. of the clock afternoon, I saw in the *Reet* the *Rams horn*, a little past South. The *Plaiades* wanted 1. hour 28. minutes of South, as the *Label* shewed me in the *Limb*; \sphericalangle was rising, but *Cor* \sphericalangle . not yet up. I would know now what he wanted of rising, therefore I turned forward the *Reet* till *Cor* \sphericalangle came to the Horizon, and observed how many degrees of the *Reet* passed under the *Label* (or by any point of the *Limb*) while the *Reet* turned: and I found that \sphericalangle 0 (and so any other point) moved on in the *Limb* 10 degrees in the while that *Cor* \sphericalangle was coming to the Horizon. Whereupon I understood that he would rise 40 minutes after.

CHAP. XXXI.

The Time, and Latitude given, to find the Altitude, and Azimuth of any Star: and thereby to get the knowledge of the Stars.

Find the hour of the Star, by the former Chapter: And by the *Label* observe his Declination: then set your *Planiſphere* in the Meridional Projection, and in the Parallel of the Stars Declination, number his hour-distance from the South; where the number ends, set a needles point; there is the place of the Star; and the *Almicantar* and *Azimuth* that cut him there, shew your desire.

Example.

Example. I would know the cloudy Star *Prasepe*, in the breast of *Cancer* (which indeed is a glimmering light, made up of five smal and bright Stars, as by the *Telescope* appeareth) This *Prasepe* I found by the last Chapter to want .6. hours 21. min. of South; his Declination, found by the *Label*, is 21. degrees North. Therefore setting the Finiter to our Latitude $52\frac{1}{2}$, I follow the 21. Parallel of North Declination, from the Meridian till I come 5 degrees 15 minutes past the Axletree (because I found him 6 hours 21 minutes before the Meridian) there the 17th. *Azimuth*, from the East Northward, cutteth the Parallel of *Prasepe*; and there cutteth him also the 13th. *Almicantar*. Now to find him out, I lay my Planispher horizontally, setting the Meridian of my Planispher in the Meridian of the Place (by Chap. 3, and 4.) and I turn my *Label* and Sights to the *Azimuth* of *Prasepe* 17 degrees from the East Northward, and before my Sights I hang up a Plumb-line upon a Pole, to keep the *Azimuth*; then keeping my station, I set my Planispher upon his edge, or hang him upon a staf with a socket, in the *Azimuth* of the Star; so that the Plumbet show Altitude 13 degrees (by Chap. 1.) then do the Sights point just upon *Prasepe*, and would teach me the Star, if I did not know him before.

CHAP. XXXII.

The Latitude of the Place, the Declination of a Star, with his Altitude, or Azimuth given, to find both the Hour of the Star, and the Hour of the Night.

BY this Chapter you may find the time of Night, at any time, by any Star, if he be visible above the Horizon. Use the first Mode of the Meridional Projection; and having Observed the Altitude or *Azimuth* of the Star, look where that Altitude or *Azimuth* cutteth the Parallel of the Stars Declination, there cutteth also a Meridian which sheweth the hour of the Star, that is, the distance of a Star from the Meridian in hours and minutes. And by this hour of the Star, to get the hour of the Night, you shall place the Star at the hour found, in the Equinoctial Projection: which done, the *Label* laid to the place of the Sun shall shew the hour of the Night in the *Limb*.



Example.

Example. December 25. I observed *Procyon* to be full East, his Declination North, is 6 degrees 3 minutes. In the Meridional Projection I looked where the *Axis* of the *Reet* (which is the East *Azimuth*) cut the sixth of the North Parallels, and I found the intersection 1 degree South-ward from the Axtree of the *Mater* (or hour-line of six) there also cutteth the $5\frac{1}{2}$ *Almicantar*, which shewes more then I sought, that *Procyon* was 5 degrees 30 minutes above the Horizon. Now having the hour of the Star, 6 hours, 4 minutes, before the Meridian, I take the Equinoctial Projection, and having laid the *Label* one degree from *Oriens* South-ward in the *Limb*, I turn *Procyon* to the *Label*, which sheweth his Hour 6 hours 4 minutes, and leaving him there, I turn away the *Label* to \sphericalangle 14 the Suns place, and it shewes me in the *Limb* the time of night 6 hours 26 min, past noon. And the same I might have found, if instead of his *Azimuth*, I had observed his Altitude 5 degree $\frac{1}{2}$, the crossing of that *Almicant* in which the 6th Parallel would have given me the same hour of the Star, and further, his *Azimuth*, undesired.

CHAP. XXXIII.

Your Latitude known, and the Altitude, and Azimuth, of any Star, Planet, or Comet, observed, and the time of Night: how to find his Right Ascension, and Declination.

THis Case differeth little from the Case of Chapter 26. where, from the same things given, the Declination and hour was required. For the hour and Right Ascension are in a sort the same thing, only the account of the Right Ascension beginneth alwayes at \sphericalangle 0. and is made in degrees and minutes of a degree. The account of the Hour beginneth at the Meridian, and is made in hours and minutes of an hour. Fifteen whole degrees make an hour, and consequently 15 minutes of a Degree make one minute of Time, for in every minute of Time, there passeth the Meridian a quarter of a degree of the Equinoctial. The time of Night is here further required to be given; which may be had by Chap 29. or 32.

The rule. When you observe the Altitude and *Azimuth* of the Star, observe also the time of Night, by Chapter 29. or 32.
and

and to save you labour herein, you shall do best to observe your Altitude and *Azimuth*, when some known Star is seen just in the Meridian. Then with your Latitude, and the Altitude, and *Azimuth* of the Star, get by Chapter 26. the Declination, and hour of the Star: Then in the Equinoctial Projection, lay the degree of the Sun to the hour of the Night: thence turn the *Label* to the hour of the Star, and you have his Right Ascension in the Limb of the *Reet*, between \vee 0 and the *Label*.

Example. Put case I would find the Declination and Right Ascension of *Lucida Pleiadum*. The Sun being in *Sagittarius* 10, December 2. I observed that when *Australis cauda Ceti* is full South, *Lucida Pleiadum* was near South-east viz. in the *Azimuth* 67. from the Meridian, and the Altitude of the said Star 45. 0. hence, by Chapter 26. I find his Declination 23 degrees North, and the hour-distance from the Meridian 45 degr. that is 3 hours before noon. Then in the Equinoctial Projection (according to Chapter 29.) I set *Australis cand. Ceti* in the Meridian line of the *Mater*. and turning the *Label* to 9. of the clock (which is the hour of the Star) I find in the Limb of the *Reet* (numbring from \vee 0, to the *Label*, 52 degrees, the Right Ascension of *Lucida Pleiadum*: and where the 23 degrees of the *Label* now touches the *Reet*, there may I prick the Star in my *Reet*, if I have him not before; the time of night is easily seen, by turning the *Label* to the Suns place, it shewes 7. hours 12 minutes at night: but I need not so much as look on that, though by placing *Australis cand. Ceti* in the South, I have the time implicitly. The Proposition therefore, might have been thus made; Your Latitude known, and the Altitude and *Azimuth* of an unknown Star observed, just at the time when any known Star is in the Meridian; to find both the Right Ascension, and Declination of the Star unknown.

Note also, that if you observe the unknown Star in the Meridian *Azimuth*, you have presently his Declination, by Chapter 13. and the Right Ascension of *Culmen Ceti*, is the Stars Right Ascension.

CHAP. XXXIIII.

The Declination, and Right Ascension of any Star given, to find his Longitude, and Latitude.

Look the Stars place in the *Mater*, (which is the Intersection of the Meridian of his Right Ascension with the Parallel of his Declination) and make a prick there. Then your Planisphere being set in the second Mode of the Meridional Projection, you shall presently find the Longitude and Latitude in the *Rect*: for the *Azimuth* cutting the said prick, shewes his Longitude, and the *Almicantar* his Latitude.

Example. *November 14. 1639.* I observed a Star of the third Magnitude in the Heart of *Cetus*, which I know to be no common Star, because I had never noted it before, neither could I find it in the Tables of *Ptolemy*, *Tycho*, or any other: the Right Ascension thereof was 30. 13 minutes, the Declination 4. 50. minutes South, as I observed by a way which hereafter shall be shewed Chapter 44. I made therefore a prick with ink in the *Mater* of my Bras Planisphere, where the 30th. Meridian (numbered from the Center toward my right hand) and the 5th. Parallel of South Declination do cross; regarding also the odd minutes. Then as soon as my ink was drie, I set the Finny in the *Ecliptique* line of the *Mater* with the Zenith South-wards; because the Latitude of the Star was South, and I saw the 26. *Azimuth* from the Axtree line cutting the prick, and likewise the 16th. *Almicantar* cutting about 10 minutes below the prick toward the Finiter. Therefore because in this Mode the *Azimuths* be Circles of Longitude, and the *Almicantars* Parallels of Latitude, (by Book 2. 1.) I conclude the Longitude of *Cor Ceti*, was \vee 26, and his Latitude 16. 10 minutes South.

When first I observed this strange Star in the said year 1639. and could find no mention of it in the Tables of *Ptolemy*, *Copernicus*, *Stadius*, *Tycho*, or *Maginus*, I did thereof advertise my very good friends Dr. *John Twysden*, then in *Kent*, and Mr *Samuel Foster*, Professor of *Astronomy* in *Gresham Colledge*, then at *London*, who thereupon made the same observation of the Star that I had done, for the place of it; and we all agreed that it increased in light, and was above the third Magnitude in *December*

1639. and that it had no perceivable Parallax. And as I was thinking to publish some brief advertisement thereof, in the Latin tongue, that *Astronomers* beyond the Seas as well as here, might attend the observation thereof, Mr *Foster* wrote me word that he had found the Star pictured in *Bayerns* his Images, which were printed *Anno Domini*. 1616. And in 1640. there came to me through Dr *Twydens* hands a Treatise of that Star, then newly Printed, by one *Phacylides*, Professor of *Logique* at *Franequers*, whose observations agreed with ours. But he thought this Star to have been made of the great Eclipse of the Moon which hapned *December* 10. 1638. in the foremost foot of II. wherein we were not of his mind, you may read this conceipt in his Book pag. 197. This Star doth often appear, and again disappear; it is sometime of the 3d. Magnitude, sometime of the 4th. I have seen it oft in the Eastern Hemispher, seldome in the Western. It is lost sometimes divers weekes together: this year I could never see it, till *February* 2. 1656. Such as have leasure for the Study of these Arts, may do well to observe it, and to search the reason of its changes: for which purpose I thought it fit to give this notice.

CHAP. XXXV.

The Longitude, and Latitude, of any Star given, to find his Right Ascension, and Declination; and to place the Stars in the Mater.

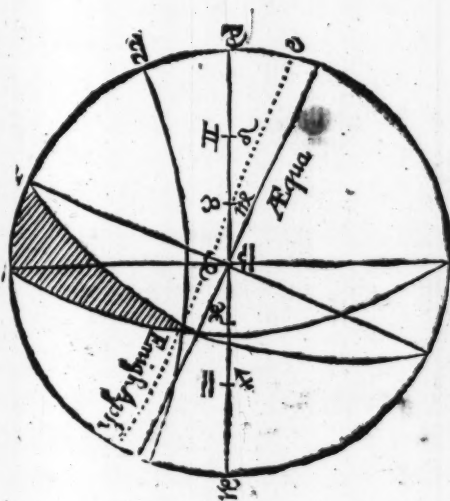
THis Probleme is the converse of the precedent. The Stars are registred by their Longitudes and Latitudes, because their Longitudes increase equally, and their Latitudes remain the same. And so the Tables are easily rectified to any Age, by Addition or Subtraction of a few degrees or minutes of Longitude onely: but the Right Ascension and Declination of the Stars happen to increase and decrease very unequally, and must therefore be calculated from Age to Age, from the Longitude and Latitude whose Tables are more certain.

See the Planispher in the second Mode of the Meridional Projection, as in the former Chapter, and bearing in mind that the *Azimuths* here are Circles of Longitude and the *Almicantars*

stars Parallels of Latitude, look where the Longitude and Latitude of the Star meet, and there make a prick in the *Reet*; and look what Meridian and Parallel of the *Mater* cut, under that prick they shew the Right Ascension, and Declination of the Star.

Example. *Eniph. Alpharats*, that is, *Os Pegasi*, had by *Tycho's* Tables *An. Dom.* 1600. Longitude ≈ 26.22 minutes, Latitude $22.07 \frac{1}{2}$. North. The *Finiter* set to the *Ecliptique* line of the *Mater*, and the *Zenith* toward the North Pole (because the Stars Declination is North) I count the Longitude of the Star upon the *Finiter*, (here *Ecliptique*) thus. At the Center say I, is $\gamma 0$. thence proceeding rightward to the *Limb*, I say, here is $\odot 0$. whose Right Ascension is 90 . thence returning to the Center, I say, here is $\simeq 0$. upon the Axis of the *Reet* and Right Ascension 180 . upon the Axis of the *Mater*; thence I proceed in the *Finiter* to the other side of the *Limb*, and say here is $\simeq 0$. bounded by the *Limb* of the *Reet* and Right Ascension 270 . bounded by the *Limb* of the *Mater*, which *Limbs* here fall into one Circle; and are *Colurus Solstitiorum*: these numbers I keep, and returning back in the *Finiter* toward the Center, when I am gone 30 degrees, I say, here begins \approx , and going on 26.22 minutes further, I say, thus far is the Star gone in Longitude. Now here cuts the *Finiter* (by this account) the *Azimuth* $35 \frac{1}{2}$. from the *Limb*; in this *Azimuth* I number the Stars Latitude, by the *Almicantats* $22.07 \frac{1}{2}$. and at the end of that number in the said *Azimuth* I prick the Stars place. And here I see the 8th. Parallel of North Declination upon the *Mater* cutteth him, and the Meridian $51 \frac{1}{2}$. from the *Limb* shewing the excess of his Right Ascension above 270 . which I kept before. Therefore I conclude the Right Ascension of *Eniph. Alpharats*, *Anno Dom.* 1600. was 321.20 minutes; and his Declination 8 .deg. North.

Another Example. In the Year 1670. *Aldebaran* will have one degree of Longitude more then he had in *Anno Dom.* 1600. therefore he will be in $\pi 5.12$ minutes Latitude 5.31 minutes South. Now because the Latitude is South, I turn the *Zenith* towards the South Pole (the *Finiter* being placed on the *Ecliptique* line as before) and beginning at the Center, I number on the *Finiter* (here *Ecliptique*) the Longitude of *Aldebaran* 65.12 minutes; and a little beyond the 65th. *Azimuth* I climb up by the *Almicantats*, toward the *Zenith* 5.31 minutes to the place
of



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of *Aldebaran*. There the $64\frac{1}{3}$. Meridian of the *Mater* cutteth under him; shewing his Right Ascension: and likewise the 16th. Parallel almost of North Declination; shewing that *Aldebaran* declines North almost 16 degrees, though he have South Latitude 5.31 minutes.

Another way to place the Stars in the *Mater* by their Declination and Horary-distance from the Meridian. See hereafter Chapter 52.

CHAP. XXXVI.

The Latitude, and Declination of a Star given, to find his Longitude, and Right Ascension.

S Et your Planisphear in the second Mode of the Meridional Projection, turning the *Zenith* Northward or Southward as the Stars Latitude hapneth to be North or South. Then look where the Parallel of the Stars Latitude in the *Reet* cutteth the Parallel of the Stars Declination on the *Mater*, the *Azimuth* cutting that intersection sheweth the Longitude of the Star; and the Meridian there cutting sheweth his Right Ascension.

Example. The Declination of *Spica* π , *Anno Dom.* 1670. will be $9\frac{1}{2}$. South, the Latitude was always 1. 59 minutes South. Now where the second *Almicantar* cutteth the $9\frac{1}{2}$. Parallel of South Declination, there passeth the 19th $\frac{1}{4}$. *Azimuth* from the Axis toward my left hand shewing *Spica's* Longitude $\simeq 19\frac{1}{4}$. and the 17th. Meridian from the Axis, to which I add a Semi-circle (because $\simeq 0$. is at the Center) and I make 197 degrees the Right Ascension of *Spica* for 1670.

CHAP. XXXVII

The Longitude, and Latitude of two Stars given, to find their Distance.

M Ake one of the Poles of the *Mater* to be Pole of the *Ecliptique*, for this turn, and set the Star which hath most Latitude at his distance in the *Limb*, and turn the *Zenith* to him; count thence by the Meridians the difference

difference of Longitude, till you come to the other side of your Triangle; and in that side number either the Latitude from the Equator, or his complement from the Pole; at the end of this number is the other Star: and the *Azimuth* passing from him to the *Zenith*, shewes the distance. This is done by the second Probleme of Obliquangled Triangles. Book 3. 15.

Example. In *Tycho's* Tables for 1600.

Aldebarans Longitude is Π 4. $12\frac{1}{2}$. Latitude 5. 31. min. *A.*

Sirius Longitude \Im 8. $35\frac{1}{2}$. Latitude 39. $30\frac{1}{2}$. *A.*

Difference of Longitude 34. 23.

I number therefore 39. 30 minutes $\frac{1}{2}$, the Latitude of *Sirius* from the Equator in the *Limb*, or the Complement thereof from the Pole, (all is one,) there I set the *Zenith* to stand for *Sirius*; then because *Aldebaran* is distant from *Sirius* in Longitude 34. 23. minutes, I take the $34\frac{1}{2}$. Meridian from the *Zenith*, and where the $5\frac{1}{2}$ Parallel cutteth him, there say I, is *Aldebaran* (and C of my Triangle) and the *Azimuth* passing thence to the *Zenith* measureth the distance of the Stars 46 degrees almost.

CHAP. XXXVIII.

The Declination, and Right Ascension of any two Stars given, to find their distance.

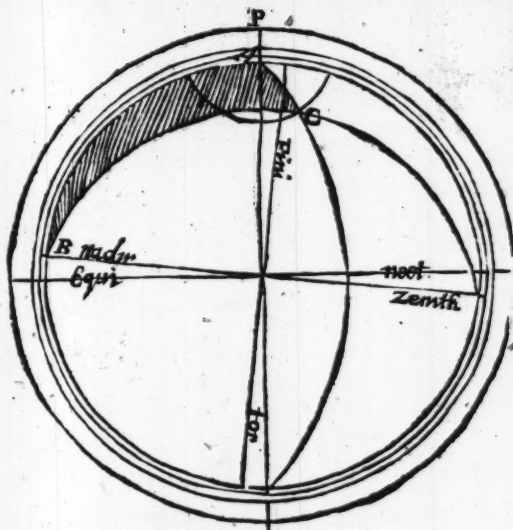
DO here with the Right Ascension and Declination as you should do with the Longitude and Latitude, by the former Chapter, for the case is like, and requireth the same manner of working.

CHAP. XXXIX.

The Declination of a Star or Planet, and his distance from a known Star given, to find his Right Ascension.

BEcause this Case is the converse of the precedent, and soluble by the first Probleme of Obliquangled Triangles, Book 3. 14. an Example, or two shall suffice.

Anno Domini. 1639. I observed the Declination of *Cor Ceti* (the strange Star mentioned Chapter 34.) to be 4. 50 minutes South; and his distance from *Lucida Mandibula Ceti* to



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while that Chapter is Reading.



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FOR THE YEAR 1871

to be 13. 04 minutes, and *Lucida Mandibula* was Eastward from him. The Right Ascension of *Lucida Mandibula* then was 40. 56 minutes, his Declination North 2. 40 minutes; therefore I have a Triangle whose Sides are all known.

A B the distance of *Mandibula* from the Pole 87. 20 minutes, I set between the Pole and *Nadir* in the *Limb*, because B C will reach beyond the *Finitor*.

For A C the distance of the Stars. I seek the 13th, Parallel from the Pole. And

For B C I seek the 94. 50 minutes *Almicantar*, counted from the *Nadir* (that is the 5th, almost above the *Finitor*) and where the said Parallel and *Almicantar* cross, there is *Cor Cati*, and C of my Triangle: through it there cutteth the *Azimuth* 10²/₃, shewing the Difference of the Right Ascension of the Stars; which difference I subtract out of the Right Ascension of *Mandibula*, because he was further East; and there remaineth the Right Ascension of *Cor Cati* 30. 16 minutes, or rather 13 minutes. And I have here also numbred by the Meridians, the angle A at *Mandibula* 120 degt. though un-required.

Another Example. January 7. 1656, I observed by my Brass Quadrant of 12 inches in Radius, the Meridian Altitude of *Jupiter* 56. 20 minutes, out of which subtracting the height of the Equator here at *Edon* 37. 45 minutes; I found his Declination 18. 35 minutes North; his distance then from *Lucida Pleiadum*, I observed by my Cross-staff 5. 12 minutes, and from *Aldebaran* 10. 07 minutes.

The Complement of Decl. of *Lucida Pleiadum* is 67. 00. mi.

The Complement of \angle his Declination was observed 71. 25.

And these two Complements with the distance of \angle and *Lucida Pleiadum* 5. 12 minutes, make a Triangle, soluble by the first Probleme of Obliquangled Triangles; whereby you may find the angle of the difference of Right Ascension of *Lucida Pleiadum* and \angle is 2. 56 minutes; which added to the Right Ascension of *Lucida Pleiadum* (because \angle was East-ward) maketh 54. 44 minutes the Right Ascension of *Jupiter*.

CHAP. XL.

The Latitude of a Star or Planet, and his distance from a known Star given, to find his Longitude.

DO here with the Longitude and Latitude as you were taught to do with the Right Ascension and Declination, in the former Chapter.

CHAP. XLI.

To find the distance of two Stars by their Altitudes, and their difference of Azimuth observed at the same time.

THe Complements of the Altitudes are the distances of the Stars from the *Zenith*: Set one of the Stars at the Pole, and set the *Zenith* as much from him in the *Limb* as the Complement of his Altitude comes to, then considering what difference of *Azimuth* the Stars had, take the *Azimuth* of like distance from the *Limb* (beginning from that side of the *Limb* where the Pole aforesaid is) and in that *Azimuth* reckon from the Finitor the Altitude of the other Star (or the Complement of his Altitude from the *Zenith*, all is one) at the end thereof is C, and the other Star; and the Meridian that passeth from him to the Pole, shewes the distance of the Stars. This case is so like that of Chapter 37. that he who knowes one may know the other also.

CHAP. XLII.

To find the Angles of Station which any two Stars make with the Pole, by their Right Ascension and Declination: or with the Pole of the Ecliptique, by their Longitude and Latitude: or with the Zenith, by their Altitude and Azimuth.

THis Case agrees with the second Probleme of Oblique-angled Triangles.

Example, In the Triangle of Chapter 39. made between the

the Pole of the World, *Mandibula Ceti*, and *Cor Ceti*, I would know the angle at *Mandibula*, which is the angle of his Station. Place the Triangle upon your Planisphaer as in Chapter 39. where the angle unfought, there discovered it self to be 129. degrees.

CHAP. XLIII.

To find whether three Stars be in one great Circle, by having their Longitude and Latitude, or their Right Ascension and Declination, or their Azimuth and Altitude known.

Example. I would know whether the three Stars of *Orions Girdle* be in the same great Circle. Here I prick them down, and draw their Circles of Longitude to meet at the Pole of the *Ecliptique*; so have you two Triangles joyned in one, and the three Stars in the Base of it.

Now first, I must find by the former Chapter what angle of Station the first Star hath in the little Triangle *P A B*, and then what angle of Station he hath in the whole Triangle *P A C*, and if these two angles be equal, then be the Stars all in one great Circle, otherwise not.

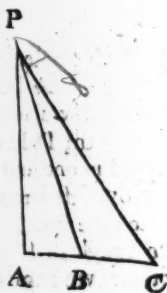


This Probleme may be of use to find how the tayle of a Comet pointeth upon the Sun, or upon any other Planet or Star, below the Horizon. But if the three points enquired of, be all in view; I know no better way then to stretch a thrid straight at a reasonable distance from your eye, applying it to the Stars; for if the same straight line cut them all, they be all in one great Circle, otherwise not.

CHAP. XLIV.

If a Comet or Star unknown be seen in a straight line with two other known Stars, and his distance from one of the known Stars be observed; how to find the true place of the Comet or Star unknown.

EXample, *Anno Domini* 1639. I observed that *Mandibula Ceti*, *Gena Ceti*, and the strange Star *Cor Ceti* (spoken of Chapter 34.) made a straight line; and by a *Radius*, such as I then had at hand, I observed that *Cor Ceti* was distant from *Mandibula* 13. 04 minutes. Now if I would find the Longitude and Latitude of the other Stars; but because I intend to find first his Right Ascension and Declination, I make use of their Right Ascension and Declination. The manner of working is alike. The Scheme of the last Chapter may serve here if you turn it up-side down; Then P is the North Pole, A *Mandibula*, B *Gena*, C *Cor Ceti*. PA is the Complement of Declination of *Mandibula* 87. 20 minutes, PB the distance of *Gena* from the North Pole 91. 16 minutes, (for he declines Southward 1. 16 minutes) APB the difference of their Right Ascension 5. 35 minutes.



Therefore I set the *Nadir* of my *Racet* as far from the Pole as P is from A, and so between them on the *Limb* is the side PA. Then for the side PB it reacheth from *Nadir* beyond the *Finitor* 1. 16 minutes, therefore in the $1\frac{1}{4}$ *Almicantar* I number from the *Limb* 5. 35 minutes, the difference of Right Ascensions for the Angle APB, and where the $1\frac{1}{4}$ *Almicantar* and the $5\frac{1}{2}$ *Azimuth* do meet, there is B for *Gena*: thence I go in a Meridian to the Pole at A, and as I go I number the distance of B and A, that is, *Gena* and *Mandibula*, 7 degrees almost; and I observe that this Meridian is the 125. Meridian from the *Limb*; so much is A, the angle of station at *Mandibula*.

Now

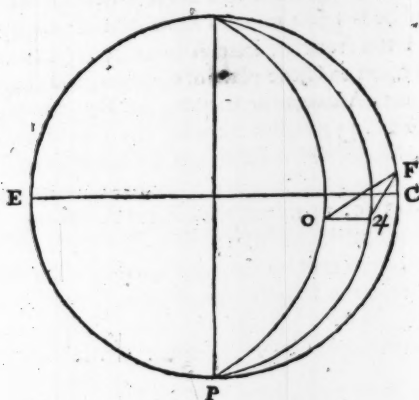
Now I say, in this Meridian also is *Cor Ceti*, because he is in a right line with the other two Stars which are cut by this Meridian : and he is 13. 4 minutes from *Mandibula*, by observation; therefore I run from the Pole A so many degrees in this Meridian, and so come to C, the place of *Cor Ceti*, and there cutteth the 4. 50 minutes *Almicantar*, shewing the Declination of it, and the *Azimuth* 10. 43 minutes, shewing his difference of Ascension from *Mandibula*; which difference I subduct from the Right Ascension of *Mandibula* (because *Mandibula* is further East,) and there remains 30. 13 minutes, the Right Ascension of *Cor Ceti*: which being found, you may find his Longitude 26 degrees, Latitude 16. 10 minutes, by the 34th. Chapter: Observe how your Triangle lies in the Planispher, where *Nadir* is used for the North Pole, the North Pole is the place of *Mandibula*, and the 125. Meridian represents the great Circle cutting the three Stars.

CHAP. XLV.

The distance of a Planet from two known Stars being Observed, to find his Longitude and Latitude.

IT is true, that Mr. *Blagrove* saith, Book 5. 25. that in Questions of this sort it is harder to conceive how they should be resolved, then to resolve them; And therefore he adviseth to draw a rude Scheme of your work, agreeable to the Meridional Projection of your Planispher, after this manner.

December the 28. 1656. I observed somewhat grossly by my Cross-staff that ν was between the *Hyades* and the *Pleiades*, distant from *Aldebaran* 9. 49 minutes, and from *Lucida Pleiadum* 5. 26. and to the Southward of the Stars. I draw therefore a rude Scheme representing somewhat near the posture of these three Stars. E C is *Ecliptique*, and P his South Pole, P C the Circle of Longitude of the Westerly Star *Lucida Pleiadum* 8 25. 12 minutes, and because he hath North Latitude 4. degrees, I place him at F; *Aldebaran*, whose Longitude is Π 5. Latitude South 5. 31 minutes, I place somewhat like at O, and *Jupiter* I place below the line drawn between them, and nearer to the *Pleiades* then to *Aldebaran*, as I observed his situation in the Heaven.



That I seek now here, is $P\alpha$, the complement of *Jupiters* Latitude; and $FP\alpha$, his difference of Longitude from *Lucida Pleiadum*.

First, in the great Triangle FPO , I have the angle P , the difference of Longitude between *Lucida Pleiadum* and *Aldebaran* 9 degrees 48 minutes, and the including sides PO 84.29. (*Aldebaran* distance from the South Pole) and PF 94. (distance of the *Pleiades* from the South Pole) and hence by the second Problemes of Obliquangled Triangles Book 3. 15. I get at once, the Base OF , distance of *Lucida Pleiadum* and *Aldebaran* 13. 45 minutes, and the angle of station at F , viz. PFO 45. 28 minutes.

2. Then in the Triangle $FO\alpha$, whose three sides are now known, I get the angle $OF\alpha$ (by the first Problem of Oblique Triangles, Book 3. 14.) 35. 14 minutes) which being Subducted from the angle $OFFP$, leaveth the angle $PF\alpha$ 10. 14 minutes.

3. In the Triangle $PF\alpha$, having now the angle F , and the sides including it, I get the third side $P\alpha$, the Complement of α Latitude 88. 39 minutes (by Oblique Problemes 2. Book 3. 15.)

And

And lastly the three sides in the Triangle P F \perp being now known my Planisphere unmoved will shew me F P \perp 58 minutes (by the Probleme 1 Oblique Triangles,) which 58 minutes being added to the Longitude of *Lucida Pleiadum* maketh up the Longitude of $\perp \approx 26. 10$ minutes, and his Latitude was even now found 1. 21 minutes South.

CHAP. XLVI.

To find the Culmen Cæli, and the Altitude thereof, at any time proposed.

Culmen Cali is the degree of the *Ecliptique* which is cut by the Meridian of your Place.

Use the Equinoctial Projection, where having laid the place of the Sun to the Hour proposed, look what degree of the *Ecliptique* is cut by the Meridian line, and you may number his Altitude from your proper Horizon.

Example. *March 29. 1652.* I laid the Suns place γ 19. 11 minutes to 32 minutes past 10. of the Clock before noon, and in the Meridian I saw \times 25 $\frac{1}{2}$ Culminating. And for his Altitude I looked where my Horizon cuts the South part of the Meridian (at 52 $\frac{1}{4}$ from the Center) and from that cutting I count in the Meridian to the *Ecliptique* 36 degrees, the Altitude of *Culmen Cali*.

But note, That if \times had been a North Signe, I must have counted first to the *Limb* 37. 45 minutes, and thence back again to *Culmen* 1 $\frac{3}{4}$. in 39 $\frac{1}{2}$.

CHAP. XLVII.

To find the Ascendent or Horoscope, and the other three Principal Houses for any time proposed.

Astrologers divide the Heaven into twelve Houses, of which, four are principal. The First House, which beginneth at the Ascendent or Rising point of the *Ecliptique*. The Fourth, which beginneth at *Imum Cali*, or Midnight. The Seventh, which beginneth at the Descendent point of the *Ecliptique*. And the Tenth, which beginneth at *Medium Cali*, or *Culmen*. These

These be the four Cardinal points, and the *Ascendent* and *Descendent*, and likewise the *Medium* and *Imum Cali*, are alwayes opposite one to the other, so that one being known, the other is known also.

To find these points, use the Equinoctial Projection, and there lay the Suns place to the hour proposed: then the degree of the *Ecliptique* rising in your Horizon is *Ascendent*, and you shall see the same degree of the opposite Signe Descending in the West part of the Horizon; and look what degree toucheth the South part of the Meridian, that is, *Medium Cali*, and the same degree of the opposite Signe shall be in *Imo Cali*, that is, in the North and *Subterranean* part of the Meridian.

Example. *March 29. 1652.* I observed the great Eclipse of the Sun, the middle whereof hapned at *Elton*, at 10 hours 32 minutes 04 seconds before noon in apparent time, at what time the Sun was darkned digits 11. 22 $\frac{1}{2}$, in γ 19. 11 minutes. I would know for this time the Figure of the Heavens.

Therefore laying the *Label* to 10. 32 minutes before noon, and bringing γ 19. 11 minutes to the *Label*, I see in our Horizon \S 24. 7 minutes rising, and ν 24. 7 minutes setting. In the Meridian above the Horizon I see κ 25. 19 minutes: and in *Imo Cali*, toward *Septentrio*, π 25. 19 minutes.

CHAP. XLVIII.

To find the beginnings of the other eight Houses.

THere be six great Circles, by which the twelve Houses are distinguished. They be called Circles of Position: and so they call the rest of the Circles which serve to subdivide the Houses. They be all Horizons to some Country or other in the World, and therefore are most fitly represented by the Horizons of the *Master*. The First House beginneth alwayes at the *Ascendent*: and the rest follow in order according to the Sequel of the Signes. But *Astrologers* are not well agreed about their situation. For 1. Some will have the domifying Circles drawn from the Poles of the *Ecliptique* through every 30th. degree thereof, as *Ptolemie*. 2. Some draw them from the Poles of the World, through every 30th. degree

degree of the Equator; as *Alcabius*. 3. Some draw them from the interfections of the Meridian and Horizon, through every 30th. degree of the Equator; as *Regiomontanus*. 4. Some draw them from the same interfections, by every 30th. degree of the *Prime Vertical* or East *Azimuth*; as *Campanus*. Yet every *Astraloger* will pretend he can tell you your Fortune, though they go about it so divers wayes, that they may be all false, and but one of them can be true: and no Man hath shewed any better reason for his way then another, but his own opinion.

If you will follow the first or second way, the matter is plain. For in the first way every 30th Circle of Longitude reckoned from the Ascendent downwards, and so round, is a *Domifying* Circle: and likewise every 30th. Meridian from the Ascendent is a *Domifying* Circle, in the Second way. And if you know but what Longitude a Star hath, you presently find in what House he is, after the first way. And if you know the Right Ascension of a Star, and of the Ascendent, you presently find in what House he is, after the second way.

But if you will use the third way (now commonly used) you shall set the *Zenith* line of the *Reet* to the Latitude, and so the *Azimuths* are your Circles of Position; then look what *Azimuth* cutteth every 30th. degree of the Equinoctial, that is a *Domifying* Circle; and you shall reckon here from the *Limbe*, which shall stand for the beginning of the 10th. House, and so in our Horizon $52\frac{1}{2}$. the forty third *Azimuth* cutteth the 30th. degree of the Equator, serving the 11th. and third House: and the *Azimuth* $70\frac{1}{2}$ cutteth the 60th. degree of the Equator, serving the 12th. and second Houses: and because I know that on the other side the Center the Intersections will be like, I look no further.

But now I must get the Depressions of these Circles under the Pole in this manner. I number in the forty third *Azimuth* the Latitude of my Place from the *Zenith*; to the end of which number I lay the *Label*, and I see the *Azimuth* cutting on the *Label* $32\frac{1}{2}$ for the depression of that Circle. And in like manner, laying the *Label* upon the 52 degrees of the *Azimuth* $70\frac{1}{2}$ I find on the *Label* his depression 48 degrees; by the third Probleme of Rectangl. Triangles, and the third Variety Book 3.5.19.

These Horizons therefore I chooke out in the *Mater*, viz. $32\frac{1}{2}$, and 48 . for these with the Meridian and Horizon of my Place,

shall serve to get the Houses for ever, in my Latitude: for the $32\frac{1}{2}$ Horizon shall be the beginning of the 11th. and third Houses; and the 48th, the beginning of the 12th and Second, Thus have I the Circles of Position of the 11, 12, 2, and 3. Houses: and the 10th, and first, are had by the former Chapter: and these six being had, I have all; for opposite Hemispheres are always alike, and one description serveth both,

CHAP. XLIX.

To know what degree of the Ecliptique is in the beginning of every House.

DO as in this Example. By Chap. 47. I had the degree *Culminating* in the middle of the great *Eclipse* there mentioned, $\propto 25\frac{1}{2}$. First I lay $\propto 25\frac{1}{2}$ to the *Axree* line at 6 in the morning, where it lieth as in a Right Horizon; thence I move it 30 degr. Southward in the *Limb*, viz. to 8. of the clock, and in the Horizon of the 11th. house ($32\frac{1}{2}$) I see $\propto 7$ degrees setting, the said degrees of Culmination: 30 degrees further, viz. to 10. a clock, I see in the Horizon of the 12th. House (48.) $\Pi 24\frac{1}{2}$. And setting the said degree of Culmination to the Noon-line, I see in our Horizon ($52\frac{1}{2}$ which begins the first House) $\S 24\frac{1}{2}$ ascending. And setting the said degree 2 hours further on, I see in the Horizon of the second House (48) $\S 13$. And setting the said degree to 4 a clock, I see in the Horizon of the third House (the $32\frac{1}{2}$) $\propto 1$.

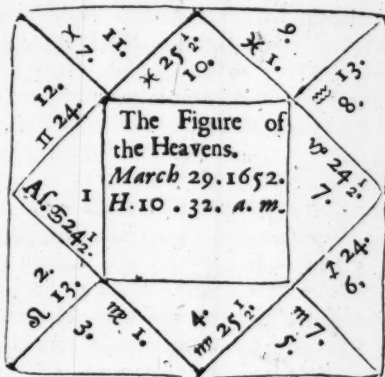
Thus have I the degrees of the *Ecliptique* in the beginning of 6 Houses, and the 6 Houses opposite begin with the same degrees of the opposite Signs.

CHAP. L.

Another way to find what degree of the Ecliptique is in the beginning of every House, and thereby to set a Figure more easily then by the former Chapter.

IT was found by Chapter 48. that the *Azimuths* 43. and $70\frac{1}{2}$ are evermore *Domifying* Circles in our Latitude ($52\frac{1}{2}$) and how you may find them for any other Latitude was there

there shewed. There I reckoned them from the *Limb*; but here I shall reckon them from the *Axis*; and say, the *Azimuth* 47. serveth the 11th. House; the $19\frac{1}{2}$ serveth the 12th. the *Axis* for the first, and seventh; the $19\frac{1}{2}$ below the *Axis* for the second; the 47th. for the third; the *Meridian* for the 10th. and 4th. You may therefore mark the ends of these *Azimuths* in the *Finis*, setting 12 to the $19\frac{1}{2}$ above the *Axis*, (here made *Horizon* for this turn) and 11.



at the 47th. at the *Axis*, 1. then at the $19\frac{1}{2}$ below the *Axis*, write 2. at the 47th. write 3. and at the *Limb* 4.

Your Houses being thus distinguished on the *Reet*, get the degree of Culmination, and the Altitude thereof, by Chapter 46. then set the *Zenith* under the North Pole, so much as the Altitude of the Culmination comes to: and if the Ascendent be a North Signe, let the Pole be toward your left Hand; and contrary if it be a South Signe: so shall the *Axis* of the *Reet* be *Horizon*, and the Pole *Culmen Cali*.

Next get the Ascendent by the 47th. and his Amplitude by the 16th: this Amplitude you shall number in the *Axletree* of the *Reet* from the Center alwayes to your left Hand, or toward *Septentrio*; and mark what *Meridian* there cuts the *Axletree* of the *Reet*, in that degree of Amplitude; that *Meridian* shall be your *Ecliptique* for this time: follow him up to the Pole, and you trace out the arch of the *Ecliptique* from the Ascendent to mid-heaven: and if you go down in his match to the like degree of Amplitude on the other side of the Center, there is the Western arch of the *Ecliptique* from the mid-heaven to the Descendent; and here you may see every degree of the *Ecliptique* above the *Horizon*, and in what House it is, without any more coursing after them.

Example. $\propto 25 \frac{1}{2}$ was Culminating; his Altitude 36 degrees; the Ascendent had $\oslash 24$. whose Amplitude is $36 \frac{1}{3}$. Setting the Zenith therefore 36 degrees to the right Hand under the Pole, I number in the Axtree-line of the Reet, from the Center to my left Hand the Amplitude of the Ascendent $36 \frac{1}{3}$. there cometh the 23. Meridian from the Center, who must serve for the *Ecliptique*. Now because it is troublesome to number the degrees of the Signes backward, I will begin at the Descendent $36 \frac{1}{3}$ from the Center on the other side : and say, Here is $\vee 24$ degrees descending, (because $\oslash 24$. was ascending.) hence I count on toward the *Culmen*, till I come to the *Azimuth* $19 \frac{1}{2}$, (which is the *Domifery* of the 12th. and 8th. Houses,) and here I say, begins the 8th. House in ≈ 13 . for there are but 19 degrees from the Descendent hither: hence I count to the 47th. *Azimuth* (the *Domifery* of the 9th. and 11th. Houses) and there I count $\propto 1$ degree, for the beginning of the 9th. House: hence I number on to the Pole, and there I happen on $\propto 25 \frac{1}{2}$, the *Culmen* and beginning of the 10th. House. Thence I number on the other side of the *Maters* Axtree, in the twenty third Meridian, toward the Ascendent, and I find the 47th. *Azimuth* cuts $\times 7$ degrees for the beginning of the 11th. House; but the $19 \frac{1}{2}$ *Azimuth* which should shew me the 12th. House, is cut off by the *Finitor*, and I am left to seek him else where : And to find him I need but turn about my whole Planispher (the *Reet* unmoved) and make the other Pole *Culmen* for this turn, and then I find among the *Azimuths* that peece of my *Ecliptique* which I wanted in the former posture; and I may reckon on him between the Ascendent and the *Azimuth* $19 \frac{1}{2}$, $29 \frac{1}{2}$. and thereby see that $\pi 24 \frac{1}{2}$ is in the beginning of the 12th. House: so have I 6. of my Houses, and may by them find the other 6. (as was shewed Chapter 48.) and set them down as in the Figure.

CHAP. LI.

A third way to set a Figure with less labour.

LEt the Meridians and *Azimuths* here change their offices in which they served in the former Chapter: that is, let the $19 \frac{1}{2}$ and 47th. Meridian on both sides the Axis of the *Maser* be *Domifiers*; and let the 23 *Azi-*
muth

must be *Ecliptique*: and to that purpose, set the *Zenith* above the Pole, according to the Altitude of *Culmen* 36 degrees, and make the Axis of the *Mater* Horizon. Then beginning as you did before at the Descendent, go up in the *Ecliptique* till you come to the Meridian 19 $\frac{1}{2}$, and follow the *Almicantar* that there cutteth to the *Limb*, and there make a mark for the 8th House; then mark where the same *Ecliptique* cuts the next *Domisier* (the 47th. Meridian) and follow the *Almicantar* from that point to the *Limb*; prick there the 9th. House: the *Zenith* is the 10th; thence go toward the Ascendent, and do in like manner; making pricks for the 11th. and 12th. Houses: also in the *Limb* of the *Reet* at the end of that *Almicantar* which cutteth the beginning of the Houses in the *Ecliptique*. Then in the *Zodiaque* of the Ring, look the degree of Culmination, and set the *Zenith* of the *Reet* to it; and the *Label* laid to these pricks, shall shew you presently in the *Zodiaque* the degrees for the beginning of every House.

CHAP. LII.

How to place any Star or Planet in his proper House.

IN the Equinoctial Projection, get the Stars Hour distance from the Meridian, thus. Lay the Suns place to the hour proposed: then turn the *Label* to the Star (or to his Right Ascension if he be not in the *Reet*) and it shall shew in the *Limb* how many hours and minutes the Star is past or short of the Meridian: get also the Stars Declination North or South, by the *Reet*, or by the 35. or some other Chapter; and where the Parallel of the Stars Declination crosseth the hour of the Star in the *Mater*, there is his place for this turn: therefore having made a prick with ink for him there, set the *Zenith* line to your Latitude, and having your *Domissing Azimuths* marked upon the *Reet* (as Chapter 49. 30.) you shall presently see in what House the Star is.

Example. 1652. March 29, 10. hours 32 minutes before noon, I would know in what House the *Pleiades* are. The hour of *Lucida Pleiadum* for that time is 8. 14 minutes after midnight: the Declination is 23 degrees North. I number therefore in the 23. Parallel of North Declination from the *Atree*

of the *Mater* to the Meridian 33 $\frac{1}{2}$, there is the place of *Lucida Pleiadum*, where I prick him down; and setting the *Zenith* line to the Latitude, I find the 39 *Azimuth* or Circle of Position cuts him: by which I see he is 8 degrees from the beginning of the 11th. House, for that begins at *Azimuth* 47, as appears Chapters 49, 50.

CHAP. LIII.

To find the division of the Houses, according to Campanus.

C *Ampanus* begins the Houses at every 30th. degree of the East *Azimuth*, accounting from the Ascendent in the Sequel of the Signes, as was said Chapter 48. Therefore if you will use his way, set the *Zenith* line to the Latitude, and the *Finitor* shall become the East *Azimuth*; and every 30th. *Azimuth* from the *Limb*, or *Axtree* line, is a *Domifying* Circle: you shall therefore in stead of *Azimuths* 19 $\frac{1}{2}$, and 47. (which are *Domifiers* after *Regiomontanus* for our Latitude, as was shewed Chapters 49, 50.) take *Azimuths* 30. and 60. on both sides the *Axtree* line, which are distinguished to your hand; and with these *Domifiers* you shall work in all respects as you did with the other in the three former Chapters.

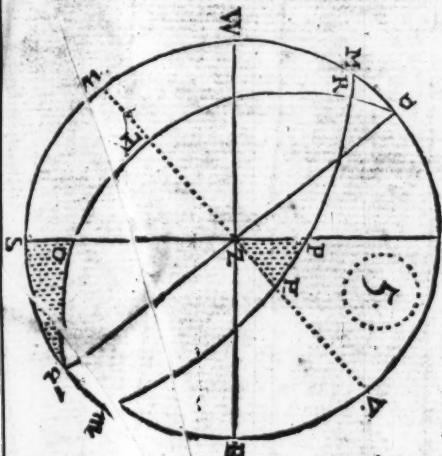
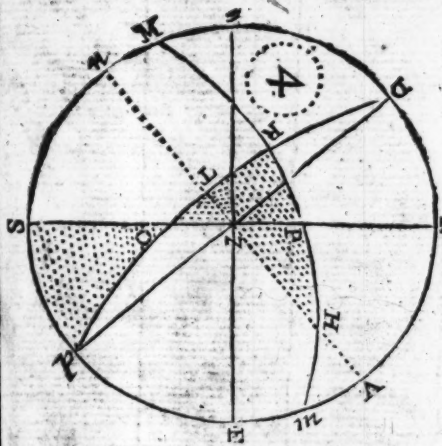
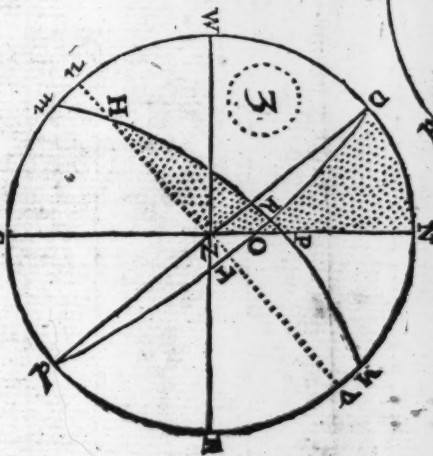
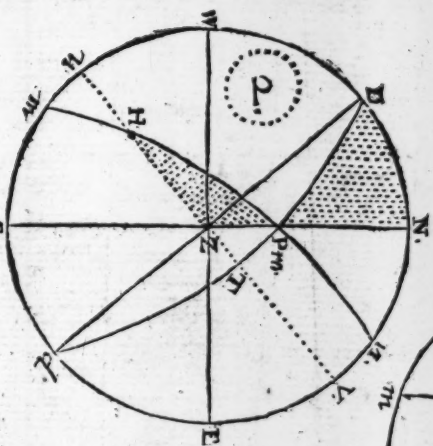
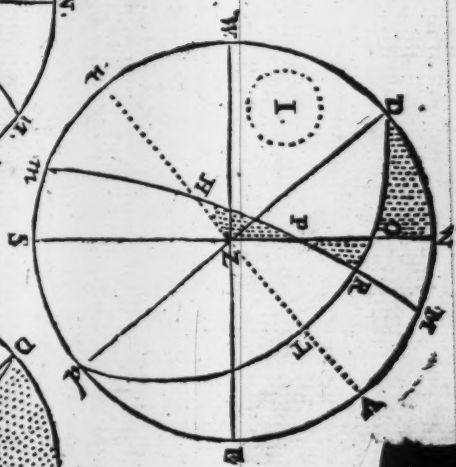
CHAP. LIIII.

How to Direct a Figure.

TO Direct is to turn on the Sphear, till some Star in the second House come into the first, or contrarily: and so observe how many degrees the Equinoctial is moved forward or backward in the same time.

Place the Star or Planet on the *Reet*, or on the *Label*, (as Chapter 18. is taught, then in the Equinoctial Projection (as Chapter 47.) set the Ascendent at your Horizon, and note the degree Culminating: then turn on the *Reet* forward or backward till the Star come to the Horizon: then lay the *Label* on the degree which Culminated before; and mark how many degrees of the *Limb* he is distant from noon, so many degrees of the Equator have passed the Meridian and Horizon: which *Astrologers* take to signifie so many years before the effect promited by the said Star shall happen.

Appendix,



Appendix, Concerning Judiciarie Astrologers.

Some learned Artists may perhaps think that these 8. last Chapters pertaining to *Astrologie* might be spared; and I think so too: but that I foresee they may be of use to such as would examine the errors and fallacies of *Astrologians*. *Astrology* of old was no more then *Astronomy*, an Ingenious Science, leading a Man to the knowledge of that which may be known, and ought to be Studied, the greatness and wisdom of God manifested in his works. But *Astrology*, as the word is now commonly used, is *Ægypti* *Art.* 19. 19. and *ἡνδρόμου* *γνώσις* 1. *Tim.* 6. 20. Teaching Men to search into that which neither can be known, nor ought to be Pryed into; Con-tingencies to come, which belong to God onely to know, and re-veal. *Esa.* 41. 23. Tell us things to come, (saith he) that we may know that ye are Gods. And *Favorinus* an Heathen Philoso-pher could say, *Tollitur quod maxime inter Deos atq; homines differt, si homines quaq; res omnes futuras prænoscerent.* This kind of *Astrology* God derides by his Prophets, and forbids to his People, *Esa.* 47. 12, 13. He saith to *Babylon*, where this Art then flourished. Stand now with thine Inchantments, and with the Multiitude of thy Sorceries, wherein thou hast laboured from thy Youth; if so be thou shalt be able to profit; if so be thou mayest prevail. Thou art wearied in the Multiitude of thy Counsels: Let now the *Astrologers*, the *Star-gazers*, the monthly prognosticators stand up, and save thee from these things that shall come upon thee. *Jerem.* 10. 2. Thus saith the Lord, Learn not the way of the Heathen, and be not dismayed at the signes of Heaven: for the Heathen are dismayed at them. For the customes of the people are vain.) And it was one of the pre-fages of their Captivity, when they began to be replenished with those Eastern Arts, and to be South-sayers, like the *Philistims*, *Esay* 3.

I have seen what glosses have been put upon some of these Texts: and how the judgements of Mr *Perkins*, and Mr *Gataker*, are slighted by some late pretenders to *Astrology*; whereat I wonder not: having seen the works both of the one side, and of the other.

Judiciary Astrology hath two parts, The *Meteorological*, and the *Genethliacal*. And against both there are these just exceptions. 1. Whereas about the time of *Nabonassar*, or soon after, the Heaven was divided upon the Poles of the *Ecliptique* into 12. Spaces, called *Dodecatemoria* and Signes: and the *Astrologers* of the next Ages ascribed to these spaces certain vertues or Powers over the several parts of Mans Body, and over the several Countreys and Nations of the World: especially by reason of the qualities they supposed to be in the fixed Stars; which then occupied those spaces: their Rules are still observed, notwithstanding that those Stars are removed into the succeeding spaces. For those Stars which in *Nabonassar's* time were in the *Dodecatemoria* of γ , are all removed into the *Dodecatemoria* of δ , and π ; and those of κ and ω are come in their roomes: for the fixed Stars are found to pass through a whole Signe, that is, a 12th. part of the Compass of the Heaven, in 2118. Years; and it is now above 1400. Years since *Ptolemie* wrote, and above 2400. since *Nabonassar* began his Reign. 2. That *Astrologers* scarce look beyond the *Zodiacke* for their *Aspects*, whereas the fixed Stars on the North and South may have, for ought they know, as operative configurations with the Planets, as the Planets one with another. 3. That their own Rules are so manifold, and the Planets and fixed Stars and their *Aspects* also are so many, and so divers in qualities and degrees, that it is impossible to judge what effect the mixture of those influences shall produce: especially considering that from the beginning of the World to this time, the Heavenly bodies never had twice the same posture: and therefore there wants experiment to build the Art upon.

For the *Meteorological* part, I was much helped by the Studies of my Father, who for 10. Years did most curiously observe all changes of Wind and Weather; while I was waking; and noted them daily over against the dayes in *Magnus* his *Ephemerides*. His conclusion was, that he could find no certainty in the rules of *Astrology* commonly received, nor frame any other upon his experience. Yet had I a mind to try a little further, and about the Year 1631. and forward for some years, I made dayly Observations of all Winds and Weather at home, and got also the best information I could by Letters from Friends abroad; by relation of Travellers, *Journals* of Sea-men, *Currantries* (as they were

were then called) *Mercurius Gallabegicus*, &c. And I found so great diversity of Weather in the same Climate, and sometime in places scarce three degrees distant in Longitude or Latitude, that I despair'd of Prognosticating Weather, till I could learn which way the Wind would list to blow. This among my Observations is memorable, that the Weather *Capt. James* had in his Voyage, Wintering, and return from the Mid-land Sea of *America*, was very divers from ours, and oft times contrary; and all the agreement I could find, was, that one day when it Thundred in *America* very fore, we had Thunder 18. hours after: yet he was many moneths in *Charlton Island*, which is in our Latitude; where his Ship was so Frozen, and the Sea so full of Ice, that he could not sail till *May*. And I know a learned Gentleman that used for a recreation at *Christmas* time to put a Dozen new Almanacks into the hands of so many of his servants, and set them to read in order the several judgements of the Prognosticators about the Weather; wherein he found as good sport as *William Duke of Mantua* did in reading the judgements of several *Astrologers*, upon a Figure erected upon the Nativity of his young *Mule*.

For the *Genethliacal* part, since Planets signifie diversly according to the Houses in which they are, it were very needfull for Men of this craft, first to demonstrate how the Houses ought to be divided, before they undertake to give any judgement: but herein they are not agreed: those Stars which after *Ptolemy* are in one House, and signifie thus; after *Regiomontanus* are in another House for the same time and place, and so signifie otherwise. Of the four ways above mentioned Chapter 48. I cannot say which is best: but that of *Regiomontanus* which is now most followed, and called by some the Rational way, seemes to me the most Irrational of all, because of the very unequal division of the Houses: for let a man Erect a Figure for *Wardhuys* in *Norway*, after that way, and he shall find the 4 Houses next the Meridian, viz. 3, 4, 9, 11. hugely great, each of them containing above a seventh part of the Sphear; and the 4 Houses next the Horizon each of them not to contain a twenty fourth part; he shall also observe that all the Stars within 48 degrees of either Pole (which take up a full third part of the Sphear) are perpetually confined to two Houses; for that Parallel; though in warmer Climates some of them have a little more liberty; but *Ptolomie* and *Al-*

cabinius gives every Star the Liberty of all the Houses, and *Campanus* Imprisons but a few.

I could never see any good reason why the influences of the Stars should make more impressi^on upon the Child in the moment of his Nativity, then they did at any time before in the Womb. If mines in the Earth are not hidden from the influences of the Stars, neither is the Child in the Mothers belly. If the Stars have such operation on Men in their Nativity, it is rati^onall to think they have more force in their first conception; when the matter is fluid and more apt to receive impressi^on, then when the Child is shaped, and the temper more confirmed: and this *Johannes Angeli* an old *Astrologer* considering, framed a Table to discover to a minute the time of conception, by the time of the Birth given, where he extends the time of gestation to 40. Weeks, and (as I remember,) 6 dayes over; but he doth not tell us whether he made that Table by experience, or divination; nor how many experiments he had used for the triall of it.

Favorinus once demanded of these *Genethliacal* men, who pretend to know mens Fortunes by the Positi^ons of the Stars in their Nativity. How it comes to pass that thousands of people, of both Sexes, of all Ages, born in sundry places, and under sundry configurations of the Stars, have hapned to perish in the same hour and moment, and by the same misfortune, as by Shipwrack, Stormes of War, Earth-quakes, fall of Buildings, and such like accidents? And whether this fate could have been foreseen in all the Figures Erected for their several Nativities? Which demand I think never yet received any good answer.

This also I have long observed that no Man (so far as my knowledge and intelligence reacheth) are so Fortunate in setting Figures for discovering things lost, or Prognosticating of Life and Death, as some who scarce know (*Charles Wain*, nor any Planner in the Skie beside the Sun and Moon: and some of these have given out that I allowed of their practises, before ever they consulted me, and so gave me occasion to make this digressi^on. He that would see more of this argument may read what my Lord *Howard*, sometime Earle of Northampton, and Mr *Perkins* have written thereupon. *Pliny Book*- 30. Chapter. 2. hath recorded *Nero's* experiment and judgement of this Art. *Species magiae plures sunt; namq; & ex Aquâ, & ex Spheris, & ex Aere, & Scellis,*

Stellis, & Lucernis, ac Pelvibus, securibusq;, & multis alijs modis divina promittit: preterea umbrarum, inferorumq; colloquia: qua omnia aiaie nostrâ princeps Nero vana falsiq; comperit: quippe non Citharæ tragicique cantus libido illi maior fuit, fortuna rerum humanarum summa gestiente in profundis animi vitijs: Primumq; imperare Dijs concupivit, nec quicquam generosius voluit. Nemo unquam ulli artium validius favit: Ad hac non opes ei defuere, non vires, non discendi ingenium; aliaq; non patiente mundo, Immensum & indubitatum exemplum est falsa artis, quam dereliquit. Nero, as if he had said, What shall the Man do that comes after the King? And a little after, Proinde ita persuesum sit, intestabilem, irritam, inanem esse, habentem tamen quâsdam veritatis umbras, sed in his veneficas artes pollere, non Magicas. The judgement also of Favorinus, a learned Philosopher, is worthy to be here rehearsed, as it is reported by A. Gellius Noct. Attic. 14. 1. With whose words I will end this digression.

Cavendum ne qua nobis isti Sycophantæ ad fidem faciendam irrepent, quod videremur interdum vera effutire aut spargere. Non enim comprehensa (inquit) neque definita, neq; percepta dicunt, sed lubrica atq; ambagiosa conjectatione nitentes, inter falsa atq; vera pedetentim quasi per tenebras ingredientibus eunt: & aut multa tentando incidunt repente imprudentes in veritatem; aut ipsorum, qui eos consulunt, multa credulitate ducente perveniunt callide ad ea qua vera sunt: & ideo videntur in præteritis rebus quàm in futuris veritatem facilius imitari. Ista tamen omnia qua aut temere aut astute vera dicunt, præ ceteris qua mentiuntur, pars ea non est millesima. And a little after, Idem Favorinus deterrere volens ac depellere adolescentes a Genethliacis istis, & quibusdam alijs id genus, qui prodigiosis artibus futura omnia dicturos se pollicentur, nullo pacto adendos esse consulendosq; huiusmodi argumentis concludebat. Aut adversa (inquit) eventura dicunt, aut prospera: si dicunt prospera, & fallunt; miser fies frustra expectando: si adversa dicunt, & mentiuntur: miser fies frustra timendo sin vera respondent, eaq; sunt non prospera; jam inde ex animo miser fies antequam è fato fias: si felicia promittunt, eaq; eventura sunt, tum plane duo erunt incommoda: & expectatio te spe suspensum fatigabit: & futurum gaudij fructum spes tibi jam defloraverit; nullo igitur pacto notandum est istiusmodi hominibus res futuras presagientibus.

CHAP. LV.

To find the Angles of the Ascendent, or the Angle of the Ecliptique with the Horizon, and the Altitude of the Nonagesimus gradus, at any time.

IN the Equinoctial Projection set the Suns place to the time proposed, and get the Altitude of *Culmen Cali*, by Chapter 46. Then, if the Eastern arch of the Ecliptique be shorter then the Western, you shall count the degrees between the Ascendent and Mid-heaven; otherwise count from the Descendent to Mid-heaven. Number these degrees on the *Label* from the Center, and where they end make a prick; which prick if you put upon the Parallel of the Altitude of *Culmen Cali*, you shall have in the *Limb*, between the *Finitor* and the *Label*, the measure of the lesser angle, which taken out of 180 degrees leaveth the greater angle. This is done by Probleme 2. Rectang. And note that the lesser angle, and the Altitude of the *Nonagesimus gradus* be always equal.

Example. March 29. 1652. 10. hours 32. minutes *a. m.* $\propto 25\frac{1}{2}$ was in *Culmine*: the Meridian Altitude thereof is 36. Between *Culmen* and the Descendent I find $61\frac{1}{2}$. therefore I prick the degree $61\frac{1}{2}$ from the Center in the *Label*; and when I have turned that prick to the 36. *Almicantar*, the *Label* shewes in the *Limb* of the *Rect* 42 degrees for the lesser angle of the Ecliptique with the Horizon (exactly 41. 58 minutes) which also is the Altitude of the *Nonagesimus gradus*; the greater angle is 138 degrees 2 minutes.

Another way. In the Equinoctial Projection: lay the *Label* on the *Nonagesimus gradus*, and observe his Declination on the *Label*, and his Horary distance from the Meridian. Then in the Meridional Projection and his first mode, observe where that Declination and Horary distance meet on the *Mater*, and the *Almicantar* touching the same point sheweth the Altitude of *Nonagesimus gradus*, which is equal to the angle sought.

Example. In the former Case, where $\propto 25\frac{1}{2}$ was in our Meridian, $\gamma 24$. was *Nonagesimus gradus*; the *Label* laid to it shewed me his Declination $9\frac{1}{2}$ almost, North: and his Horary distance

distance from the Meridian in the *Limb* 26. 20 minutes, then the *Finitor* being set to the Latitude, I seek the Intersection of the $9\frac{1}{2}$ Parallel of North Declination with the $26\frac{1}{3}$ Meridian from the *Limb*: and there toucheth the 42 *Almicantar*; shewing the Altitude of *Nonagesimus gradus*, and the quantity of the lesser angle sought, as before. And there cometh unasked also, the $36\frac{1}{3}$ *Azimuth* being the *Azimuth* of the *Nonagesimus gradus*, which is alwayes equal to the Amplitude of the Ascendent. Other wayes, See Chapter 56. and 57.

CHAP. LVI.

The Ascendent and his Amplitude, and the Altitude of Culmen Caeli given; so to represent the Ecliptique, that you may presently find not onely the Altitude of the Nonagesimus gradus, but the Altitude and Azimuth of every degree of the Ecliptique at one view.

S Et your Planispher in the third Mode of the Meridional Projection: that is, If the Ascendent be a North Signe, move the *Finitor* from *Meridies* toward the North Pole, till the North Pole be elevated above the *Finitor* according to the elevation of *Culmen Caeli*; but if the Ascendent be a South Signe, move the other end of the *Finitor* from *Septentrio* toward the North Pole, till the Pole have the Elevation of *Culmen Caeli*. Then number the Amplitude of the Ascendent upon the *Finitor* from the Center to your left hand, (toward *Septentrio*) and take the Meridian that crosseth there for the Eastern arch of the *Ecliptique*, and his match so much distant from the Axtree towards *Meridies* shall be the Western arch; so do the *Azimuths* and *Almicantars* of the *Reet* shew at once the Altitude and *Azimuth* of every degree of the *Ecliptique*.

Example, *March 29. 1652. 10. hours 32 min. a. m.* I found $\times 25\frac{1}{2}$ Culminating, and his Meridian Altitude (by Chapter 46) 36 degrees, the Ascendent $\ominus 24$. (by Chapter 47.) and his Amplitude $36\frac{1}{3}$ (by Chapter 15, and 16.) the Sun being then Eclipsed in $\vee 19. 11$ minutes. I would know his Altitude and

Azimuth, and likewise the *Altitude* and *Azimuth* of the *Nonagesimus gradus*. To this purpose, I take the North Pole for *Culmen*, and set the *Finitor* 36. below him toward *Meridies*; and from the Center toward my left hand, I number on the *Finitor* the Amplitude of the Ascendent $36\frac{1}{3}$, there cuts the twenty third Meridian from the Axis: (which here serveth for the Eastern arch of the *Ecliptique* :) the degree in this *Ecliptique* here cut by the *Finitor* is the Ascendent \odot 24. thence I number in this *Ecliptique* South ward 90 degrees by help of the Parallels, and so I come to γ 24 degrees, being the *Nonagesimus gradus*. Here the 42 *Almicantar* toucheth the *Nonagesimus gradus*, shewing the *Altitude* thereof, and here also cutteth the *Azimuth* of the *Nonagesimus gradus* $36\frac{1}{3}$ equal to the Amplitude of the Ascendent, as it is alwayes and ought to be; so as that you might have found the *Nonagesimus gradus* by this *Azimuth* with less numbring. Now for the Sun, he is in γ 19. 11 minutes, that is, nearer the Meridian then the *Nonagesimus gradus* by almost 5. degrees: I count therefore 4. 49 minutes (for so it is) past the *Nonagesimus gradus*; there is the Sun, and the *Almicantar* cutting there shewes his *Altitude* $41\frac{2}{3}$, and his *Azimuth* is shewn by the 29 *Azimuth* some what near. Or if you would reckon after the order of the Signes, which is easier, begin at the Descendent, where is ν 24. thence $61\frac{1}{2}$ makes κ $25\frac{1}{2}$ at the Pole, for *Culmen Cali*: thence in the Eastern arch to the Suns place I make 85 degrees 11 minutes; and 4. 49 minutes further is γ 24. the *Nonagesimus gradus*.

CHAP. LVII.

To do the same another way, by the Horizontal Projection, very plainly.

TAKE the Zenith for the Ascendent, and set him in his place in the *Limb* (which here is *Horizon*) so much from *Oriens* as his Amplitude comes to; and that toward *Septentrio*, if it be a Northern Signe, or if it be a Southern Signe toward *Meridies*. Then number upon the Meridian line from the *Limb* inwards the *Altitude* of *Culmen Cali*, and the *Azimuth* that cutteth there shall be your *Ecliptique* in this Case: If the *Azimuths* reach not the Meridian, turn

turn about the *Rect*, and set *Nadir* for *Ascendent*. Lay the *Label* to any degree of this *Ecliptique*, and the degrees of the *Label* from that degree to the *Limb* shall be the *Altitude* thereof: and between the *Label* and *Meridies* in the *Limb* the *Azimuth* thereof.

Example. Because in the Case of the former Chapter I foresee that the Sun will be past the *Nonagesimus gradus*, and so in the West Quadrant of the *Ecliptique* (though he be in the East Quadrant of the Horizon) therefore I set *Nadir* at the Amplitude of the *Ascendent* viz. $36\frac{1}{3}$ from *Oriens* North-ward, then in the Meridian line I number from the *Limb* inwards 36. for the *Altitude* of *Culmen*, where I make a prick, and say, Here is $\times 25\frac{1}{2}$ *Culminating*, and through that prick passeth the 42. *Azimuth* from the *Limb*, which is now my *Ecliptique*; and by that I see that the angle of the *Ecliptique* which the Horizon (called the angle of the *Ascendent*, and alwayes equal to the *Altitude* of *Nonagesimus gradus*, as was said) is 42 degrees: and if I follow this *Azimuth* to the *Finitor*, there is *Nonagesimus gradus*, and the *Altitude* thereof 42 degrees counted from the *Limb* (here Horizon) the *Azimuth* thereof lies in the *Limb* between the *Finitor* and the Meridian $36\frac{1}{3}$ as before, equal to the Amplitude of the *Ascendent*, I number also from $\times 25\frac{1}{2}$ in the Meridian 23. 41 minutes to the left hand still, and there I have $\gamma 19. 11$ minutes, the Sun's place, which cuts on the *Label* $41\frac{2}{3}$, for the *Altitude* of the Sun there, and the *Label* at the same time cutteth in the *Limb* about 29. from South East-ward for the *Azimuth* of the Sun; and after the same manner you have before you the *Altitude* and *Azimuth* of every other degree of the *Ecliptique* for the time proposed.

CHAP. LVIII.

To do the same by the *Nonagesimal Projection*, if the *Altitude* of *Nonagesimus gradus* be first given instead of the *Altitude* of *Culmen Cæli*.

S Et your Planispher in the *Nonagesimal Projection* (by Book 2. 3.) that is, make the *Limb* now to represent the Circle of Longitude or *Azimuth* (for it is both) which cutteth

cutteth the *Nonagesimus gradus*, and make the Equinoctial line here to be Horizon: and from the Equinoctial line number in the *Limb* the Altitude of *Nonagesimus gradus*, and thereto set the *Finitor*, so shall the *Finitor* be *Ecliptique*, the *Nonagesimus gradus* at the *Limb*, the Ascendent and Descendent at the Center; and because the Equinoctial line is Horizon in this Projection, therefore the Meridians become *Azimuths*, and the Parallels *Almicantars*, shewing the Altitude and *Azimuth* of every degree of the *Ecliptique*, if you reckon as you ought in this manner. Reckon in the Equinoctial line (here Horizon) from the Center the Amplitude of the Ascendent, to the right Hand, if it be a North Signe, and contrarily if it be a South Signe. Where this Amplitude ends is the East point, from whence you shall reckon all your *Azimuths*. Count thence to the *Limb* and back again (if need be) in the said Equinoctial line, till you have made 90 degrees, there is your Meridian, as far distant from the *Limb*, as the East point was from the Ascendent. Follow this Meridian to the *Finitor*, and there he shewes you *Culmen Cali*, and the Parallel there cutting shewes the Altitude thereof. Now may you find every degree of the *Ecliptique* above the Horizon, if you know but what Ascends, or Descends, or Culminates; and of every such degree the Parallels shew you the Altitude, and the Meridians shew his *Azimuth*, if you begin your numbring from the East or South *Azimuth*.

Example. When \odot 24 degrees was Ascending (as in the Example before used) as by consequence \vee 24. in *Nonagesimo gradu*, $\textcircled{3}$ was in $\textcircled{8}$ 4. 45 minutes, and had but 3. or 4. minutes South Latitude: I would know $\textcircled{3}$ his Altitude, and *Azimuth*, setting go the *Finitor* above the Equinoctial line 42 degrees (which is the Altitude of *Nonagesimus gradus*) I say, because the *Nonagesimus gradus* at the end of the *Finitor* in the *Limb*, is \vee 24. therefore I must count back 10. 45 minutes toward the Ascendent for *Mars*, and there the Parallel 41 degrees with 10 minutes cutteth the *Finitor*, for the Altitude of $\textcircled{3}$, and the 14th. Meridian East-ward from the *Limb* gives me his *Azimuth*, which if I begin to reckon from the East point, falleth out to be almost the 40th. *Azimuth* from the East. *Mars* his Latitude here is not regarded.

CHAP. LIX.

The Nonagesimus gradus, and his Altitude and Azimuth given, as in the former Chapter. How in the same Projection to get the Altitude and Azimuth of any Planet or Star, by his Longitude and Latitude.

Your Planisphaer set as in the former Chapter: you shall number the Longitude of the Star upon the *Finitor*, (here *Ecliptique*) beginning at the Descendent or *Nonagesimus gradus*; and in the *Azimuth* serving his Longitude, count his Latitude by the *Almicantars*, at the end of which account is the Stars place for this time. The Parallel cutting there shewes his Altitude, and the Meridian cutting there shewes his *Azimuth*, if you count from the East point as you were taught in the former Chapter.

Example, *Lucida Pleiadum* was in Longitude γ 25. 10 minutes, Latitude 4 degrees 00 minutes North. Therefore from the *Nonagesimus gradus* γ 24. I number in the *Finitor* toward the Ascendent 31. 10 minutes, and there is the Longitude of *Lucida Pleiadum*; in the *Azimuth* that cuts here I go up Northward 4 degrees, and there I make a prick for *Lucida Pleiadum*. Now the Parallel $38\frac{1}{2}$ shewes me his Altitude, and the 48th $\frac{1}{2}$ Meridian from the Center, shewes me that *Lucida Pleiadum* is gone $48\frac{1}{2}$ in *Azimuth* from the Ascendent, but from the East point onely 12 degrees 10 minutes.

CHAP. LX.

The Altitude and Azimuth of any Star taken, and either the Ascendent, Nonagesimus gradus, or Culmen Cæli known: How by the same Nonagesimal Projection to find the Stars Longitude and Latitude.

IF you know either the *Ascendent*, *Nonagesimus gradus*, or *Culmen Cæli*, you have enough to put your Planisphaer in the *Nonagesimal Projection*, by the former Chapters. And your Planisphaer so set, you shall seek out the Meridian, which

which standeth for the *Azimuth* in which you observe the Star; and therein number from the Equinoctial line the Altitude observed: the *Azimuth* and *Almicantar* cutting there shew the Longitude and Latitude of the Star inquired. If the *Azimuths* reach not the place of the Star, turn the *Reet* half round, and let the *Zenith* and *Nadir* points change places; and your turn is served.

Example. *Febr.* 13. 1657. I observed (somewhat near) that Υ was gone West-ward from the Meridian in *Azimuth* 14 degrees, and that his Altitude was 61 degrees; *Sirius* was then in the Meridian, by which I have the *Ascendent*, *Culmen*, and *Nonagesimus gradus*, any or all of them given. For when in the Equinoctial Projection I bring *Sirius* to the Meridian line, it is all one as if I had set the Sun's place to the hour of the Night (by Chapter 46.) and I see there Culminates with *Sirius* \ominus 7. 10 minutes, whose Meridian Altitude (by the 46.) is 61. 5 minutes; and I see \simeq $5\frac{1}{2}$ ascending in my Horizon, and \simeq $5\frac{1}{2}$ descending; therefore \ominus $5\frac{1}{2}$ is *Nonagesimus gradus*, which is 90 degrees distant both from the Ascendent and Descendent: his Altitude (by Chapter 55.) 61. 10 minutes almost. Therefore I set the *Finitor* 61. 10 minutes above *Meridies*, (as Chapter 58.) and in the *Finitor* at the *Limb* I count \ominus $5\frac{1}{2}$ *Nonagesimus gradus*; thence I go inwards in the *Finitor* 1. 40 minutes where I come to \ominus 7. 10. the degree of Culmination; this degree is cut by the 4th. Meridian from the *Limb*, whereby I learn that this 4th Meridian will be the Meridian of my place, and that the Amplitude of the *Nonagesimus gradus*, and likewise of the Ascendent, is 4 degrees. Now to place Υ in the *Mater*, I count his *Azimuth* first, beginning from the Meridian of my Place now found. First I reckon up from the *Culmen Cali* to *Nonagesimus gradus* in the *Limb* 4. degrees, (for so much the *Nonagesimus gradus* is West of the Meridian) and thence back again, I tell to the 10th. Meridian from the *Limb*, which maketh the 14th. *Azimuth* from *Medium Cali*, in which *Azimuth* I observed *Jupiter* in that Meridian; (used here for the 14th. *Azimuth*) I reckon the Altitude of *Jupiter* from the Equinoctial line, 61 degrees, and at that Altitude I make therein a prick for the place of Υ : And immediately I see this prick standeth a quarter of a degree above the *Finitor*; shewing the Latitude of Υ 15 minutes North, and it is cut by almost the 5th. *Azimuth* from the *Limb*, which sheweth me that the

the Longitude of \mathcal{U} is 4. 50 minutes less then the Longitude of *Nonagesimus gradus*; and therefore that \mathcal{U} is in \mathfrak{S} 0, 40 minutes.

CHAP. LXI.

The Latitude and Azimuth of a Star, and either the Ascendent, Nonagesimus gradus, or the Culmination given, to find his Longitude.

Y Our Planispher being set in the *Nonagesimal Projection*, (as in the former Chapter) seek the Meridian that serveth for the *Azimuth* of the Star, and mark where it cutteth the *Almicantar* serving for the Parallel of the Stars Latitude. The *Azimuth* cutting there shewes the Longitude, which you shall reckon from the *Ascendent*, or *Descendent*, or *Nonagesimus gradus*; whose Longitudes are known, as was shewed in the former Chapter.

Example. Suppose \mathcal{U} his *Azimuth* observed 14 degrees from South Westward (as Chapter 60.) and suppose his Latitude known 15 minutes North: (Though I know the Tables make *Jupiters* Latitude here divers minutes less, that matters not to our purpose here) I say where the 10th Meridian (which by the former Chapter is the 14. *Azimuth* in this posture of my Planispher) cutteth the *Almicantar* $0\frac{1}{4}$ serving for *Jupiters* Latitude, there cutteth an *Azimuth* which gives me *Jupiters* Longitude, as in the former Chapter.

CHAP. LXII.

To find the Parallaetical Angle; that is, what Angle the Azimuth maketh with any point of the Ecliptique, by the Altitude of that point, and of the Nonagesimus gradus.

Number on the Label from the Center the Complement of the Altitude of the point proposed, (which may be known by Chapter 56.) and at the end of it make a prick, and having (by Chapter 55. or otherwise) the

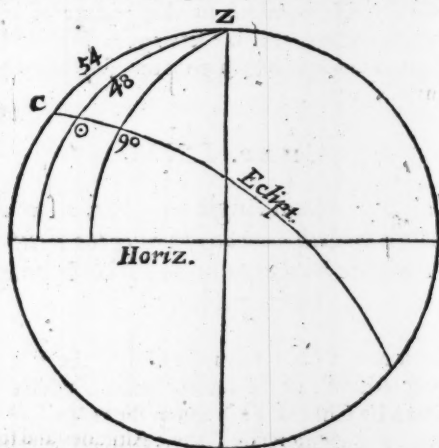
Altitude of *Nonagesimus gradus*, turn the prick you made on the *Label* to touch the *Almicantar*, which is Complement of that Altitude: then in the *Limb* of the *Reet* between the *Finitor* and the *Label* is the quantity of the angle.

Example. In Chapter 56. the Altitude of the Sun in the middle of the *Eclipse* which hapned *March 29. 1652. 10. hours 32 minutes a. m.* was 41. 47 minutes, and the Altitude of *Nonagesimus gradus* 41. 58 minutes; wherefore I make a prick on the edge of the *Label* at 41 $\frac{3}{4}$ counted from the *Limb*, (or I count the Complement hereof from the Center, and make the prick) and having turned that prick to the fourth second *Almicantar* from the *Zenith*, I find the *Label* shewing 87 degrees in the *Limb* of the *Reet*, the quantity of the angle.

But because the *Label* here cutteth the *Almicantar* so slope that you can hardly observe the just point of Interfection, I will shew you another way.

The Complement of the Altitude of *Culmen Cali*, the distance of the point proposed from *Culmen*, and the Complement of Altitude of the said point, make a Triangle; whose 3 sides are all known, or may be known by the Chapters foregoing: Therefore by the first Probleme of Obliquangled Triangles you may find the angle.

Example. I set the Complement of the Suns Altitude Z ☉

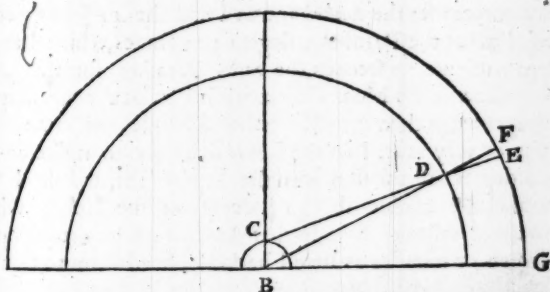


for A B in the *Limb*, and marking where the 54th Parallel, counted from the Pole meets with the *Almicantar* 23. 41 minutes, (counted from the *Zenith*,) there I find the *Azimuth* 93. 19 minutes, shewing the greater angle at the Sun, whose Supplement 86. 41 minutes is the lesser angle sought; and this lesser angle below the *Ecliptique* is alwayes Westward in the West Quadrant, and contrary in the East. In the first way you resolve the Rectangled Triangle Z. 90. \odot , by the Probleme 2. Rectang. and third Variety: in the second way you resolve the Oblique Triangle Z \odot C by Probleme 1. of Obliqueangled Triangles,

CHAP. LXIII.

To find the Parallax of Altitude of the Sun, or Moon.

THe true Altitude of the Sun, or Moon, ought to be observed in the Center of the Earth, whereto the Tables are conformed: but because we dwell upon the Superficies of the Earth almost 4000 English miles from the Center, therefore the Planets seem lower to us then indeed they be. Suppose a Man observed the apparent Altitude of the Moon at C on the Superficies of the Earth to be E G 10 degrees; he that could observe it in the Center at B might find the



true Altitude F G almost 11 degrees. Now the smal angle at D (being equal to the difference of these Altitudes, and subtended on

this side by the Semidiameter of the Earth B C, and on the further side by the arch of the difference of these Altitudes in the *Primum mobile*,) is called the angle of the Parallax of Altitude. This Parallax is greatest in the Horizon, and decreaseth as the Planet riseth higher, till in the *Zenith* it vanish into nothing: because there the line drawn from the Center falls into the line drawn from the Superficies of the Earth to the Planet, and makes therewith no angle at all.

To get the Parallax for any Altitude proposed, you must first get the Horizontall Parallax out of some Astronomical Tables: for it varies according to the Planets distance from the Earth; which is not alwayes the same; yet the Suns Horizontal Parallax you may alwayes reckon to be about 3 minutes, and the Moons Horizontal Parallax to be at the least 50 minutes, and at the most 68 minutes. This had, I number the Horizontal Parallax in the *Limb* from the Equinoctial line, and thereto lay the *Label*; and number the Altitude of the Planet on the *Label* from the *Limb*, and the Parallel that cuts that Altitude shewes the Parallax desired. And note here, that for every minute of the Horizontal Parallax you may reckon 5, 10, or 20, times so many, so that your *Label* rise not beyond 10 degrees in the *Limb*; so shall you attain the minutes more exactly.

Example. *March 29. 1652.* the Altitude of the Sun in the middle of the Eclipse was 41.47 minutes, and his Horizontal Parallax according to *Lantsbergius*, 2 minutes 18 seconds, for which I number 2 degrees 18 minutes from the Equinoctial line, and thereto set the *Label*; and so I find the $43\frac{3}{4}$ degrees of the *Label* to cut the Parallel 1 degree 30 minutes, which I am to accompt 1 minute 30 seconds, the Suns Parallax for this Altitude. Likewise the Moons Horizontal Parallax according to *Lantsbergius*, was then 62 minutes, her Altitude the same with the Suns, or very near; I set the *Label* therefore to make an angle of 6 degrees 12 minutes with the Equinoctial, and so I find the Parallel $4\frac{2}{3}$ cutting the $41\frac{3}{4}$ degree of the *Label*; which shewes the Parallax of the D in that Altitude $46\frac{1}{2}$, accounting every degree 10 minutes, as here I had appointed them to signifie.

CHAP. LXIV.

The Parallaſtick Angle, and the Parallax of Altitude given, to find the Parallax of Longitude and Latitude.

IF the *Azimuth* or Circle of Altitude make no angle with the *Ecliptique*, but be co-incident with it (as where the *Ecliptique* cuts the *Zenith*) then doth the Parallax of Altitude vary the Longitude only; and so much as the Parallax of Altitude is, so much is the apparent Longitude of the Planet greater then the true Longitude in the Eastern Quadrant of the *Ecliptique*, and so much lesser in the Western.

If the *Azimuth* make a Right angle with the *Ecliptique* (which it may do only in *Nonagesimo gradu*) then doth the Parallax of Altitude vary the Latitude onely; and so much as the Parallax of Altitude is, so much must be added to the apparent North Latitude, or subducted from the apparent South Latitude, to make the true Latitude of the Planet North or South. If the *Azimuth* cut the *Ecliptique* with Oblique angles (as most commonly it hapneth to do) then doth the Parallax of Altitude vary both the Longitude and Latitude. And the nearer the Planet is to the *Nonagesimus gradus*, the greater is the Parallax of Latitude, and the Parallax of Longitude less: and contrarily the further the Planet is from *Nonagesimus gradus*, the greater is the Parallax of Longitude, and the Parallax of Latitude the less.

The Parallax of Altitude is always the *Hypotenusa*, and the Parallax of Longitude and Latitude are the legs of a small Rect-angled Spherical Triangle, which may be called the Parallaſtick Triangle, and the leg which hath the Parallax of Longitude is a segment of the *Ecliptique*, or of a Parallel near it, and the leg which hath the Parallax of Latitude, is a segment of a Circle of Longitude passing through the apparent place of the Planet, and through the Poles of the *Ecliptique*, and cutting the *Ecliptique*, or his said Parallel at Right angles, as in the Figure.

C is the apparent place of the Planet.

B is his true place, in which he must be seen from the Center.

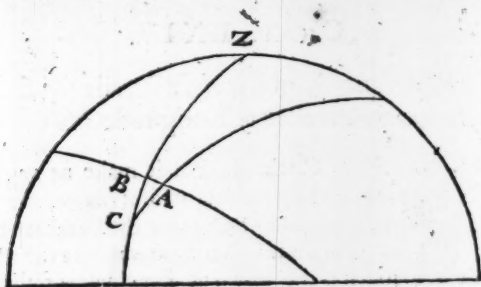
A B C is the Parallaſtick angle.

B C is the Parallax of Altitude.

B A the Parallax of Longitude.

C A the Parallax of Latitude.

Where-



Wherefore by the third Probleme of Rectangled Triangles, Book 3. 5. you may presendy get both the legs.

Example. The Parallaetical angle B, was found Chapter 62. to be 86. 41 minutes, and the Parallax of the Moons Altitude, (Chapter 63.) to be $46\frac{1}{2}$ minutes for the same time. Here therefore having laid the *Label* to 86. 41 minutes from the Equinoctial, I number in the *Label* from the Center 46 degrees and an half (in stead of 46 minutes and an half the Parallax of Altitude) and I find that the $46\frac{1}{2}$ Parallel cutteth the said $46\frac{1}{2}$ degree of the *Label*; by which I know that the Leg C A for the Parallax of Latitude is $46\frac{1}{3}$ very near, (for the Δ here being near the *Nonagesimus gradus* all her Parallax almost goes into Longitude,) but B A of my Triangle is covered by the head of my *Label*. Nevertheless I may see his measure in any of the Parallels to be $3\frac{1}{2}$ minutes for the Parallax of Longitude, for it is the $3\frac{1}{2}$ Meridian from the Axis, which cutteth $46\frac{1}{2}$ of the *Label*: and if I had not this shift, I might have my choice of other shifts, shewed Book 3. the 8, 9, 10, 11, 12, and 13th. Chapters.

The Suns Parallax of Altitude Chapter 63 for the same time was found 1 minute $\frac{1}{2}$. therefore laying the *Label* to the Parallaetique angle (as before) I number on the *Label* for the side B C (the Suns Parallax of Altitude, being 1 minute $\frac{1}{2}$) 9 degrees; so every degree here signifieth 10 seconds; and I find there cutting almost the 9th Parallel, shewing me that C A the Parallax of the Suns Latitude is 1 $\frac{1}{2}$ minute almost (that is almost as much as his Parallax of Altitude) and there cutteth also the Meridian $0\frac{2}{3}$, shewing me that the side B A, Parallax of Longitude, is almost 7 seconds.

The

The Sun therefore (though he never have Latitude) by reason of his Parallax, appeared in the middle of this Eclipse to have South Latitude $1\frac{1}{2}$ minute, the Moons true Latitude was then by *Lantsbergius* his Tables 45 minutes, 24 seconds North; so that by this accompt the Sun and Moons Centers were distant in Latitude 46 minutes, 54 seconds: but when out of this distance you have subtracted $46\frac{1}{3}$ for the Moons Parallax of Latitude, there remains 34 seconds for the apparent distance of the Centers of the Sun and Moon. But by Observation, I found them distant 1 minute 48 seconds: for the digits Eclipsed at *Edon*, were 11. $22\frac{1}{2}$ minutes; and so perhaps might I have found by my Planisphere, or some what near, had it been large enough, and had I regarded every minute and second precisely in setting down this Example, which were more then needed for my purpose in this place.

CHAP. LXV.

To find the Moons Latitude, by her distance from either of the Nodi, called Caput, and Cauda Draconis.

AS the *Ecliptique* crosseth the Equator with an angle of 23. 30 minutes for our Age, so the *Orbite* or Circle in which the Moon moveth crosseth the *Ecliptique*: but the angle of Inclination is not alwaies nor long the same: for in the *Conjunctions* of the Sun and Moon the angle is ever 5 00 minutes, and increaseth to the time of the *Quadrature*, when it is found 5 degrees 16 minutes; thence it decreaseth to the *Opposition*, where it is again but 5 degrees, as in the *Conjunction*; thence it increaseth again to 5 degrees 16 minutes in the latter \square , and again thence decreaseth to 5 degrees in the δ .

Get by the *Astronomical* Tables the quantity of the angle made between the *Ecliptique* and the *Orbite* of the Moon, (which in all *Conjunctions* and *Oppositions*, and therefore in all Eclipses is 5 degrees, as was now said) and get also by the like Tables the Moons distance from the nearest of the *Nodes*: then may you find the Moons Latitude, by the Probleme 3. Rectangled Triangles, Book 3. 5. just as you use to find the Suns Declination, by his Longitude and greatest Declination.

Example. The ν in the former Case was distant from *Caput Draconis* by *Lantsbergius* Tables 8 degrees 43 minutes. I lay

T

the

the *Label* from the Equinoctial line to 5 degrees in the *Limb*, and counting in the *Label* from the Center 8, 43. I see there the Parallel of $0\frac{3}{4}$ (that is, 45 minutes, or 46 minutes) crossing for the Moons Latitude.

CHAP. LXVI.

To find the Dominical Letter, the Prime, Epact, Easter day, and the rest of the moveable Feasts for ever, by the Calender, described Book I. II.

AN Example, shall serve here instead of a Rule. For the Year 1657. I would know all these: wherefore I seek the Year 1657. in the Table of the Suns Cycle, and over against it, I find 14. for the Year of the Cycle of the Sun, and D for the Dominical Letter. And note here, that every Leap-year hath 2 Dominical Letters (as 1660. hath A G) and the first (*viz.* A) serveth that Year till February 25, and the second (G) for the rest of the Year. And note that these letters go alwayes backwards when you count forwards (as B A, then G F, &c. not F G, and then A B) as you may see by the Table.

Then in the Table of the Cycle of the Moon, I have for the Year 1657. the Prime 5. the Epact 25. Those had, I go to the Table for Easter, and seek there in the first rank the Prime 5, and under it in the middle rank stands E; that is not my Dominical Letter; therefore I seek not backward, but alwayes forward in the middle rank, till I come to my Dominical Letter D. and under it I find in the third rank March 29. upon which Easter day falls this Year 1657. The rest of the moveable Feasts may be had by their distances from Easter, which are alwayes the same. One-ly for Advent Sunday, remember that the next Sunday after November 26 is Advent Sunday. Read Book I. II. and that will sufficiently instruct you with this Example.

CHAP. LXVII.

To find the age of the Moon, by the Epact,

Remember first that the Epact begins with March, which must be here accounted the first Moneth: Then if you add

add to the *Epaēt* the number of the Moneth current, and the number of the day of the Moneth current, the sum or the excess above 30. is the Moons age.

Example. *January* 20. 1656. According to the account of the Church of England, (who begin the Year with *March* 25. which was the Equinoctial day about Christ time) the *Epaēt* is 14. *January* is the 11th Moneth, and the 20th day is proposed; now add 14, 11, and 20. together, they make 45. out of which I take 30. and there remains 15. the Moons age.

This Rule is of good use. not onely to find the age of the Moon, and so her changes to a day, but also for examining of *Chronologie*, where the time is most certainly reckoned by Eclipses. But you must note, that if you apply this Rule to the Years past before *Anno Dom.* 1600. then for every 312. Years that the Year proposed precedes *Anno Dom.* 1600. you must subtract one day out of the age of the Moon, found by this Rule.

Example. *Picinus lib.* 1. Reports, That in the beginning of *Tiberius Caesar's* reign there was an Eclipse, of the Moon, and *Temporarius* saith, that whereas *Augustus* died *Aug.* 29. (I think he should say 19.) this Eclipse hapned *Sep.* 27. I would know whether it were possible for an Eclipse to happen that day, supposing the beginning of *Tiberius* to be in *August*, *Anno Dom.* 14. and *Anno Periodi Juliana* 4727. The *Prime* for that Year is 15, and the *Epaēt* 15. by Book 1. 11. add now to the *Epaēt*, for *September* 7. and for the day of the Moneth 27. and the sum is 49. out of which subducting 30. I leave the Moons age 19. but because *Anno Dom.* 14. precedes *Anno Dom.* 1600. 5. times 312. Years, therefore out of 19 I subduct 5. and there remains 14. the age of the Moon, corrected for *September* 27. *Anno Dom.* 14. Therefore it was about the full Moon: and it is possible the Moon might be Eclipsed then, as *Temporarius* saith. But it could not be Eclipsed *September* 27. *Anno Dom.* 13. for then the *Epaēt* being 4. the age of the Moon by the same Rule was 3. neither could it happen *Sep.* 27. *Anno Dom.* 15. for then by the same Rule the age of the Moon, was 25. at what age the Moon was far from her opposition to the Sun: and therefore could not be Eclipsed.

CHAP. LXVIII.

To find in what Parallel and Climate a Place is, by the Latitude given.

Parallels in *Geography* are lesser Circles Parallel to the Equator, and passing through the *Zenith* of a Place, and succeeding one another at such distance that at every Parallel the length of the day is varied a quarter of an hour.

A *Climate* is such a Parallel as altereth the length of the day half an hour. The Parallels and Climates begin from the Equator, under which the day is alwayes equal to the Night, and each 12 hours long: hence they count the Parallels and Climates Northward, and Southward: but because the Earth was not so far known to *Ptolomy* and the Ancient *Geographers*, as it hath been to those of later Times, therefore there is great difference between the Ancient and later *Geographers* about the number and quantity of the spaces contained by them: as among others *Kerkerman Syst. Geography, lib. 1.* hath shewed.

Yet may they easily be found to every Mans mind, by the Planispher in the Meridional Projection, thus. Find by 4. 17. what is the *Semi-diurnal* arch of the Sun in \odot , out of which, take 6 hours, and look how many quarters of an hour the double of the residue containeth, so many *Geographical Parallels* is the place removed from the Equator, and half so many Climates.

Example. I find the *Semi-diurnal* arch in our Latitude to be 8 hours 16 minutes, in the *Tropique* of *Cancer*; out of which taking 6. and doubling the residue, I have 4. 33. which is more then 9 half hours, or more then 18. quarters: so much our longest day exceeds 12 hours; therefore we should be past the 18th Parallel, and 9th Climate, viz. in the beginning of the 10th Climate, and 19th Parallel.

CHAP.

CHAP. LXIX.

*The Longitude and Latitude of two Places given,
to find their Distance.*

WHat Longitude and Latitude in *Geography* are, and how they differ from Longitude and Latitude in *Astronomy*, hath been shewed, Book 4. 5. 11.

If the places differ only in Latitude, and have one Longitude, bearing full North or South one from another; then take their difference of Latitude, by subducting the less out of the greater, if the places have both North Latitude, or both South Latitude: or take the sum of their Latitude, if one be North, and the other South. Then for every degree of this difference or aggregate number, you may reckon $69\frac{1}{2}$ English miles of the Statute, which ordaineth 1760. Yards to be a Mile: but of English Miles measured by common estimation, there go not above 60. to a degree; so that every such Mile that you Travel North or South shall alter your Latitude about one minute. If they differ in Longitude onely, and have no Latitude, but be both under the Equator, you shall reckon in like manner for every degree they differ in Longitude $69\frac{1}{2}$ Miles of distance.

In all other Cases you have a Triangle soluble by the second Problem of Obliquangled Triangles: of which Triangle the Complements of Latitude make the two comprehending sides, and the difference of the Longitudes of the places is the angle comprehended between them, and the third side is the arch of the distance of the places; which when you have found in degrees and minutes of a great Circle, you may turn into Miles as before: mark how the distance of two Stars is found by their Longitude and Latitude given, Chapter 37. in the same manner may you find the distance of two Cities or Towns.

Example. I would know the distance of *London* from *Jerusalem*. The Complement of the Latitude of *London* is 38. 28. minutes: the Complement of the Latitude of *Jerusalem* is 58. 05. minutes: the difference of their Longitudes 46. 0 minutes. I set the Zenith to the Latitude of *London* in the Limb, that is 38. 28. minutes from the Pole, so the Limb is the Circle of Longitude in which *London* standeth, then I seek the 46 Meridian from

that side of the *Limb* where *Zenith* is set for *London*, for that 46 Méridian is the Circle of *Jerusalem* Longitude: (because the difference of Longitude is 46.) Now because *Jerusalem* Latitude is 31. 55. and the Complement thereof, or distance from the Pole 58. 5 minutes, I walk on in the 46 Meridian till I come where the 58th Parallel from the Pole crosseth him, and there is the place of *Jerusalem*: the *Azimuth* that goes hence to the *Zenith* is the nearest way from *Jerusalem* to *London*: what *Azimuth* this is I regard not, for I enquire not the angle at *London*, but I observe by the Parallels how many degrees there be in him between the places of *Jerusalem* and the *Zenith*, and I find 38 degrees 20 minutes: which being resolved into Miles is 2300. Miles of common estimation, but Miles of the Statute 2664. the distance of *London* from *Jerusalem*.

CHAP. LXX.

The Latitude and distance of two Places given, to find the difference of Longitude.

THe Triangle will stand as in the former Chapter: there by two sides and the angle comprehended you sought the third side, by Probleme 2. Obliquangled Triangles: here by three sides given, you seek an angle by Probleme 1 Obliquangled Triangles.

Make the Pole, Pole: and set the *Zenith* to the Latitude of one of the places, as you did *London*, (Chapter 69.) 38. 28 minutes from the Pole, then number the Complement of the Latitude of the other place from the Pole, by the Parallels, and the distance of the two places from the *Zenith* by the *Almicantars*; and where the last Parallel and last *Almicantar* meet is C of your Triangle: (see Book 3. 14.) Now count how many Meridians there be between C and the *Limb*, so many degrees is the angle at the Pole sought, for the difference of Longitude.

Example. Having the distance of *London* from the Pole 38. 28 minutes, and of *Jerusalem* from the Pole 58. 5 minutes, and the distance of *London* from *Jerusalem* 2300. common English Miles, (of which 60. make a degree) I set the *Zenith* for *London* 38. 28 minutes from the Pole in the *Limb*, then because *Jerusalem* is distant from the Pole 58. 5 minutes, I go to the 58th Parallel

Parallel from the Pole, and lay one finger or the point of a bodkin on him; and because *London* is distant from *Jerusalem* 38 degrees 20 minutes, I count from the *Zenith* to the *Almicantar* 38. 20 minutes; now where this *Almicantar* crosseth the Parallel last found, there is C of the Triangle, and the place of *Jerusalem*; and you may see that you must cross 46. Meridians before you can go thence to the *Zenith* in the *Limb*; which sheweth that the angle at the Pole for the difference of Longitude is 46.

CHAP. LXXI.

To find what degree of the Ecliptique Culminates in another Country, at any time proposed, if the difference of Longitude be known.

IN the Equinoctial Projection, Bring the Suns place to the hour proposed, by help of the *Label*: and in the Noon-line you see presently what degree Culminates in your Country. (as Chapter 46, is shewed.) Now to know this for another Town, set the *Label* so many degrees from the Noon-line as the difference of Longitude requires, and that Eastward, if the place proposed be East, or Westward if it bear West; and so the *Label* shall cut the degree of Culmination, for the place proposed.

Example. If it be demanded what degree is Culminating at *Jerusalem* March 10. at 10. a clock before noon, I will set the Suns place γ 0. to the hour; and I see upon the Noon line, which is our Meridian, there Culminates \approx 28 almost. Now for the Meridian of *Jerusalem* I must lay the *Label* 46 degrees Eastward, that is from *Meridies* towards *Oriens*, and look what Star or degree of the *Ecliptique* is then cut by the *Label*, that is then Culminating in the Meridian at *Jerusalem*; (as here I find γ 17 $\frac{1}{2}$.) for in this Projection the *Label* (lay him where you will) is a Meridian.

CHAP. LXXII.

To find what a Clock it is in another Country, by knowing the hour at Home, and the difference of Longitude.

THis is done easily enough without an Instrument: for if you turn the difference of Longitude into hours and minutes, and add the same to your hours for any place which lies Eastward, or subtract the same for any place which lies Westward, you shall make the hour of the place.

Example. The difference of Longitude between *London* and *Jerusalem* is 46. or being converted into time 3 hours 4 minutes: therefore adding this to the time at *London*, I say, when it is noon at *London*, it is 4 minutes past 3 a clock after noon at *Jerusalem*: and when it is 2 a clock at *London*, it is 5. and 4 minutes at *Jerusalem*.

If you will do it by the Planispher, you shall do it in the Equinoctial Projection, thus. Whereas the *Limb* of your *Reet* is graduated into 360 degrees, if you distinguish the hours also at every 15th degree, beginning at the *Zenith* (which shall be 12) and numbring thence in the *Limb* of your *Reet* to your right hand or Westward, 1, 2, 3, &c. then shall you need to do no more but set the *Zenith* to the difference of Longitude, East or West from your Meridian, as the strange place happeneth to be situate: for then the *Label* laid to the hour of your Country in the *Limb* of the Mater, shall shew the hour of the other Country in the *Limb* of the *Reet*. And so the *Zenith* being laid to 60 degrees Westward, which is the Meridian of the *Ile* of *Barbados*. the *Label* laid to *Meridies* shall cut in the *Limb* of the *Reet* 8 of the clock before noon: which sheweth me that when it is noon with us, it is at *Barbados* but eight in the morning.

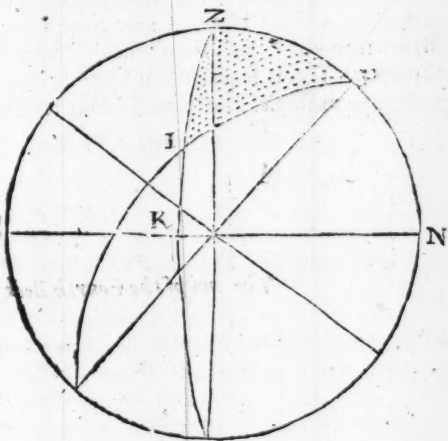
The end of the Fourth Book.

CHAP. LXXIII.

The Longitude and Latitude of one Place known, and the Rumb and distance of a second Place, to find both the Longitude and Latitude of the second Place.

S Et the *Zenith* to the Latitude of the first Place, then seek the *Azimuth* which serveth for the Rumb of the second Place, and in that *Azimuth* count his distance from the *Zenith*: where this distance ends there is the second Place, whose Latitude is shewn you by the Parallel which cutteth him, and the Meridian cutting there also, shews his Longitude.

Example, Let *Z* be London, and because *Jerusalem* beareth from London almost *S 6 E* or $77\frac{1}{2}$ from South Eastward, therefore I choose the *Azimuth* $77\frac{1}{2}$ *Z K*, therein I number *Jerusalem*s distance from London *Z I* 2300. miles or minutes, that is



38. 20. minutes. Now in the Triangle *Z P I*, I may find *P I* the complement of *Jerusalem*s Latitude 58. 05. minutes, and *Z P I* the difference of Longitude 46, which must be added to the Longitude of London to make the Longitude of *Jerusalem*.

CHAP. LXXIV.

The Latitudes and Distance of two Places given, to find the Rumb, and the difference of Longitude.

Count in the Meridian from P (the Pole) the complement of the Latitude of the first place, and thereto set Z the *Zenith*. Count also from P the complement of the Latitude of the second place, and lay your finger on the Parallel at which your number ends. Count also from Z the distance of the places in Degrees and Minutes, and note the *Almicantar* at which this number ends: where this *Almicantar* crosseth the aforesaid Parallel there is C of your Triangle; (but here marked I,) Look what *Azimuth* cutteth here, it sheweth the Rumb: and the Meridian that cutteth here, (if you count his distance from the *Limb*) shews the difference of the Longitude of the places. This is so plain from Chapter 69, 70, and 73. that it needeth no example. The same Scheme serveth these 4. Chapters,

The end of the Fourth Book.

The Fifth Book.

Shewing the way to resolve all
GNOMONICAL PROBLEMES,
 And to make all sorts of *SVNDYALS*,
 very easily by the
PLANISPHEAR.

CHAP. I: *The Preface.*

Of the kinds of Dyals.

Although *Gnomoniques* pertain to *Astronomy*, yet I think it not amiss, for the ease of the Reader in finding them, to place the *Gnomonical Problemes* in a distinct Book by themselves.

Suns Dyals may be reduced to two sorts.

Some shew the hour by the Altitude of the Sun, as Quadrants, Rings, Cylinders, &c. for the making whereof you must know the Suns Altitudes for every day, or at least every 10th day of the year, and for every hour of those dayes: which Altitudes you may find immediately upon this Planispher, as in a Table made to your hand, for any Latitude, by Book 3. 25. and so make them of any shape according to your mind.

The other sort shew the hour by the shadow of a *Gnomon*, or *Style*, Parallel to the Axis of the World: and of those I treat chiefly in this Book. Those be all Projections of the Sphear upon a plain which lies Parallel to some Horizon or other in the World. And if upon such a plain the Meridians onely be projected, they shall suffice to shew the hour, without projecting the other Circles, as the Ecliptique, the Equator with his Pa-

parallels of Declination, the Horizon with his *Almicantars* and *Azimuths*, which are sometimes drawn upon Dyals, more for ornament, then for necessity.

CHAP. II.

Theorems *premised*.

FOR the better understanding of the reason of Dyals, these *Theorems* would be known.

1. That every plain whereupon any Dial is drawn, is part of the plain of a great Circle of the Heaven: which Circle is an Horizon to some Country or other: that the Center of the Dial represents the Center of the Earth and World, and the *Gnomon* which casteth the shade representeth the Axis, and ought to point directly to the two Poles. And if upon the Center of the Dial you fasten a Label with Sights of equal Altitude, and keeping your eye in the line of the Sights turn this Label round, you shall thereby describe in the Heavens that great Circle wherein your Dial-plain lies, and see where it cuts our Horizon, and how much it is Elevated above it on one side, and depressed on the other.

2. That those Dial-plains *Geometrically* are not in the very plains of great Circles; for then they should have their Centers in the Center of the Earth, from which they are removed almost 4000. Miles: and in truth they lie in the plains of Circles Parallel to the said Horizons, but so near them, that *Optically* they seem to be the plains of those Horizons: because the Semidiameter of the Earth beareth so small proportion to the Suns distance, that the whole Earth may be taken for one point or Center, without any perceivable error.

3. That (as all great Circles of the Sphear: so) every Dial-plain hath his Axis, which is a straight line passing through the Center of the plain, and making right angles with it: and at the ends of the Axis be the two Poles of the plain, whereof that above our Horizon is called the Pole *Zenith*, and the other the Pole *Nadir* of the Dial.

4. That every Dial-plain hath two faces or sides: and look what respect or situation the North Pole of the World hath to the one side, the same hath the South Pole to the other, and these

these two sides will alwayes receive 24 hours ; so that what one side wanteth, the other side shall have; and the one is described in all things as the other.

5. That (as Horizons, so) Dyal-plains are with respect to the Equator divided into. 1. Parallel or Equinoctial, 2. Right, 3. Oblique.

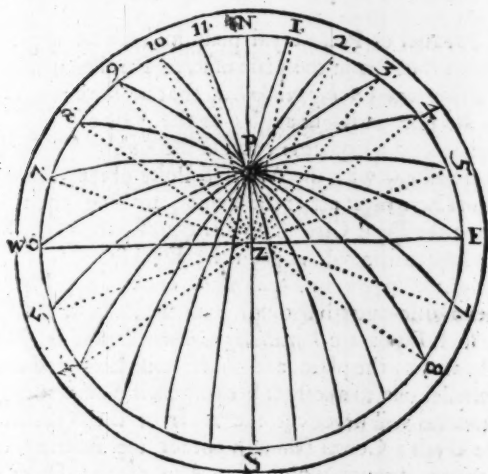
6. A Parallel or Polar Dyal-plain maketh no angles with the Equator : but lies in the plain of it, or Parallel to it. Such Dials are *Scioterica Orthognomonica*, that is, have the *Gnomon* erected on the plain at Right angles, as the Axis of the World is upon the plain of the Equator: because the Axis and Poles of the Dyal be here all one with the Axis and Poles of the World : and the hour lines here meet all at the Center, making equal angles, and dividing the Dyal Circle into 24. equal parts as the Meridians do the Equator, in whose plain the Dyal lies.

7. A right Horizon or Dyal-plain cutteth the Equator at right angles, and so cutteth through both the Poles of the World. Therefore such Dyals are *Parallelognomonical*: that is, have the *Gnomon* Parallel to the plain, and so the hour lines and the hour lines all Parallel one to another: because their plains though infinitely extended will never cut the Axis of the World. Yet have those Dyals a Center, (though not for the meeting of the hour lines) *viz.* through which the Axis of the Dyal Circle passeth, cutting the plain at right angles, and cutting also (near enough for the projecting of a Dyal) the Center of the World.

8. An Oblique Horizon or Dyal-plain cutteth the Equator at Oblique angles : such Dyals are *Scalenognomonical*: that is, have for their *Gnomon* the side of a Triangle whose angles vary according to the more or less Obliquity of the said Horizon: and the *Gnomon* shall alwayes make an angle with the plain of so many degrees as the Axis of the World maketh with the plain; or as either of the Poles of the World is Elevated above the plain.

9. Every Oblique Horizon is divided by the Meridians or Hour Circles of the Sphear into 24. unequal parts: which parts, are alwayes lesser as they are nearer to the Meridian of that Horizon or plain, and greater as they are further off : and on both sides the Meridian of the plain the hour Circles which are equally distant in Time, are also equally distant in Space : whence it is that the divisions of one Quadrant of your Dyal plain being known, the division of the whole Circle is likewise known.

10. The Hour-lines in an Oblique Dyal are the Sections of the plains of the Hour-circles of the Sphear with the Dial plain. And because the plains of great Circles do alwayes cut one ano-



ther in halves by Diameters, which are straight lines passing through the common Center, therefore lines drawn from the Center of the Dyal to the Intersections of the Hour-circles with the great Circle of the plain, shall be those very Sections, and the very Hour-lines of the Dyal.

11. Every Dyal-plane (being an Horizon to some place in the Earth, as was said *Theorem 1.*) hath his proper Meridian; which is the Meridian cutting through the Poles of the plain, and making Right angles with the plain. If the Poles of the Dyal-plane lie in the Meridian of our place; then is the Meridian of the plain all one with the Meridian of the place; and the *Gnomon* or *Style* shall stand erected upon the Noon-line, or line of 12 a clock, as in all direct Dyals: but if the plain decline, then shall the substylar or line wherein the *Gnomon* standeth, which is the Meridian of the plain, vary from the Noon-line, which is the Meridian of the place: and this variation shall be East if the Declination of

of the plain be West, and contrarily : because the visual lines by which the Sphear is projected on Dyal-plains, do all like the beams of a Burning-glass intersect or cross one another in a certain point of the *Gnomon* (to be assigned at pleasure, and called *Nodus*) and so do all place and depaint themselves on the Dyal-plain beyond the *Nodus* the contrary way.

12. Dyals are most aptly denominated from that part of the Sphear where their Poles lie: though some Authors have chosen to denominate them from the Circles in which their plains lie: as the Dyal-plain which lieth in the Equinoctial or Parallel to it, is called by many an Equinoctial plain: but I concur with those who would rather call it a Polar-plain, because the Poles thereof are in the Poles of the World.

CHAP. III.

*How to draw an Horizontal or Vertical line, upon
any plain.*

BECAUSE in the Delineation of most Dyals the Horizontal or the Vertical line of the plain must first be drawn, before you can place the hour-lines; I will shew you first how to draw either of them. Know this first, that they cross one another at Right angles in the Center of the Dyal: and therefore if you can draw either of them, you may draw the other also. Also in upright plains, as are Walls, a Quadrant or a Square with a Plumbet applied to the Wall, will shew you how to draw both of them very easily. Or if you hang a Plumb-line quiet before the Wall when the Sun shineth, the shadow of it shall be a Vertical line at any time.

But if the plain incline or recline, you shall set to it a Square with a Plumbet, and thereby first draw the Horizontal line; for when the Plumbet (which must play in an hole) hangs Parallel to one side of the Square, a line drawn by the other shall be Horizontal: that drawn, you shall lay your Square flat on the plain, and draw the Vertical from any point of the Horizontal at Right angles by your Square.

Another way is this. Hang your Planisphere by the handle with his Plumbline, so that the Plumbline fall upon one of the Diameters; then setting your *Label* and Sights to the other Di-

meter, look through the Sights, and mark where the visuall line cuts the plain neer to one side, and there make a prick, then direct your Sights to the other side of the plain, and make another prick, (your *Label* and Plumblin being still at Right angles as before) by these two pricks draw a line, and it shall be an Horizontal line. And note, that all lines Parallel to an Horizontal line be Horizontal: and all lines Parallel to a Vertical line be also Vertical.

CHAP. IV.

How to make the Polar Dyal, and how to place it.

THe plain of the Polar Dyal lieth in the Equinoctial: where the 12 cheife Meridians or Hour-circles divide both the Equinoctial and this plain into 24 equal parts. The *Gnomon* stands upon the Center at Right angles with the plain. You may learn to make him only by the 6. *Theorem* of the second Chapter.

Take your Planispher in the Equinoctial Projection, and there is your Dyal ready made on the *Limb*, and the Hours already marked. Erect now a wyer or thred Perpendicular upon the Center, or hold a Square to the Center, so that his top be equally distant from all the parts of the Circle: and there is your *Gnomon* placed.

To place this Dyal do thus. Having (by Book 4.3.) found a Meridian line, if you cross it with another line, that shall be an East or West line. Have also in a readines a square board upon which you may fasten your Planispher or Dyal-plate with pins, screws, or wax, so that the Noon-line may be Parallel to two sides of the board, and the East-line to the other two: then set the North side of the board in the East line, even now found, and raise the South side by a Quadrant to the height of the Equinoctial; and so may you place your Dyal in any Window if it be made upon a loose round plate; but if the plate be square, you need not the board to place it.

Note that both faces of this Dyal must be divided, and the *Gnomon* must appear on both sides, like the stick in a Purge (or whirligig) which Children use: otherwise you must turn him upside down, as oft as the Sun passeth the Equinoctial.

CHAP. V.

How to make the South Equinoctial Dial, or Parallelognomonical Dial direct.

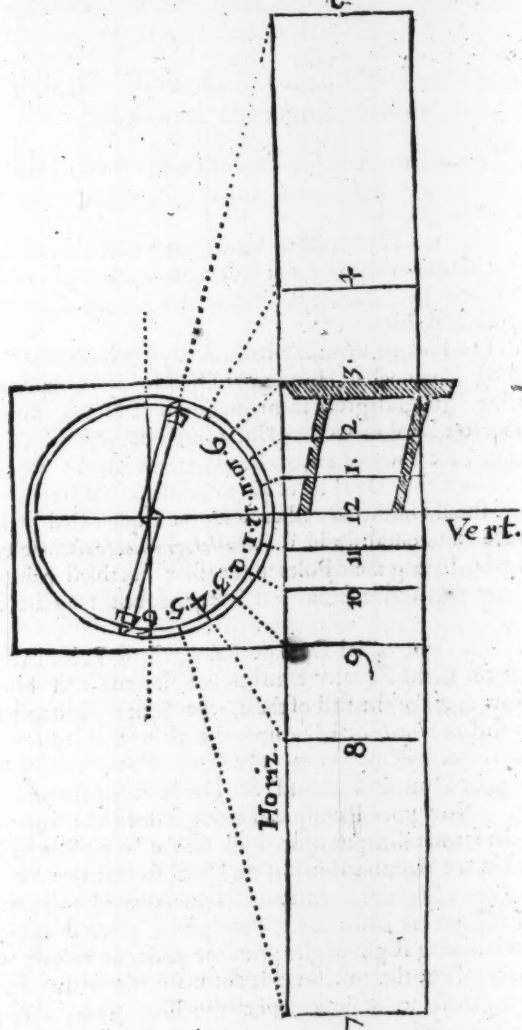
THe Equinoctial Dial we call that which hath his Poles in the Equinoctial Circle: of which there be three kinds,

1. The direct or South Equinoctial Dial, which fa-
ceth the Meridian directly, not looking from him to one side more
then to the other, having his Poles in the Intersections of the E-
quinoctial and Meridian.

2. The East or West Equinoctial Dial, which may also be
called the Equinoctial Horizontal Dial: for an Horizontal Dial
declining just 90 degrees from the South or North, becomes an
Equinoctial Dial, as well as Horizontal: because there his Poles
light upon the Intersection of the Horizon with the Equinoctial.
And though this Dial be of kin to both, yet his *Gnomon* shews
that he should be sorted rather with the Equinoctial Dials then
with the Horizontal: for he is *Parallelognomonical*: these two sorts
be regular, having their Poles in the four notablest points of the
Equator: the third is somewhat Irregular, but may be brought
to Rule.

3. The Equinoctial Dial declining, whose Poles happen any-
where else in the Equator between the Horizon and Meridian.

Now to make the first of these, the South Equinoctial Dial,
draw first an Horizontal-line upon the plain, and cross it with a
Vertical-line, by Chapter 3. The Intersection of these is the Cen-
ter of your Dial, and would be chosen about the middle of the
plain. Now your Planisphear being fastned to a square board,
as in the former Chapter, you shall set the North side of the said
board in the Horizontal-line of the plain, so that the Axis or East
line of your Planisphear may be Parallel thereto, and the Noon-
line (or Equator line of the *Mater*) may point directly to the
Center, making Right angles with the plain, or at least with the
Horizontal line thereof: (for it is not material whether the board
be upright, slope, or lie flat upon the Dial plain) then placing
your Sights first in the Noon line, they shall point to the Center
for the point of 12. thence remove your *Label* to 1. of the
clock



clock in the *Limb*, and they shall point out in the Horizontal line of the plain, the point of Interfection for one a clock, where you shall make a prick: In like manner remove your *Label* to 1, 2, 3, 4, and 5. in order, making pricks in like manner When you remove your *Label* to the *Axtree* line for 6. you shall find that the line of the Sights maketh no Interfection with the plain, but runneth Parallel to it; because the Sun is then in the Horizon of this Dyal, where he projects the shadows of all upright things infinite. And as you found the points for the hours afternoon, so may you by like reason find the points for the 5. morning hours, and their quarters also, if you please: which had, if by these points found you draw lines Parallel to the Vertical line of the plain (which is here the Meridian of the plain, and of the place) they shall be the true hour-lines. And the *Gnomons* edge must stand over the Meridian, and Parallel to it, at the same distance that the *Axtree* line of your Planisphear was situate in projecting the hour points. If you cannot fix your Planisphear on a board, as above laid, or if your plain require a *Gnomon* of a greater or lesser height, you may upon any board presently draw so much of your Planisphear as serves for this purpose. Or to say more briefly, Do but make the height of your *Gnomon Radius*, and the *Tangents* of 15, 30, 45, 60, 75. shall give the distances of the hour points in the Horizontal line, on both sides, from the Center of the Dyal, as may appear in the Figure.

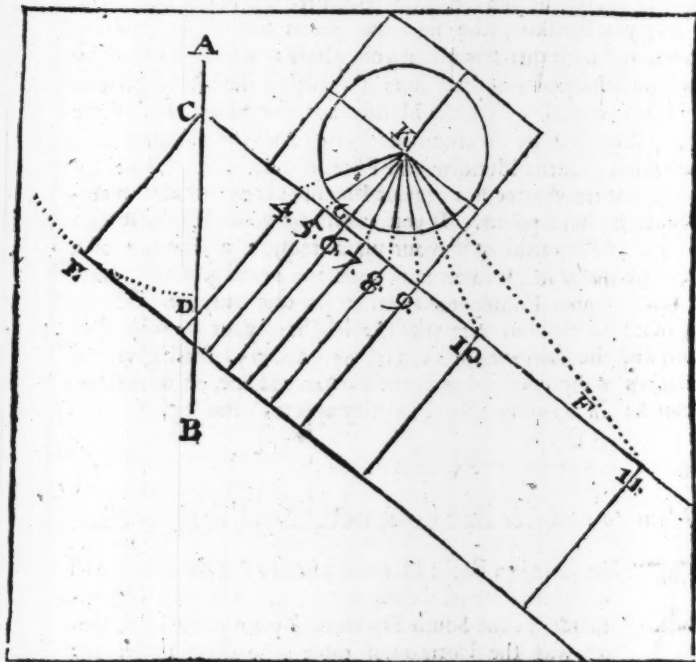
CHAP. VI.

How to make the East Equinoctial Dyal, or the West.

THis plain is a Right Horizon of those People who dwell under the Equator, distant from us 90 degrees of Longitude; as the South Equinoctial-plain of the last Chapter was the Horizon of those who dwell under the Equator, in the same Longitude with us. Therefore these Dyals are in all points alike: onely the Substylar-line which in the South Equinoctial Dyal is 12. in this East Equinoctial Dyal is but 6. in the Morning for our Country, because of the difference of Longitude.

To protract this on the wall or plain, first draw a Perpendicular or Vertical line by Chapter 3. as A B. Pitch one foot of your

your Compasses in any convenient point thereof (as C) and with the other foot draw a blind arch from some lower point of the Perpendicular South-ward (as D E). In this arch number the Elevation of the South Pole above this Perpendicular (that is, the Complement of your Latitude, being with us 37. 45 minutes) and from that degree to the Center of the said arch draw the line E C, which is the very Axis of the World, pointing to both the



Poles; Cross this Axis at Right angles with the line C F, and that shall be a Diameter of the Equator and the Contingent-line, as they call it. Now choose a fit point in this Contingent for the Substyle or 6. a clock point, as at G, and thereto by the square board mentioned in the former Chapter, set *Oriens*, or *Occidens*, of your Planisphaer; and so the *Label* set to the several hours in the

the *Limb* of the Planisphear shall shew the hour-points in the Contingent line: onely for 12. the line of the Sights will not intersect the plain at all, and therefore here is no Noon-line, as there was no 6. a clock-line in the South Equinoctial Dyal: but so soon as the Sun leaving the plain makes the shadow of the *Gnomon* infinite, then it is Noon.

Lastly, draw a line Parallel to the Contingent line at such distance as the plain will afford, as the line E I, and to this you shall protract your hour lines, drawing them from every point of the Contingent to this; so that they make Right angles with the Contingent and with this Parallel, even as the rounds of a Ladder do with the sides, but that the distance of the rounds of a Ladder are equal, and these distances be unequal. The *Gnomon* must be set like a Bridge Perpendicularly over the 6. a clock hour-line, the edge that casteth shadow being Parallel to it, and of such height as the line K G of your Planisphear, or so that if the *Gnomon* fall, his edge may lie in the line of 3. or of 9. of the clock. This also may be made speedily by help of the *Tangents*, as the South Equinoctial Dyal.

For the West Equinoctial Dyal, it is made like the East in all points; onely it shews but the after Noon hours, as the East shews but those of the fore noon. When you have drawn on paper the East Dyal, and set it by guess in its Situation, go on the West side of it, and you may see through the paper the picture of the West Dyal, and so will the back side of the West Dyal shew you the true picture of the East.

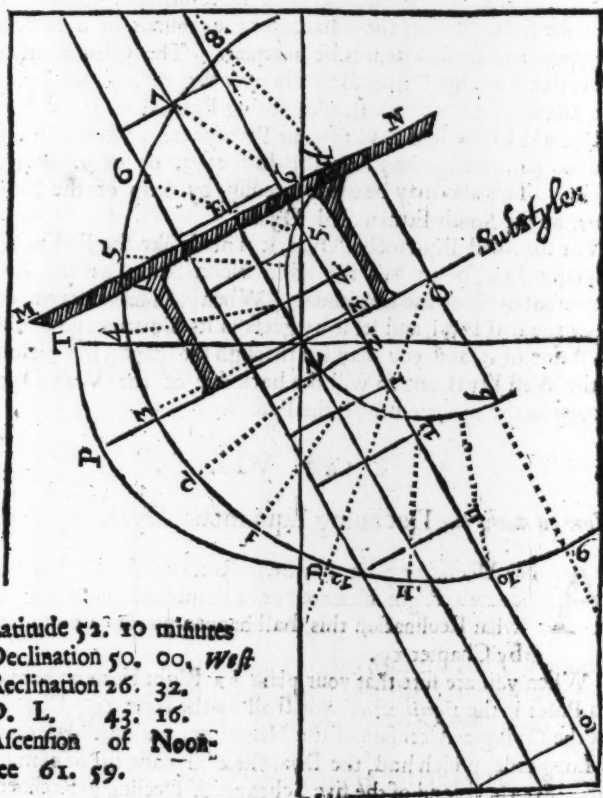
CHAP. VII.

How to make the Declining Equinoctial Dyal.

ANy Declining plain may be so Reclined that he shall become a Right Horizon or Equinoctial plain, and at what Reclination this shall happen you may easily find by Chapter 19.

When you are sure that your plain is a Right Horizon, having his Poles in the *Equinoctial*, you shall by the same 19th Chapter get the Oblique Ascension of the Noon-line, and the difference of Longitude; which had, the Dyal shall be made in this manner. See the second of the five Schemes of Declining-Recliners,

Chapter 20. Draw upon your plain (by Chapter 3.) an Horizontal line *D d* (answering to *D d* in the said Scheam) therein take a point at pleasure, as the point *Z*, (answering to *Z* in the said Scheam) and thereupon draw above the Horizontal line Westward, if the Declination be West (as the said Scheam shall direct you) the Quadrant of the plain *D P T*; (answering *D Pro T* of the said Scheam) herein number from *D* the arch *D P*, which is the Oblique Ascension of the Noon line, and draw *Z P* for the Axis and common Section of all the Meridians. It appeareth now



Latitude 52. 10 minutes
Declination 50. 00. West
Reclination 26. 32.
D. L. 43. 16.
Ascension of Noon
lice 61. 59.

that no Dyal can be drawn upon the very plain of a Meridian, for there all the hour lines will be represented by one line, which is the Axis of the World; therefore you must draw such Dyals on a Parallel plain, as you did the two former after this manner.

Set the line M E N for the Axis of the World or *Gnomon*, and prop him up over the line P Z with two props of equal height, and Perpendicular to the plain, and make the point E (which standeth Perpendicularly over Z) the Center of the World; then from this Axis or *Gnomon* mounted in the Air, shall the hour-lines be projected distinctly, and all of them shall be Parallel to the Axis and one to another, as it hapneth in all sorts of Equinoctial Dyals. The line Z P shall remain now onely the Meridian of the plain or *Substyle*. And to find the hour-lines you shall do thus.

Draw through Z an Equinoctial or Contingent line E Z, making Right angles with the Axis M E N or Z P, then setting Z O equal to Z E, draw upon the Center O (with an extension of the Compasses,) the arch of the Equinoctial *b Z d*, or the Parallel arch passing by D. Then number in this arch from the *Substyle* (Westward if your plain decline West, or Eastward if it decline East) the difference of Longitude, and where it ends there is the point of Noon in this arch: from that point begin to divide the said arch by fiftens of degrees, or 24th parts of the whole Circle. And remember, that when you come to 90 degrees from the *Substyle*, you need divide no further, for the Sun is no longer upon this plain. Also you may leave out those hours at which the Sun is alwayes under our Horizon, as the hours from 8. at Night, to 4 in the Morning: then lay a Ruler from the Center O to every one of these divisions of the Circle, and where the Ruler cuts the Contingent, there make points for the hours respectively, and through these points you may draw the hour-lines Parallel to the *Substyle*, of what length you please; and mark them from the Noon line Eastward 1, 2, 3. &c. because the Suns Diurnal course is Westward, and the course of the shadow is contrary.

He that will may make use of his Planispher for dividing the hours, as was taught Chapter 4, and 5. or use a *Quadrant*, or a *Scale of Chords*, or the Tables of *Tangents* with a *Sector*, or a *Scale* of equal parts. But it needs not.

Note that this Dyal may compare with the hardest: however

Mr *Blagrove* and other Dyalists have omitted it, as seeming easy: and here *Wittekindus*, (to whom all later Dyalists are much beholden) and after him *Fale* were mistaken, using the Declination of the plain, where they should have used the difference of Longitude in the making of this Dyal.

CHAP. VIII.

Of the kinds of Oblique Dyals.

WHat an Oblique Dyal is, and why it is so called, hath been shewed Chapter 2. They be $\left\{ \begin{array}{l} \text{Regular.} \\ \text{Irregular.} \end{array} \right.$

The Regular lie in some notable Circle of the Sphear; as, 1. The Vertical Dyal, whose plain lieth in the Horizon: for which cause many call it the Horizontal Dyal. 2. The South and North Horizontal Dyal, whose plain lies in the East *Azimuth*: and it is commonly called the South or North Erect Direct Dyal. As for the East and West Dyals, they belong to another place, as was said Chapter 5.

The *Irregular* are such as lie Oblique to the Horizon, as Reclining or Inclining Dyals; or lie Oblique to the Meridian, as Decliners: or else Oblique to both, as Recliners or Incliners Declining; which are esteemed the hardest of all, because of their double Irregularity, though by the Planisphaer they are made almost as easily as the rest.

The Declination of a plain is the *Azimuthal* distance of his Poles from the Meridian of the Place, East or West.

The Reclination is the distance of his Poles from the *Zenith* and *Nadir* of your Place. Inclination is the nearest distance of the Poles of the plain from your Horizon. And whatsoever the Reclination of the upper face of a plain is, the Inclination of the lower face is the Complement thereof.

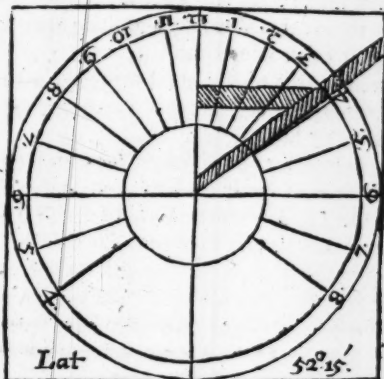
CHAP. IX.

How to make the Vertical Dyal.

IN the Meridional Projection the *Finitor* being set to the Latitude of your Place, you shall see the *Limb* which is your Me-

Meridian, and the Axtree-line which is the sixt hour-circle, dividing the *Finitor* into 4 Quadrants; and the rest of the Meridians dividing every Quadrant alike. Mark now at what degree numbred from the *Limb*, every hour-circle (that is, every 15th Meridian being a ragged or blacker line) cutteth the *Finitor*; at the same distance shall the same hour-circle cut the *Limb* of your Dyal in the plain.

Example. To make a Vertical Dyal for our Latitude 52 degrees 15 minutes. I set the *Finitor* to this Latitude, and because I see the Meridian and Axtree divide the *Finitor* into 4 equal Quadrants, therefore I open my Compasses to the Semidiameter of my Planisphear, or of any other Circle



which I have at hand already divided, and with that measure I draw a Circle, and cross it square with two Diameters dividing it into four equal parts: of which Diameters I appoint one to be the Noon-line, and at the North end thereof I write 12. the other Diameter then is the East line, and at both ends thereof I write 6. Then I count in my Planisphear how many degrees from the Meridian or Noon line every other Circle cutteth, and I find that the first cutteth 11. 58 minutes, wherefore I take with my Compasses from off the *Limb* of my Planisphear, or other Circle used for this purpose, the space of 11. 58 minutes, and set it in the Circle of my Dyal from 12. both wayes, for the hours of 1. and 11. and because I find the second hour Circle cutting the *Finitor* at 24. 32 minutes, therefore I take in like manner the Chord of so many degrees from the *Limb* of my Planisphear, and set it also in the Circle of my Dyal both wayes from 12. for the hours of 2. and 10. And when you have done the like for the 3. 4. and 5. hours, you shall draw lines from those

those points to the Center, and set to those lines from the North Eastward 1, 2, 3, 4, 5. and Westward 11, 10, 9, 8, 7. And because the Sun in Summer is above our Horizon more then 2 hours before and after 6. (for I see the 7th and 8th hour Circles intersecting the *Tropique* above the *Finitor*) and because hour lines equally distant from the Meridian or Axtree cut like degrees of the Horizon (as my Planispher here shews me) and so shall make equal angles at the Center; therefore laying my Ruler to 7 in the Morning I prolong that line beyond the Center to the other side of the Circle for 7 at Night: likewise by the prolongation of 8 in the Morning, I make 8 at Night, and by the prolongation of 4 and 5 of the after Noon, I make 4 and 5 of the Morning hours.

Lastly, for the *Gnomon*, set your Compasses to the Chord of the arch of the Poles Elevation in the *Limb*: that is, measure in the *Limb* from the Pole to the *Finitor*, and setting that distance in the Circle of your Dyal from 12, either way, make a point, through which if you draw a deble line from the Center, you have between this line and the line of 12. the angle of your *Gnomon*, by which when you have shaped him, you must set him upright over the 12 a clock line, with the point of the said angle at the Center, and all is done.

CHAP. X.

How to make the South and North Horizontal Dyal.

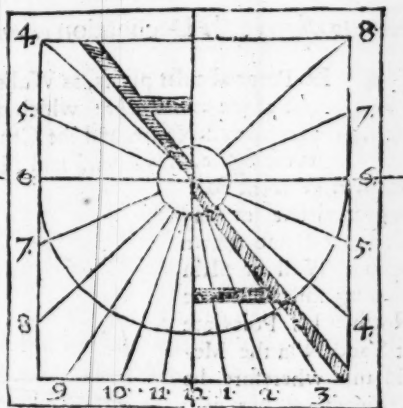
THis is usually called the Erect Direct Dyal, and belongs to an upright Wall looking full North or South: and the plain of it lies in the East *Azimuth*, which on the Planispher in the Meridional Projection is represented by the Axis of the *Reet*.

The *Finitor* set to the Latitude, as in the former Chapter, mark where the hour Circles cut the Axis of the *Reet*, which is the proper Horizon of this Dyal; you shall find the first cutteth 9. 20 minutes from the Meridian, the second 19. 30 minutes, the third 31. 30 minutes, the fourth 46. 45 minutes, the fifth 66. 24 minutes; the sixt 90. And you shall see the North Pole depressed under this plain, as much as is the Complement of our Latitude, and the South Pole as much Elevated above it.

1. Where-

1. Wherefore for the South Dyal, draw an Horizontal line about the top of your Dyal plain, which shall be the hour of Sixes, from the midst whereof let fall a Perpendicular, which shall be both the Vertical and the Meridian, both of the Place, and of the Plain. wherein the *Gnomon* must stand Elevated 37.45 . minutes, or the Complement of your Latitude toward the South Pole.

From the Center (which is the point from whence the Perpendicular falls.) draw a Semi-circle beneath the Horizontal line, of equal Semi-diameter with that of your Planisphere: or of any other Circle which you have divided; and in this Semi-circle let off on both sides from the Perpendicular or Meridian line the distances of the hours before found, making pricks in the Semi-circle, and thereto drawing lines from the Center, and setting figures, after the same manner as you did in the former Chapter; and your Dyal is done. This Dyal shews the Hours from 6 in the Morning to 6 at Night; the other Hours before and after 6 belong to the North face of this Dyal.



Another way. Because the Almicantars may oft obscure the Intersections of the Hour Circles with the Axis, you may avoid that inconvenience, if you reduce this Dyal to a Vertical Dyal.

For the South Horizontal Dyal being the very Vertical Dyal of those People that live 90 degrees Southward from us. that is, in South Latitude 37.45 minutes, if you set the *Finsior* to the Latitude 37.45 minutes, you shall see the sections of the Hour Circles with the *Finsior* more apparently, and thereby make your Dyal,

2. For the North face, Imagine you had for your *Gnomon* a wyre thrust aslope through the Center of the plain from the South side Northward, and you will presently conceive that in the North Dyal the Horizontal or 6 a clock line will be lowest, and that the *Gnomon* will turn upwards toward the North Pole, as much as he turned downwards on the other side: and that all the hours save 4, 5, and 6. in the Morning, and 6, 7, and 8. at Night may be left out in our Latitude; because the Sun shineth no longer upon it: and those hour-distances you may find, and set off from the 12 a clock line, or from the 6 a clock line, as you did the hours of like distance in the South face.

Another general and pleasant way to delineate the opposite face of any Dyal, see hereafter in the end of the 12th Chapter.

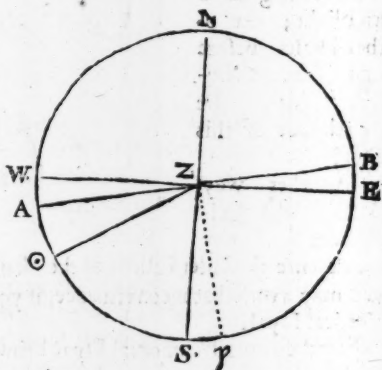
CHAP. XI.

How to Observe the Declination of any Declining Plain.

ALL Perpendicular plains, as Walls, lie in the plains of one of the *Azimuths*: which plains alwayes cut both *Zenith* and *Nadir*, and the Center of the Earth. As in the figure. *Z* is *Zenith* and *Nadir*: *E S W N* Ho-

rizon, *E W* is the Base or ground-line, or any Horizontal line drawn upon a Wall or plain looking full South or North; his Poles are at *S* and *N* in the Meridian, wherefore he declineth not, but lieth in the East *Azimuth* *E W*.

A B is a Wall or plain declining East by the arch *S p*, to which *E B* or *W A* are equal, for so much as the Wall bendeth from the East *Azimuth*, so much doth his Pole at *p* decline or bend from the Meridian.



1. Now to find how much any plain declineth, and so in what *Azimuth* he lies, one good way is this: when the Sun begins to inlighten the Wall, or when he leaves it, then is the Sun in the same *Azimuth* with the Wall; take at that instant his *Altitude*, and thereby get his *Azimuth* (according to Book 4. 27.) and that is the *Azimuth* of the Wall.

2. Another way. First draw upon the Wall an Horizontal line, by Chapter 3. then your Planispher being fastned to a Square board (as in Chapter 4.) set one side of the board to that Horizontal line or Parallel to it, and fix there your board and Planispher level, by the help of a Square set under him like a bracket, then place your *Label* and Sights in one of the *Diameters* of your Planispher, and mark when the Sun comes into the line of the *Label*, casting the shadow of one Sight upon the other, if the *Label* be then in the Diameter which is Parallel to the Wall, then is the Sun at that time in the *Azimuth* of the Wall: if the *Label* be in the other Diameter which is Perpendicular to the Wall, then the Sun coming to it is in the *Azimuth* of the Pole of the plain.

Now having the hour, or the *Altitude* of the Sun get his *Azimuth* (by 4. 27.) the same is the *Azimuth* of the Wall or plain, if the *Label* were Parallel to the Wall; or the same is the *Azimuth* of the Pole of the plain (that is the very *Declination*) if the *Label* stood Perpendicular to the Wall.

3. Another way. If you have not time to watch till the Sun come into the *Azimuth* of the Wall or the Vertical of it, which cutteth the Pole thereof, then get the Suns *Azimuth* by the said Book 4. 27. when you can, and at the same time Observe by your *Label* the Suns Horizontal distance from the Pole of the plain, and by comparing these together you may easily gather the *Declination* of the Wall: as in Example.

I observed the Sun to be gone West from the Pole of the plain 70 degrees, and by the *Altitude* of the Sun then taken, I found his *Azimuth* 60 degrees: here I reason thus, The Sun is gone from the Pole and Vertical of the Wall 70 degrees, and from the Meridian but 60 degrees. therefore the Meridian lies between the Pole of the plain and the Sun, and because $\odot p$ is 70. and $\odot S$ 60. therefore $S p$ the *Declination* of the plain, is 10 degrees the difference of 70. and 60. and the *Declination* is East, for the Sun is neerer to the Meridian then to the Vertical of

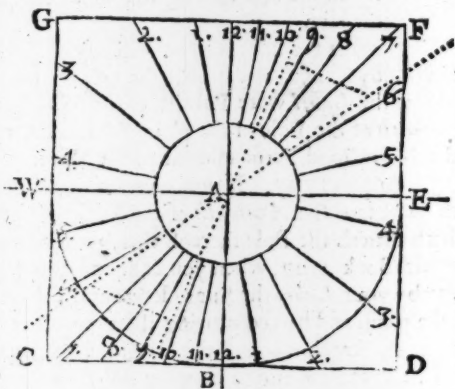
the plain: and thus if you draw a rude Scheme of your Case, you may soon reason out the Declination, better then do it blind-fold by the rules commonly given,

And by these two last wayes you may take the Declination, not only of upright plains, but of Recliners also, for which the first way will not serve,

CHAP. XII.

How to make a Declining Horizontal Dyal.

Here three things are required. For besides the distances of the several hours from 12, and the Elevation of the *Gnomon*, which are requisite to the making of all Direct and Regular Dyals, we must here know also the Declination of the *Gnomon*, which some call the distance of the Substyle from the Meridian, or the distance of the Meridian of the plain from the Meridian of the Place. For in all Dyals the Noon-line in the Meridian of your Place, projected on the Dyal, and in all Horizontal or Mural Dyals, not Reclining or Inclining, the Noon-line is a Perpendicular cutting the Center of the Dyal, how much soever they Decline.



But Declining Dyals which look awry from our Meridian, have a Meridian of their own, which is called the Meridian of the plain, and the Substyle. (because the *Style* or *Gnomon* stands upon it) and is indeed the Meridian of that Place, where this Declining Dyal would be a Vertical Dyal, and where the Substyle would

would be the Noon-line : and to this Substyle the hours of the plain are alwayes so conformed, that the nearer they be to the Substyle the narrower are the hour spaces, and contrarily : because the Meridians do so cut every oblique Horizon, that is, thickest near the Meridian of the place: and this Declining Dyal (being a stranger with us) followeth the fashion of his own COUNTRY, and so hath his narrowest hour spaces near his own Meridian, rather then ours. Now as that is the Meridian of our place which cutteth our Horizon at Right angles, passing through his Poles *Zenith* and *Nadir*, so the Meridian of any plain is that which cutteth the plain at Right angles, and passeth through his Poles.

You may find all these requisites in the Meridional Projection, not only for one, but for all Declinations, lying as in a Table before you, with admirable ease and delight; for there is no Declining Wall or Horizontal plain, but we have an *Azimuth* in the *Reet* which shall picture him : and look how the Meridians divide these *Azimuths*, so do they divide the Horizons or Circles of the Declining plains. The Pole of any *Azimuth* is found in the *Finitor* 90 degrees distant from him; the Meridian that cuts the Pole of the *Azimuth*, cuts also the *Azimuth*, and the plain thereby represented at Right angles, and is the Meridian of the plain or Substylar, (Chapter 2. Theorem 11.) and the degrees of that Meridian between the plain and the next Pole of the World are the Elevation of the Pole above the plain : and so the Elevation of the *Gnomon* or *Style*, and the arch of the plain comprehended between this Meridian of the plain and the *Limb*, is the Declination of the *Gnomon*, or distance of the Substyle from the Meridian, or distance of the Meridian of the plain from the Meridian of the Place. What would you more ?

Example. If a Wall Decline East 30 degrees. I say, because the face of the Wall looketh 30 degrees from the South Eastward, therefore the plain, which lieth 90 degrees from his Pole, is in the 30th *Azimuth* from the East Northward : therefore I go to the 30th *Azimuth* from the East line or Axis, counted either way, and take that *Azimuth* and his Match (which is equally distant from the Axis) for the very picture of my Declining plain.

Then seeking the Substyle or Meridian of the plain. I say, the Pole of the plain is in the *Finitor* at the 30th *Azimuth* from *Meridies*

ridies in the *Limb*, (because the plain it self is the 30th *Aximuth* beyond the *Axis*) the Meridian that cuts this Pole is the 36¹/₄ (exactly 36. 8 minutes,) the number whereof shewes me the difference of Longitude between our Country and the Country of this Dyal. This 36¹/₄ Meridian, being the Meridian of the plain, I follow toward the Pole, and find him cutting both the arches of my plain on both sides the *Axis*: but I regard the cutting only in that arch which is nearest to the Pole, because there the angle looks more like a Right angle, and there is the nearest distance of the Pole from the plain, and there I see the hour spaces least: from that Intersection therefore, I reckon in the same Meridian to the Pole 32 degrees and perhaps a minute more, (you may find it by Calculation,) this is the Elevation of the Pole above the plain, and of the *Gnomon* likewise: also from the same Intersection I reckon in the plain to the *Limb* or Meridian 21. degrees 10. minutes, the distance of the Meridian of the plain from the Meridian of the Place: the same is the Declination of the *Gnomon*, or of his Substyle.

Then for the hours, I begin at the *Zenith* of the *Reet*, where is our Meridian, and numbring first toward the Substyle, I seek at what number of degrees from the *Zenith* the hour Circles cut my plain, and I find as followeth,

deg. min.

11.-- 9. 35

10.-- 17. 54

9.-- 25. 54

8.-- 34. 22

7.-- 44. 17

6.-- 52. 10

5.-- 75. 4

Then in the other arch of
the plain I have the afternoon
hours, thus.

deg. min.

1-- 12. 10

2-- 28. 59

3-- 52. 26

4-- 80. 17

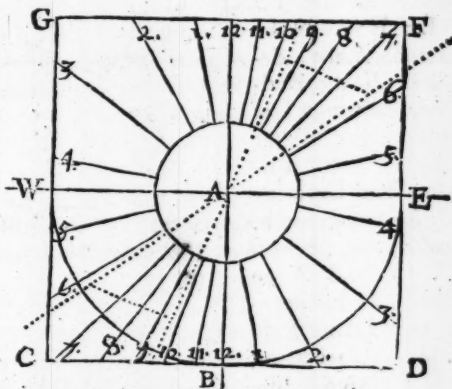
And further I cannot go, because I see the next hour is above 90 from the Substyle; therefore my Dyal receives him not on this side, but on the North side there is use of him.

Now to draw the Dyal, I consider that because the plain declines East therefore the *Gnomon* shall decline West: for the Dyal being such a projection of the Sphear wherein all the Visual lines cross in the *Nodus* of the *Gnomon*, and thence disperse themselves again toward the plain, therefore that which is East in the Sphear will be expressed West on the plain, and contrarily, (as

was

was shewed Chapter 2. Theorem 11.) Also I consider that howsoever the plain be turned East or West, the *Gnomon's* place is fixed, because it is a part of the Axis of the World, or a line Parallel to it. Now therefore if I turn a South Dyal, and make him Decline East, and hold the *Gnomon* unmoveable; the West side of the Dyal will approach nearer to the *Gnomon*, as reason and sense will tell me: likewise the hours which are found on the same side of the Meridian or Noon-line with the Substyle must be set the same way with it from the Noon-line in the Dyal. Therefore having drawn an Horizontal line E W on the Wall, from the Center taken at A, I let fall the Perpendicular A B for the Noon-line, then upon the Center A, I draw a blind Semi-circle with the Semi-diameter of my Planisphaer, or of some Quadrant, as E B W and therein I prick down the Substyle and the hours, after the manner used in the 10th Chapter.

And if you would draw the North Dyal of this plain, do but prolong those hour lines, and the Substyle upwards beyond the Center, and you have the North Dyal, above the Horizontal line E W, as the South Dyal below it; and note, that because in our Latitude the



Sun sets soon after 8 in Summer, therefore the 3 hours next before and after mid-night may be left out in this Dyal, and in all others which must serve in our Latitude.

This is the most ready way to delineate the opposite face of any Dyal. See another way to make this Declining Horizontal Dyal, Chapter 21.

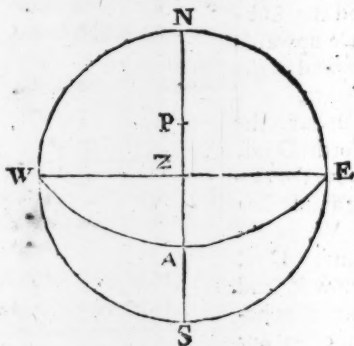
CHAP. XIII.

How to Observe the Reclination or Inclination of any Plain.

WHat Reclination and Inclination are, hath been shewed Chapter 8.

All Reclining and Inclining plains have their Bases or Horizontal Diameters lying in the Horizontal Diameter of some *Azimuth*: but the top or *Nonagesimus gradus* of the plain from the Horizon leaneth back from the *Zenith* of your Place, in the Vertical of the plain (which is the *Azimuth* cutting the plain at Right angles) so much as the Reclination hapneth to be; and the Pole of the plain, on that side the plain inclines to, is sunk as much below the Horizon as the *Nonagesimus gradus* of the plain is sunk below the *Zenith*, and the opposite Pole is mounted as much,

Let E S W N be Horizon, Z the *Zenith*. E W the Horizontal Diameter of the plain, and of the East *Azimuth* E A W a plain not Declining but Reclining Southward from the *Zenith* by the arch Z A 50 degrees. and his opposite face Inclining to the Horizon according to the arch A S 40 degrees, the Pole of the



Reclining face is at P in the Meridian (which here is also Vertical of the plain) and is Elevated 50 degrees in the arch N P equal to the arch of Reclination Z A: and the Pole of the Inclining face is depressed as much on the other side under the Horizon.

To find the quantity of the Reclination you shall draw a Vertical line on the plain, by Chapter 3. and thereto apply a long Ruler which

which may over-shoot the plain either above or below : to that Ruler apply any Semidiameter of your Planisphear, or of any Quadrant; and the degrees between that Semidiameter and the Plumb-line shall be the degrees of Reclination.

Or stick up in the Vertical line two pins of equal height, and Perpendicular, and placing your self either above or below the plain, as you find most easy, direct the Sights of your Planisphear or Quadrant to the heads of the two pins being in a right line with your ey; and the Plumbet shall shew the Reclination on one side the Quadrant, and the Inclination (which is always Complement thereof) on the other.

CHAP. XIV.

How to make a South and North Reclining Dyal.

THe Base or Horizontal line of such a Dyal lieth in the East *Azimuth*, and his Pole in the Meridian; as you may see in the plain of the former Chapter. In the Meridional Projection having set the *Finitor* to the Latitude, count from the *Zenith* the degrees of Reclination Northward or Southward as you observed it to be, and remove the *Zenith* so many degrees the same way, then shall you see presently which Pole is Elevated above the *Zenith* line, (for that is the picture of your plain) and how much : to which Elevation you shall make your Dyal by the tenth Chapter, remembring to turn the *Gnomon* upwards or downwards as the North or South Pole is Elevated above the face of your plain.

Example. The plain of the former Chapter was a North plain Reclining Southward 50 degrees, that is, almost to the Equinoctial : when the *Finitor* is at our Latitude the *Zenith* is distant from the North Pole the Complement thereof 37. 45. toward the South. Now I must put the *Zenith* yet 50 degrees more Southward, because my plain Reclines so much that way, and I see that then the North Pole is Elevated 87. 45. minutes, and I see upon the *Zenith* line or *Axis* of the *Rees* how the hour Circles cut my plain almost in equal spaces: if this plain had Reclined but 2. 15 minutes further, he had fallen into the plain of the Equinoctial, and so the Dyal would have been a Polar Dyal, and all the hours would have had equal spaces, and the

Gnomon would have stood Perpendicular, which are the properties of a Polar Dyal, as hath been shewed Chapter 4.

For the opposite face of this Dyal, the general rule given Chapter 12. may suffice.

CHAP. XV.

How to make an East or West Reclining Dyal.

AS it hath been shewed Chapter 14. that the base or Horizontal line of a South Recliner lieth alwayes in the East *Azimuth*, so the base of an East Recliner lieth alwayes in the Meridian of the Place. And as all Declining plains lie in some *Azimuth*, and cross one another in the *Zenith* and *Nadir*, by Chapter 12. so these Reclining plains lie in some Circle of Position, and cross one another in the North and South points of the Horizon: which being considered, those East Recliners shall be made as easily as the Decliners Chapter 12.

For these East Recliners be in very deed South Decliners to those that live 90 degrees from us Northward or Southward; and have one of the Poles Elevated as much as the Complement of our Latitude: for the Perpendicular or Plumb-line of those People is Parallel to the Horizontal Diameter of our Meridian.

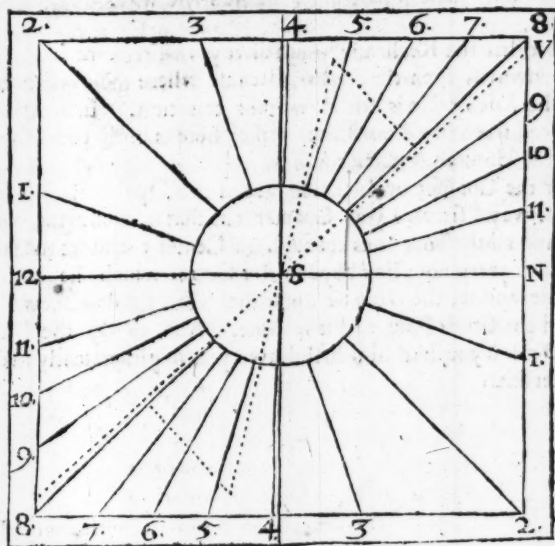
In the Meridional Projection, set the *Zenith* line to the Latitude, and then are the *Azimuths* Circles of Position, and are also those very East or West Reclining plains, and the *Zenith* line is the base or Horizontal line to them all, and to the Meridian likewise; Take any of these *Azimuths*, and see how the Meridians of the *Mater* divide him, so shall the Dyal-plain represented by it be divided also. The working is very like that of Chapter 12. Compare the one with the other where you doubt.

Example. I have an East plain Reclining 45 degrees, to which I would make a Dyal. I set the *Zenith* line to the Latitude 52. 15 minutes, and going to the arch of the 45 *Azimuth* on one side the *Zenith* line, and his match so many degrees distant on the other side, I take that Circle for my plain, his Center is the Center of the Planisphaer: the Meridian or Noon line of the Place in these Dyals is evermore the Axis or *Zenith* line of the *Reet*, for he is drawn to the Intersection of the Meridian of the Place

Place (here the *Limb*) with the plain. The *Zenith* line here lies Horizontal, therefore the Noon line in these East Recliners must be evermore the Horizontal line of the Dyal, as in all Decliners (Chapter 12.) the Noon line is evermore the Vertical or Perpendicular line.

The arch of my plain which is nearest to the North Pole hath his Pole in the *Finitor* 45 degrees from the Center Southward, and there this Pole is cut by the Meridian $31\frac{1}{4}$ from the Axis, this is the Meridian of my plain, and he is distant from the Meridian of the Place $58\frac{3}{4}$. (which is the difference of Longitude) this Meridian I follow to the arch of the plain which is nearest to the North Pole, and so going on in him to the Pole I number in him between the plain and the Pole 34 degrees, which is the Elevation of the Pole, and therefore also of the *Gnomon* above this plain : and between this Meridian of the plain and the Meridian of the Place at *Zenith* I reckon in the plain $42\frac{1}{2}$ for the Declination of the *Gnomon*.

Wherefore having drawn an Horizontal line N S for the Noon line, I appoint the Center at S the South end, because



the North Pole is Elevated, and drawing a blind arch, I set therein from the Horizontal line upwards $42\frac{1}{2}$. and there draw the Substyle S V.

Then I seek my hour distances, and I find the first hour-circle from the Meridian toward the Substyle cuts in the plain $14\frac{1}{2}$, therefore taking $14\frac{1}{2}$ in the blind arch from the Noon line toward the Substyle, I set 11. for so it is, and not 1. as you may perfectly perceive, if you hold but a Book or a Trencher after the Situation of your plain, somewhat near by guess, and consider which way the shadow must move, reason will tell you it moves downward in this Dyal from 11. to 12. &c. then I see the second hour-circle cuts the plain at $25\frac{1}{2}$ for 10. the next at $34\frac{3}{4}$ for 9. the next at $43\frac{1}{2}$ for 8. which happeneth a little above the Substyle, as he ought, for the difference of Longitude is almost 60. viz. $58\frac{3}{4}$. as before, next $51\frac{1}{2}$ for 7. next $61\frac{1}{3}$ for 6. next $73\frac{1}{3}$ for 5. next $88\frac{1}{2}$ for 4. and further I need not go in our Country.

Then in the other arch of the plain I find $19\frac{1}{2}$ for 1. 45 for 2. 71 for 3. and these I put in their places, as in the Figure. The *Gnomon* must stand square upon the Substyle, at an angle of 34 degrees.

Note that the Reclination must always be reckoned from the *Limb* inwards upon the *Finitor*, because where the *Finitor* touches the *Limb* there is our *Zenith* for this turn. Inclination is reckoned from the *Zenith* line, which here is both the Diameter of the Horizon, and Horizon itself.

For the Opposite or Inclining face of this Dyal plain, use the general way I shewed you, Chapter 12. that is, strike the Substyle and all the hour lines through the Center: and set the same figures to every hour line beyond the Center which he had on this side, and set the *Gnomon* upon the Substyle downward to behold the South Pole, and it is done. And so by the Inclining Dyal, if you had him first drawn, you might presently make the Recliner.

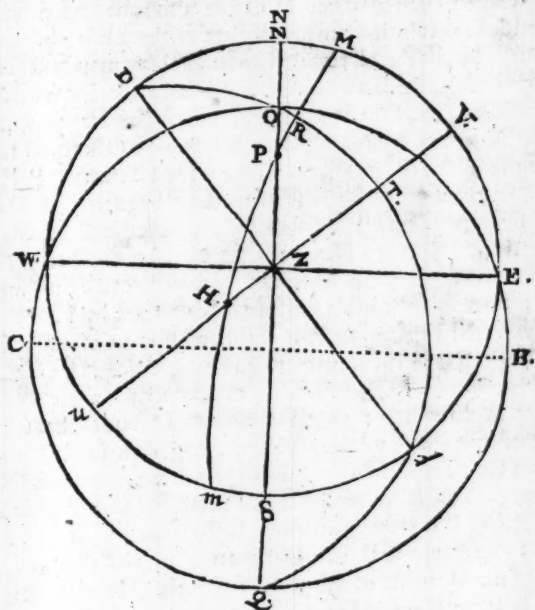
CHAP. XVI.

How to find the Arches and Angles that are requisite for the making of the Reclining Declining Dial.

BEfore you can Intelligently make a Reclining Declining Dial, which is the most Irregular of all, having two Anomalies, viz. Declination and Reclination, you must be acquainted with 3 Triangles in the Sphear, wherein certain arches and angles lie which are needfull to be known.

I advise you therefore first to draw (though it be but by aime) an Horizontal Projection of the Sphear, such as here I have drawn for a South Dial Declining West 50 degrees, and Reclining 60 degrees in the Latitude 52. 10. minutes, which shall be our Example.

The Circle E S W N is our Horizon N S our Meridian.



D T *d* the plain, Z T the Reclination thereof.

B *d* the Base or Horizontal line of the plain.

V *u* the Vertical of the plain cutting it right in T, and cutting the Pole thereof at H : for *u* is the Pole of a plain erected upon D *d*; but the Pole of the Reclined plain D T *d* is H.

S *u* or N V the Declination of the plain.

M P H *m* the Meridian of the plain, cutting the North Pole at P, the plain in Right angles at R, and the Pole thereof at H.

Now see your three Triangles all adjoyning in this Schem, viz. D N O and O R P Rectangled at N and R, and P Z H. Obtuse-angled at Z.

It is true that the last Triangle alone may do your work, or the two first may do it without the last; but you shall do well to be acquainted with them all.

In the first Triangle D N O you have given D N 40 degrees the Complement of the plains Declination, N the Right angle of our Meridian with our Horizon, D the Complement of Reclination, whereby you may find D O the Oblique Ascension of our Meridian; that is, how many degrees of the plain the noon-line shall lie above the Horizontal line : also you may find N O the Perpendicular Altitude of the noon-line, or the Inclination of the noon-line of the Dial to the Horizon ; (where you shall note that when this Altitude of the noon-line N O is equal to N P the Elevation of the Pole, then is the second Triangle P R O quite lost in the point P, and the plain then becometh a Declining Equinoctial plain) also you may find the angle O called the Position-Reclination for a reason hereafter to be shewed ; *Wittekinds* calls it, *Complementum repetendum*, because he means to have a Bout with it again, to find other arches by it.

In the second Triangle O R P you have given O, as before, for this angle was in the former Triangle, or his equal, (for *Anguli præcruæ oppositi sunt æquales*) R the Right angle of the plain with his Meridian : O P the position Latitude, that is, the Latitude of that Place wherein the Reclining plain O R T *d* Q, shall be a Circle of Position : this is given if you subtract N O the Perpendicular Altitude of the noon-line, out of N P your Latitude, (this O P is *Wittekinds* his *Differentia Retenta*.) And hence may be found O R the Declination of the *Gnomon*, or distance of the Meridian of the plain from the Meridian of the Place : R P the Elevation of the Pole above the plain in the
Plains

Plains own Meridian : P the angle between the Meridian of the plain and the Meridian of the Place: this angle is called the difference of Longitude, because it shewes how far the places are distant from us in Longitude, wherein this Dyal shall be a Direct Dyal, without Declination, having his *Gnomon* in the noon-line of the Place, and and shews also how many degrees of the Equinoctial, or how many hours and minutes there are between our Meridian and the Meridian of the plain, as the arch O R shews how many degrees of the plain come between the said Meridians, Let this be well observed by Learners.

In the Third Triangle P Z H, you have given P Z the Complement of your Latitude, Z H the Complement of the plains Reclination, and Z the Supplement of the plains Declination.

Hence may be found H P whose Complement is P R the Elevation of the Pole above the plain, P the difference of Longitude, H whose measure is R T the arch of the plain between the Meridian of the plain or Substyle and the Vertical line of the plain, the Complement whereof is R D the Substyle's distance from the Horizontal line of the plain.

Every arch and angle therefore in these Triangles is given, or may presently be found by the Problemes of Spherical Triangles, Book 3.

But I shall shew you a short and pleasant way to find them, by setting the whole Scheam at once on your Planisphear, where you shall have them almost all at one view.

For this purpose I use my Planisphear in the Horizontal Projection. But note, that I make use onely of the *Reet* and *Label*, and one of the Meridians of the *Mater*.

Thus I set D d on the Axis of the *Reet*, D T d on the 60th *Azimuth* from the Center, V u on the *Finitor*, Z N on the *Label*, fixing it in the *Limb* of the *Reet* 40 degrees from the *Zenith*, according to the arch D N. Then in the *Label* I make a prick with ink at P for the North Pole 52. 15. minutes within the *Limb*, and another prick in the *Finitor* at H for the Pole of the plain 30 degrees from the Center; which done, and keeping my *Label* fixed to my *Reet*, I turn the *Reet* till I see some one Meridian cutting both the pricks P and H, (as the 15 Meridian from the Axis shall do in this Example) and that Meridian shall serve for the Meridian of the plain for this time.

And by this time I see my three Triangles on my Planisphear,
and

their sides divided into degrees, as a Carpenters Rule into Inches, and I find for the Latitude 52. 10. minutes, that D O the Oblique Ascension of the Meridian is 44. 06.

N O the Altitude of the Meridian 20. 22. minutes.

O P the Position Latitude 31. 48. minutes.

O R the Declination of the *Gnomon* (13. 21. minutes) from the Meridian.

R P the Elevation of the *Gnomon* 29. 08. minutes, and P H Complement thereof,

H the distance of the Meridian of the plain and Vertical thereof, you may see by the arch of the plain which measureth the angle H, 32. 32. minutes.

Now have you nothing to ask of the third Book, but the angles O and P, and there you have divers ways to find that.

O the Position-Reclination is 67. 29. minutes.

P the difference of Longitude 26. 00 $\frac{1}{2}$. minutes.

CHAP. XVII.

How to find the Horary distances of a Reclining Declining Dial.

TAKE the easiest way first. You have seen Chapter 15. how easily East and West Reclining Dyals are to be made by the Planispher, because they fall out to be Circles of Position, and are plainly pictured by the *Azimuths*.

Now I will shew you how all Reclining Dyals may be reduced to East or West Recliners, for some Latitude or other, and so the hour distances found by the Method of the 15th Chapter.

The Circles of Position, as hath been shewed, do all cross one another in the North and South points of the Meridian. Now therefore by the point O where the plain cuts our Meridian, draw a new Horizon O B Q C, and then shall you see your plain in that Horizon to be a very Circle of Position. But now we are gotten into a new Latitude, O P called (before in Chapter 16) the Position Latitude, and we have here a new Reclination, for whereas this plains Reclination in our Latitude is Z D T 60 degrees, his Position Reclination is O, viz. Z O T, or P O R 67. 29. minutes.

Meridian: this therefore is the Meridian of my plain, and shall make the Sub-style on the Dyal: his distance from the Meridian of the Place in the Equinoctial is 26. and so much is the angle O P R the difference of Longitude, as before: then follow this Meridian of your plain to that arch of the plain which is next the Pole of the World, and you shall number from the plain to the Pole in the said Meridian 29. 08 minutes for the Elevation of the *Gnomon* P R, as before: and from this Meridian to the Meridian of the Place at the *Zenith* you shall number in the plain 13. 21 minutes for O R, the Declination of the *Gnomon*, as before.

Now the crossing of the plain with the Meridian of the Place is the Noon-point in the plain, and that in this case is always in the *Zenith*, and I see the rest of the Meridians cutting the plain for the Morning Hours, thus.

Hor. deg. min.

8-68 28

9-41 23

10-22 28

11- 9 35

12- 0 00

And for the Evening Hours
in the other arch, thus,

Hor. deg. min.

1- 7 56

Sub. 13 21

2-15 18

3-22 52

4-31 32

5-42 36

6-58 18

7-81 35

And because 7 in the Morning will be shewn by this Dyal in the Summer; to find the distance thereof from the Noon-line in the plain, I set *Nadir* in the place where *Zenith* was before, and so I see the 7th hour-circle cutting the plain at 98. 25. minutes. But this is more then I need to do: for having once found 12. Hour-spaces in any Dyal, I can make any of the rest by striking the Hour-line of the same denomination through the Center. As for Example. If I prolong the 7th of the afternoon Hour-lines beyond the Center, I there make the line of 7 a clock in the Morning.

line on both sides, *viz.* the Morning Hours below the Noon-line Westward, and the Evening Hours above it Eastward : as you may be taught by Chapter 2. Theorem 11. and by your own reason.

And lastly set the *Gnomon* Perpendicular upon the Sub-style A D, making his angle at A equal to the arch P R, found above to be 29.08. minutes, and your Dyal is done.

CHAP. XIX.

How to know at what Reclination any Declination Plain shall become a Declining Equinoctial Dyal-Plain, to be delineated after Chapter 7. And how to find the Oblique Ascension of his Meridian or Substyle, and the difference of Longitude, which are requisite for his Delineation.

T Here is no Declining plain but at some certain Reclination cutteth through the Poles of the World. and so becometh a Right Horizon. Therefore to find whither a Declining Reclining plain do happen to be a Declining Equinoctial plain, you shall observe what the Elevation of the Noon-line N O is ; for if that be equal to N P the Latitude, then doth the plain cut the Poles, otherwise not : And at what Reclination any Decliner shall cut the Poles, and so have the Altitude of his Noon line equal to the Latitude, you shall thus find.

Use the *Reet* and *Label* in the Horizontal Projection as you did Chapter 16. that is, set the Horizontal line of the plain D d on the Axis of the *Reet*, then number from the *Zenith* in the *Limb* of the *Reet* the Complement of the Declination, and thereto lay the *Label*, and having made a prick with ink in the *Label* for the Pole ($52\frac{1}{2}$ from the *Limb*) mark which of the *Azimuths* cutteth that Pole. for he sheweth you at what Reclination that Decliner shall cut the Pole and fall into the plain of one of the Meridians. And now you shall have but one Triangle to resolve, *viz.* D N P, (for the whole Triangle P R O of Chapter 16. is swallowed up in the point of the Pole P) and and D N P hath all his sides known, and the angle D at first Sight;

Sight; and for P you may find him if you turn the Triangle as Book 3. hath been shewed.

Example. I would make an Equinoctial Dyal in the West Declination 50. degrees, Lay the *Label* therefore 50. degrees from the *Finitor*, or 40. from the *Zenith*, and so the Axis of the *Reet* represents the plain Declining 50. degrees and the *Label* represents the North part of the Meridian, and now I see the *Azimuth* 26 $\frac{1}{2}$ from the Axis cutting the *Label* in the place of the Pole; therefore I say, that *Azimuth* represents the Equinoctial plain which belongs to this Declination.

And now I see the Triangle DNP on my Planispher, NP on the *Label* is the Latitude, and also the Altitude of the Noon line 52. 10. minutes, DN Complement of the Declination 40. DP the Oblique Ascension of the Noon line 61. 59. minutes, N is a Right angle, D is Complement of the Reclination 63. 28. minutes, (whose measure in the Scheme is TV) P the Complement of the difference of Longitude, for the difference of Longitude it self in the Scheme is HPZ, and the Complement thereof ZPT to which DNP is equal, by the Structure for it is *Angulus pre decussim oppositus*; and by any of the four first Problemes of Rectangled Triangles you may find it to be 46. 44. minutes, whose Complement is 43. 16. minutes, the difference of Longitude. The Oblique Ascension of the Noon line, and the difference of Longitude thus found, you shall have enough to make the Dyal by Chapter 7.

CHAP. XX.

An Admonition concerning the five several Cases of Declining Recliners.

BEcause by the diversity of Declination and Reclination, the figure and situation of the three Triangles mentioned Chapter 16. is so changed that you cannot alwayes find them on the sudden, unless you have a firm comprehension of the Spher in your head; and in the Case of the last Chapter the middle Triangle is quite lost, having all his sides and angles contracted into the very point of the Pole; therefore I have thought good to set down the 5 several Cases of these Dyals in so many several Schemes, and in every Scheme to mark the Tri-

angles with the same Letters, that what Case soever shall happen to be proposed; you may have a Scheme ready to direct you.

And to know which Scheme shall serve to express the situation of your plain, take these Rules

1. If the plain Recline North below the Pole, so that the arch NO the Perpendicular Altitude of the Noon line be less then NP the Elevation of the North Pole, then the first Scheme serves your Case.

2. If the plain Recline to the Pole making NP and NO equal, you shall use the Second Scheme.

3. If the plain Recline not so far as the Pole, but make NO greater then NP , you shall use the Third Scheme.

4. If the plain Recline Southward, then instead of the Triangle DNO you shall use the opposite Triangle dSO where if SO be greater then the Elevation of the Equator, or equal to it, you shall use the 4th Scheme. And if it be less, you shall use the Fifth.

And note that in the Fifth Case you may best do your work by the Triangle PHZ alone, (the Triangle PRO being here too big) setting off your Sub-style from the Vertical by the measure of the angle H , or of the arch TR , the Noon line from the Sub-style.

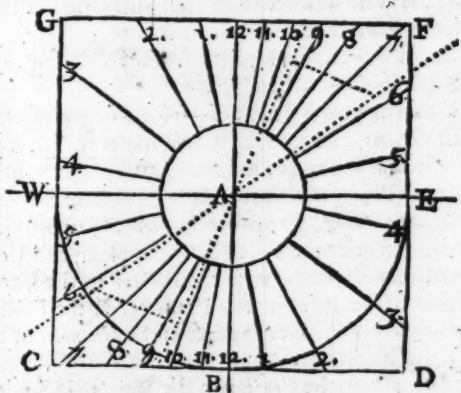
CHAP. XXI.

How to make the Declining Horizontal Dyal, another way then was shewed Chapter 12.

THough you have in the former Chapters a perfect Method for the making of all sorts of Dyals which give the Hour by the shadow of the Axis of the World, or a *Gnomon* set Parallel to it; yet I think it both pleasant and profitable for the Reader to see some other ways whereby the same things may be performed.

For the Declining Horizontal Dyal you shall first find the Elevation and Declination of the *Gnomon* after this manner. Take your Planisphere in the Horizontal Projection, and for the help of your fancy, lay it flat upon a Table, setting the Meridian, that is, the Equator line of the *Mater* in the Meridian of your Place by aim. Then set the *Finis* for your plain; and his Pole (which

(which is the *Zenith* of the *Reet*) shall be Eastward or Westward from the *Meridian* of the *Mater* so much as you observed the *Declination*: then seek the place of the Pole in the *Meridian*, viz. the North Pole 37. 45. minutes Northward from the Center, if the Wall look North, or the South Pole so much Southward, if the Wall look South: and it where not amiss if the Poles



were there marked with an *Asterisk*, or some such note, 38. or 40. degrees from the Center, somewhat near your Latitude, so these *Asterisks* (if they be not exactly the Poles for your Latitude) shall direct you to find the Poles presently, being very near them: as if the *Asterisk* be at 50. I know $2\frac{1}{4}$ more inwards is my Pole for Latitude $52\frac{1}{4}$. Next look what *Azimuth* cutteth this Pole, for he shall represent the *Meridian* of the plain; follow him to the *Finitor*, and you may number as you go the Elevation of the Pole above the plain; and the degrees of the *Finitor* between this *Azimuth* and the Center are the degrees of the *Declination* of the *Gnomon* or distance of the Sub-style from the *Meridian*.

2. Having found these two, You shall set your Planishear in the first Mode of the *Meridional Projection*: that is, Set the *Finitor* to the Elevation of the Pole above the plain, so shall you have all your Hour distances distinguished upon the *Finitor* by the *Meridians*. But here you must carry this in your head, that here the *Limb* is not the *Meridian* of your Place, but of the plain;

plain; and then to find the Meridian of your Place, number from the *Limb* in the *Finitor* the Declination of the *Gnomon*, and the Meridian cutting there is the Meridian of your place, and stands for Noon: therefore every 15th Meridian numbred from hence (and not from the *Limb* in this Case) is an Hour line for your Dyal: and look at what distance from the *Limb* they cut the *Finitor*, at the same distance from the Sub-style shall the Hour-lines be set in your Dyal plain.

Example. I have a South plain Erect Declining 30. degrees Eastward, (as in Chapter 12.)

And for this, First I set the *Zenith* 30 degrees from *Meridies*, toward *Oriens*, and so doth the *Finitor* represent my plain, and I see the *Azimuth* 21. 10. minutes cutting the South Pole of the Horizontal Projection about 38 degrees from the Center; from the Pole to the *Finitor* I number in this *Azimuth* 32. 01. minutes, the Elevation of the Pole above the plain; and from the Intersection of this *Azimuth* with the *Finitor* to the Center where the Meridian of the Place meets, I number in the *Finitor* 21. 10. minutes, so much is the Declination of the *Gnomon* or of his Sub-style from the Noon line.

Secondly, setting the *Finitor* to the Plain's Latitude 32. 01. minutes, I number from the South point of the *Finitor* inwards 21. 10. minutes, and there cuts the Meridian 36. 08. minutes from the *Limb*, shewing me the difference of Longitude, or Equinoctial distance of the Meridian of the Place from the Meridian of the plain; for this 36 Meridian is the Meridian of my Place, and therefore I mark him well, he is the Vertical of my Dyal, and also the Noon line. And here I consider that the Sub-style will be Westward from him upon the plain, because it Declines Eastward (by Chapter 2. Theorem 11.) Therefore beginning at Noon, where the 36 Meridian cutteth the *Finitor* I go 15. toward the *Limb*, and light upon the 21th Meridian from the Sub-style for 11 a clock, and he cutteth the *Finitor* at 11. 35. minutes from the *Limb*: so the 10th Hour is the sixt Meridian on this side the *Limb*, and cutteth the *Finitor* 3. 16. minutes; the 9th Hour is the ninth Meridian beyond the *Limb*, as you come back again, and cutteth the *Finitor* at 4. 44. minutes from the *Limb* or Sub-style on the other side (that is, Westward of the Sub-style in the Dyal.) In like manner you may gather the distances of the other Hour lines from the Sub-style into a Table, and thereby plot them down as in the Figure.

CHAP. XXII.

To make the Reclining Declining Dyal, another way.

HAVING found the arches and angles requisite by Chapter 16. and platted down your Horizontal and Vertical lines, and placed the Noon line above or below the Horizontal line, according as the arch of his Oblique Ascension or Descension requireth, and having placed also the Sub-style in his due situation as is above taught, you may easily find the distances of the several Hours from the Sub-style, as you found them in the former Chapter for the Declining Horizontal Dyal.

For when you have set the *Finitor* to the Latitude of your plain, as there you did, the *Limb* is Sub-stylar, and if you number thence in the *Finitor* the Declination of the *Gnomon*, there shall meet you the Meridian of the Place. Here you shall begin, and take every 15th Meridian forwards and backwards for an Hour line, and observing how many degrees are in the *Finitor* between the *Limb* and every one of these Hour lines, so many degrees shall you place that Hour line from the Sub-style in the plain. If you understand the former Chapter this will need no Example.

CHAP. XXIII.

To draw the proper Hours of any Declining Dyal.

EVERY Declining plain, whether it Recline or not, hath two great Meridians much spoken of. 1. The Meridian of the plain, which is the proper Meridian of that Country to whose Horizon the plain lieth Parallel. 2. The Meridian of the Place, which is the Meridian of your Country, in which you set up this Declining plain to shew the Hours; and so either of these Meridians Dyals may be conformed. How to draw the Hours of our Country on such a plain is the harder work, because the plain is Irregular to our Horizon: yet I suppose I have made the way very easy in the former Chapters. But to draw the Hours of the Country to which the plain belongs, is most easy. For if you take the Sub-stylar for the Noon-line,

and the Elevation of the Pole above the plain for the Latitude, you may make this Dyal in all points like the Vertical Dyal, after the precept of the 9th Chapter,

CHAP. XXIV.

To know in what Country any Declining Dyal shall serve for a Vertical Dyal.

IF the Dyal Decline East, add the difference of Longitude (found as above Chapter 21.) to the Longitude of your Place, and the sum or the excess above 360 is the number of the Longitude sought. If the Dyal Decline West subtract the said difference of Longitude out of the Longitude of your Place, and the difference is the Longitude inquired: but when the Longitude of your Place happens to be less then the difference of Longitude you must add to it 360, before you subtract the difference of Longitude. The Elevation of the Pole above the plain is the Latitude of the Place inquired.

Example. The Declining plain of Chapter 12. will be a Vertical plain in the Longitude 61. degrees, and North Latitude 32. degrees, that is, in the *Mediterranean Sea* between *Alexandria* and the Isle of *Cress*. And the Declining-Reclining plain of Chapter 16, 17, 18. is Parallel to the Horizon of those that sail in Longitude 359. degrees, and North Latitude 29. degrees, that is as *Terrestrial Globes* and *Mapps* shew me, between the *Azores* and *Hesperides*.

CHAP. XXV.

To set a Plain Parallel to the Horizon of any Country proposed.

IF you can get the Declination and Reclination of such a plain, you have enough to place him in his true Situation. And those may be found by the difference of Longitude, and the Latitude of the strange Country, (which are in this Probleme supposed to be given) even as in Chapter 16. you found both those by the Declination and Reclination given.

Example. I would set a plain Parallel to the Horizon of *Jerusalem*,

salem, to shew me what time the Sun Rises and Sets there any day of the Year, and what Hour passeth at *Jerusalem* at any time of our day. First I seek by *Geographical Tables* or *Mapps* the Longitude and Latitude of *Jerusalem*, and I find that *Jerusalem* is removed Eastward from *London* in Longitude 47 degrees, and that the Latitude there is 32 degrees, or thereabouts. Therefore in the Rectangled Triangle *P R O* of Chapter 16. I have the angle *P* 47 degrees difference of Longitude, also the side *P R* the Latitude of *Jerusalem* 32 degrees, and hence by the 4th Probleme of Rectangled Triangles Book 3. 6. I get *PO* 42. 30 minutes, and by consequence *ON* 9. 45. minutes (because *P N* is our Latitude) and I get also the angle *O* 51. 40 minutes. And these had, I get by the same Probleme in the adjoining Triangle *ON D*, both *DN* 12. 05. degrees, the Complement of the Declination inquired, and the angle *D* 39. 23. Complement of the Reclination inquired. Wherefore I conclude that a plain which shall represent here the Horizon of *Jerusalem* must Decline Eastward 77. 55. minutes, and Recline Northward 50. 37. minutes. Draw upon this plain the proper Hours of *Jerusalem*, by Chapter 23. and know that when the Sun leaveth this plain ceasing to enlighten the upper part of it, then he setteth at *Jerusalem*, and look how many Hours and minutes the Sun setteth after noon in any Country, so many Hours and minutes he rose before noon.

CHAP. XXVI.

How other Circles of the Sphear besides the Meridians may be Projected upon Dyals.

THe Projection of some other Circles of the Sphear beside the Meridians though it be not necessary for finding the Hours, yet may be both an ornament to Dyals, and usefull also for finding the Meridian, and placing the Dial in his due Situation, if it be made upon a moveable Body, as shall be shewed Chapter 33.

The Circles fittest to be projected in all Dyals for those purposes are the Equator with the *Tropiques*, and other his Parallels; which may be accounted Parallels of Declination, as they pass through equal degrees, as every 5th or 10th of Declination: or Parallels of the Signs, as they pass through such degrees of De-

clination as the Sun Declineth, when he entrench into any signe, or any notable degree thereof; or Parallels of the length of the day, as they pass through such degrees of Declination wherein the Sun increaseth or decreaseth the length of the day by Hours or half-Hours,

Also the Horizon with his *Azimuths* and *Almicantars* are an ornament to Horizontal and Vertical Dyals; and are likewise usefull for projecting the Equator and his Parallels in all Dyals. My purpose is to be breif in this Treatise of the *Limature* here following because I hasten to an end. I shall therefore think it sufficient if I shew you one way to furnish any Dial with the Circles of the Sphear. Leaving you to devise others which I could have shewn.

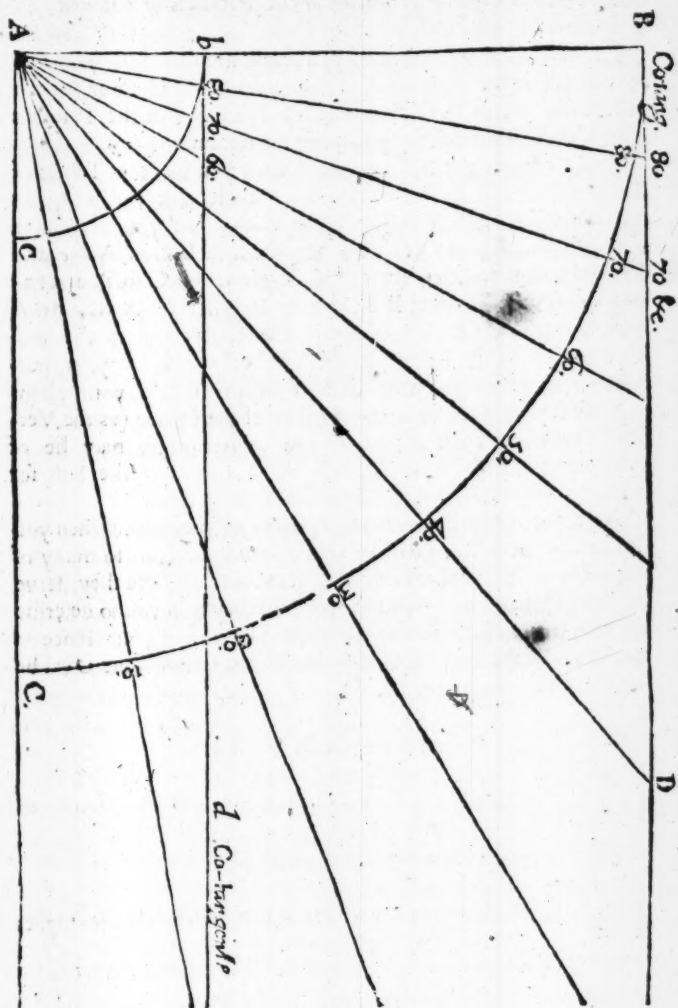
CHAP. XXVII.

How to describe on any Dial the proper Azimuths and Almicantars of the Plain.

F Rom any point of the *Gnomon* (taken at pleasure) let fall a Perpendicular upon the Sub-style; that Perpendicular shall be part of the Axis of the plain, and shall be reputed *Radius* to the Horizon of your plain. The top of this *Radius* in the *Gnomon* is called *Nodus*, because you must there set a Knot, Bead, or Button to give shade, or else cut there a notch in the *Gnomon*, or cut off the *Gnomon* in the Place of *Nodus*, that the end may give the shadow for thole lineaments. Let not your *Nodus* stand too high above the plain, for then the shadow will fall beside your point for too great a part of the plains day nor let it stand too low, for then the lineaments will run too close together. A mean must be chosen.

At the foot of this *Radius* take your Center, and describe a Circle on the plain and divide it into equal-degrees; and from the Center draw lines through thole degrees infinitely, that is, so far as your Dial-plain will bear; these lines shall be the *Azimuths* of the Horizon of the plain, and shall be numbred from his Meridian or Sub style.

Divide any of these *Azimuth* lines into degrees, by Tangents agreeable to the said *Radius*, and having made a prick at every degree, through every of these pricks, you shall draw Parallel
Cir-



Circles which shall be *Almicantars* or *Parallels of Altitude*, to be numbred inwards, so that at the Center be 90. for the *Zenith*, and from the Center outwards you shall number 80, 70, 60, &c. till you come within 10, or 5 degrees of the *Horizon*; for the plain is too narrow to receive his own *Horizon*, or the *Parallels* near, if the *Nodus* have any *Competent Altitude*.

And to divide the said *Azimuth* lines you use the *Tables of Tangents* with a *Scale of equal parts*, or else plot the *Tangents* thus on paper, let A B equal to the *Radius* of your *Horizon*, and with that *Radius* draw the *Quadrant* A B C, or A b c, and divide the *Quadrant*, numbring the degrees from C to B, and having drawn the *Tangent* B D, or B d, *Parallel* to A C, draw lines from the Center through the several degrees to the said *Tangent-line*, so shall this *Tangent-line* be divided for your purpose: and from it you may transfer the divisions to your plain.

Now if your plain lie in the *Horizon* of your place, (as the *Vertical* plain doth) theie *Azimuths* and *Almicantars* may be of some use to shew you the *Altitude* and *Azimuth* of the *Sun* for any time. See them in the *Scheam* Chapter 30.

But if your plain lie not in the *Horizon* of your place, then you shall draw the said *Almicantars* or *Azimuths*, or so many of them as you shall need, in delectable lines, because here they serve only the *Horizon* of the plain: yet shall they help you to describe the *Equator* and his *Parallels*, with the *Horizon* of your *Place* in any *Dyal*: and when they have done this, unless your *Dyal* be *Vertical*, they may be gone.

CHAP. XXVIII.

How by help of the proper Azimuths and Almicantars of the Plain to describe the Equator and his Parallels, on the Polar or Orthognomonical Dyal.

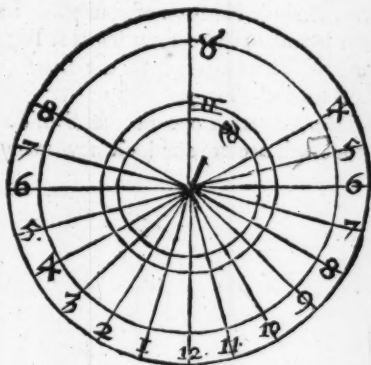
IT shall suffice here to shew how the *Parallels* of the *Sigæes* may be described, because the *Parallels* of *Declination*, and of the length of the day, are described by like reason. And know that in the *Polar* plain because the *Gnomon* is *Perpendicular* to the plain, the same *Gnomon* shall serve both *Hours* and *Azimuths*; for the *Hour-lines* be *Azimuths* in this plain. Note

also

also that the Sun is never Elevated above this plain more then he Declineth from the Equator, which at the most is $23\frac{1}{2}$ degrees, and that if the height of *Nodus* be above a sixth part of the Semidiameter of the plain, the ten first *Almicantars* will fall beside the plain. A sixth part therefore must serve, and that will give you all the Altitudes above 10 degrees, and the Parallels of the Signes whose Declination is more then 10.

Describe therefore the *Almicantars* here, as you were taught Chapter 27. for in the Hour lines you have already every 15th *Azimuth*, and may draw more if you please.

Then know that the *Almicantars* here are the very Parallels of Declination, becaute the Equator is the Horizon of this plain, and if you draw the *Almicantar* 11. 30 minutes, that shall be the Parallel of γ or π becaute so much is the Suns Declination. and also his Altitude above this plain, when he entreth those Signes the *Almicantar* for 20. 13. minutes is the Parallel for π and δ in like manner, and the *Almicantar* 23. 30. minutes the Parallel for δ . And by like reason you may draw the Parallels of the South Signes on the South face.



CHAP. XXIX.

How to inscribe the Equator and his Parallels, in the Equinoctial or Parallelognomonical Dial.

IF this plain Decline not, the Hour lines of your Country will serve you for they be also the Hour lines of the plain, and the Noon-line is Sub style: if it do Decline, you shall draw in deuble lines the proper Dial of the plain (by Chapter 23. which Declineth not.

And having here the *Azimuths* or *Almicantars* of the plain, drawn

tween the *Label* and the *Equator* line, so much is the *Azimuth* of that Hour from the East or West in the *Tropique* of *Cancer*: and the degree of the *Label* cut at the same time by the *Tropique* and the Hour line is the *Altitude* sought. Do so for the second Hour circle, (which here is 8. and so for the rest in order 9, 10, 11, 12. and you shall find that in the *Tropique* of *Cancer* in the Morning the Sun hath *Azimuth* from the East Northward, and *Altitude* as followeth,

	<i>Azi. min.</i>	<i>Alt. min.</i>	In the Equator
7.	24. 20.	13. 44.	the <i>Azimuth</i> is
8.	26. 45.	27. 18.	always the same,
9.	31. 30.	40. 25.	full East or West,
10.	40. 40.	53. 35.	and so upon your
11.	58. 30.	62. 20.	plain he must
12.	90. 00.	66. 30.	needs be a straight
			line. The <i>Altitudes</i>

in the Equator are 15, 30, 45, 60, 75, 90.

The Hours alike distant from the Meridian on both sides are alike, and so are the Parallels alike distant from the Equator alike also.

When you have therefore gathered a Table out of your Planispher for the Morning Hours of the North Parallels, and of the Equator, (as I have done here in half for the Equator, and *Tropique* of *Cancer*) you may by that Table prick down the Parallels upon one quarter of your Dial, and by that also draw the rest; for as you may see upon your Planispher, all the 4. quarters are alike.

Note that the *Azimuths* cut the Hour lines too Obliquely: it is best therefore to trust to the *Almicantars*, and so shall you have easier and surer work, though you meddle not with the *Azimuths* at all.

CHAP. XXX.

How to inscribe the Equator and his Parallels, in an Oblique or Scalognomonical Dial.

IF the plain neither Decline nor Recline, and so be a Vertical plain, the Hour lines of your Place will serve you. for they be also the Hour lines of the plain, and the Noon line is the

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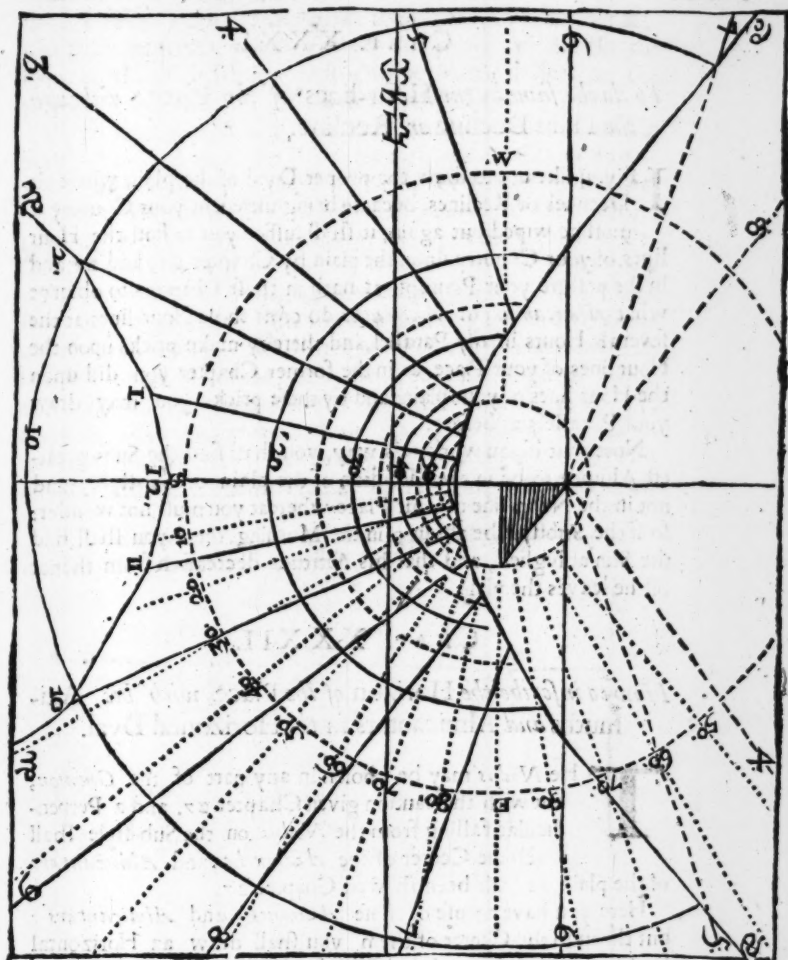
Sub-style. It it either Decline or Recline, or both Decline and Recline, you shall draw in deble lines the proper Dyal of the plain by Chapter 23. and so this Dyal shall be reduced to a Vertical Dyal, and be as easily furnished with the Parallels as the Vertical: and when you have by the deble Hour lines of the plain inscribed the Parallels, you may wipe out those Hour lines of the plain, and let the Hour lines of the place and the Parallels stand.

Having therefore drawn the *Azimuths* or *Almicantars* of your plain by Chapter 27. take your Planispher in the Meridional Projection, setting the *Finitor* to the Latitude of your plain; Then find your Equator and Parallels on the *Mater*, and where the several Hour lines intersect them above the *Finitor*, mark what *Azimuth* or rather what *Almicantar* passeth through these intersections; for in the same *Azimuth* and *Almicantar* shall the Parallels cut the Hour lines of the plain upon the plain.

Example. In the Vertical Dyal for our Latitude 52. 15. minutes, I set the *Finitor* to this Latitude, and going first to the *Tropique* of *Cancer*, I begin at the *Limb*, that is, at Noon, there I see the *Azimuth* full South, the Altitude 61. 15. minutes, at 1. a clock: *Azimuth* 27. Altitude 59. at 2. *Azimuth* 49. Altitude 53. at 3. *Azimuth* 67. Altitude 45. &c. Therefore where I find the Noon line of my plain cut by the *Almicantar* 61. I make a prick, and in the Hour lines of 11 and of 1. where the *Azimuth* 27 and the *Almicantar* 59 meet, I make pricks, and where the *Azimuth* 49 and the *Almicantar* 53 do meet upon the Hour lines of 10. 2. I make pricks, and so for the rest.

Lastly I draw with an even hand a crooked line without angles through those pricks, and that shall be the Parallel or *Tropique* of *Cancer*: and in like manner I put in all the other Parallels, and the Equator in the midst of them, though for the Equator you may draw him more speedily by striking a line through the Center of the *Almicantars* making Right angles with the Sub-style. And that may be a general Rule for the Equator in all Dyals which have a Substyle, and in the Polar Dyal where there is no Substyle, the Equator shall be a Circle, as before is shewn.

Note here that if your Dyal be great, and you have not points enough to govern you in the draught of the Conical Sections, you may draw half-hour-lines, and find points in them also, after the same manner.



C c 2

CHAP. XXXI.

To do the same by the Hour-lines of the Place, although the Plain Decline or Recline.

IF you like not to draw the proper Dyal of the plain where it Declines or Reclines, because being useless in your Country, it must be wiped out again, it shall suffice you to find the Hour lines of your Country upon the plain, by Chapter 21, and 22 and in the posture your Planispheric hath in those Chapters, to observe what *Almicantars* or *Azimuths* do cross those Hour lines at the several Hours in any Parallel, and thereby make pricks upon the Hour lines of your Place, as in the former Chapter you did upon the Hour lines of your plain; and by these pricks you may draw your Parallels as before.

Note that if you work this way, you shall find the Suns greatest Altitude to be in the Meridian of the plain or Substyle, and not in the Noon-line of your Place; whereat you must not wonder: so if the Substyle be about 9 in the Morning, there you shall find the Sun at highest, and that his Altitude decreaseth from thence till he leaves the plain.

CHAP. XX XII.

How to inscribe the Horizon of the Place, with his Azimuths and Almicantars, in the Horizontal Dyal.

THe *Nodus* may be chosen in any part of the *Gnomon*, but with the caution given Chapter 27. and a Perpendicular falling from the *Nodus* on the Sub-style shall touch the Center of the *Azimuths* and *Almicantars* of the plain, as hath been shewed Chapter 27.

Here you have no use of those *Azimuths* and *Almicantars*: but through the Center of them you shall draw an Horizontal line, by Chapter 3. and that shall be Horizon.

Now if your plain Decline not from the Meridian, and so this Center fall upon the Noon line, you shall divide your Horizon both ways from the Center, as you were taught to divide the *Azimuthal* lines by *Tangents*, Chapter 27. and shall number those

you will have them, do thus. If the plain Decline not, set the *Finitor* to the Latitude of your Place, as Chapter 10. and if it Decline, set the *Finitor* to the Latitude of your plain as Chapter 21. Then keeping your ey above the Horizon, and within the *Tropiques*, mark what Hour lines the 10th *Almicantar* (for Example) cutteth, and what *Azimuth* there with him cutteth the same Hour lines also, and in the intersections of the same *Azimuths* and Hour lines upon your plain you shall make marks, through which the tenth *Almicantar* shall be drawn: and so of the rest.

Note here That your *Azimuths* and *Almicantars* must not be drawn beyond the *Tropiques*, nor beyond the Horizon: neither must the Hour lines, if the *Nodus* be the end of the *Gnomon*.

The Scheam shews you how the *Azimuths* may be drawn on the Dyal of Chapter 12, and 21. Declining East 30 degrees.

CHAP. XXXIII.

How by the help of this Furniture to place any moveable Dyal-Plain in his true Situation, and consequently to find the Meridian-line of the Place, without any other Instrument then the Dyal it self.

S Et the Dyal upon a level Table or Board, and turn it till the shadow of the *Nodus* touch the Suns Parallel, *Azimuth*, or *Almicantar*, any or all of them: but the Parallel shall best guide you, because that is most easily known by memory without Observation. And when the shadow of the *Nodus* toucheth the Suns Parallel it shews there the Hour also; and moreover it shews the Suns Altitude and *Azimuth* for the same Time if the *Azimuths* and *Almicantars* also be drawn upon your Dyal.

But you shall note here, that the shadow of the *Nodus* may touch the Parallel at like distance from the Sub-style on both sides. Therefore if you be in doubt which is the true place of touching (as you may well doubt when the shadow cuts the Parallel near the Sub-style) you shall Observe a while whether the shadow of the *Radius* be lengthning or shortning: If it shorten, the Sun is not come to the Sub-style, and so the earlier Hour

Hour shewed is the true Hour ; If it lengthen, the Sun is past the Sub-style, and the later Hour is the true Hour. And when the Dyal shews the true Hour, the *Gnomon* and the plains Parallel thereto do point North and South. And here you may see, that the further the Sun is from the Sub-style, the more easily is the Dyal placed.

Thus may you make a very commodious Polar Dyal, to stand in a chamber Window, and to remove from Window to Window as the Sun goes, which shall find the Meridian line it self any where, in the 4. *Summer* and 4. *Winter* Moneths; and if you will make him a *Limb*, like the *Limb* of a Box-lid of a Cheese-fat, to receive the Parallels near the Equinoctial, which else fall beyond the plain, he shall serve for all the Year,

CHAP. XXXIV.

How to make a Vertical Dyal upon the Ceiling of a Floor within Dores, where the Direct Beams of the Sun never come.

THe greatest part and as much as you shall use of the Vertical Dyal described Chapter 9. may by Reflection be turned upside down, and placed upon a Ceiling, but the Center will be in the Air without Dores.

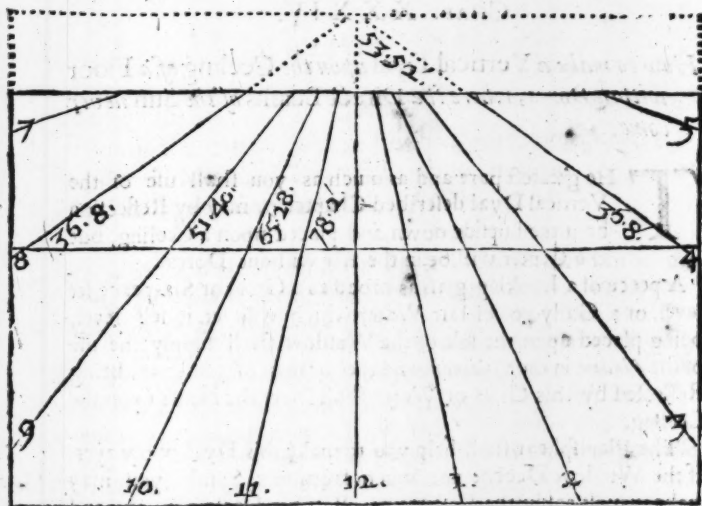
A peece of a Looking-glass as broad as a Groat or Six-pence set level, or a Gally-pot of fair Water, which will set it self level, being placed upon the sole of the Window shall supply the use of the *Nodus* in the *Gnomon*, and the beams of the Sun being Reflected by this Glass or Water shall shew the Hours upon the Ceiling.

The Planishear shall help you to make this Dyal two ways. If the Window Decline not much from the South, you may make it most easily the First way. But if it Decline much, and so the lines fall much upon the partition Walls, or if you would adorn this Dyal with the Parallels or other Circles, you shall use the Second way.

The First way is this Draw a Meridian line upon the Floor, by Book 4. 3. so that it may point upon the Perpendicular, which you shall imagine to fall from the *Nodus* upon the plain of the Floor prolonged. And this may be most easily done, if you hang

hang a Plumb-line in the Window directly over the *Nodus* of place of the Glais, for the shadow which that Plumb-line gives upon the Floor at Noon, is the Meridian line sought; and by a Ruler or a line stetched upon it you may prolong it as far as you shall need.

Then let a Plumb-line fall from the Ceiling upon this Meridian line of the Floor, and behind it Northward or Southward, place your Ey, so that the Plumb-line may hide the Meridian line of the Floor from your Ey: then keeping your head steddly, call you: Ey up to the Ceiling, and direct One to make two points at a good distance, in the line upon the Ceiling which the Plumb-line now covereth from your Ey, and by these points you shall draw a straight Meridian on the Ceiling.



Then having fastned one end of a Line at *Nodus*, let Another stretch this line up to the Meridian on the Ceiling, and let him move his hand nearer or further in the Meridian till you find by a Quadrant that this line pointeth up Northward as many degrees as the Elevation of the Equator is in your Country, and then you shall cause him to make a point where the line toucheth the

the Meridian of the Cieling, and through that point you shall draw the Equinoctial line of your Dyal, cutting the said Meridian at Right angles. The length of the thred from the *Nodus* to the point in the Meridian where the Equinoctial cuts him, is *Radius* of the Equinoctial: to that *Radius* you shall find the *Tangents* of 15, 30, 45, 60, 75. as you found the *Co-tangents* Chapter 27. (knowing that the *Co-tangents* of 80, and 70. be the *Tangents* of 10, and 20. and so of the rest) and beginning in the Meridian make pricks in the Equinoctial line, at the end of the *Tangent* of 15. Eastward for 1. and Westward for 11. and at the end of the *Tangent* of 30. prick Eastward 2. and Westward 10. &c.

Then by Chapter 9. seek what angles the Hour lines of a Vertical Dyal make at the Center, which in our Latitude are 1. 11. 58. minutes, 2. 24. 32. minutes, 3. 38. 20. minutes, 4. 53. 52. minutes, 5. 71. 17. minutes, and with the Complements of these angles shall these Hour lines cross the Equinoctial: so the Hour line of 1. shall Incline to the Meridian on the South side the Equinoctial line, and shall make his lesser angle with the Equinoctial 78. 02. minutes, and the rest as in the Figure.

The Second way is this. Fit a plain smooth Board about a foot Square to lie level from the sole of the Window inwards, and near the outer edge thereof make a Center in the board in the very place of *Nodus*, or a little under it, remembering that the *Nodus* or Center of the Glass must be set so much higher then this board, as the Center of your Quadrant is placed higher in the Projecting of the Dyal.

Upon that Center taken in the board describe as much of a Circle as you may with the Semidiameter of your Quadrant; which Circle shall be Horizon: Draw here from the Center to the Horizon inwards a Meridian line, by Book 4. 3. and where it cuts the Horizon begin to graduate the Horizon into degrees of *Azimuths* both wayes, which you may speedily do, by transferring the graduations of your Quadrant, or so much as you shall need, to this Horizon.

Next you must devise to make your Quadrant stand firm and upright upon one of his straight sides, (which I will call his foot for this time) and that you may thus do; Take a short peece of a Ruler or smal Transom, and saw in one side of it a notch Perpendicularly, in which notch you may stick fast or wedge the heel or the toe of your Quadrant, in such sort that his foot may come

close to the board, and the other straight side or leg may stand Perpendicular upon it.

Those things prepared, put your Planisphaer in the Meridional Projection, with the *Finitor* at your Latitude, and first observe there the Altitudes of the Sun in the Meridian, which in Latitude 52. 15. minutes, you shall find in the *Tropique* of \S 61. 15. minutes, in the Equator 37. 45. minutes, and in the *Tropique* of \vee 14. 15. minutes. Now having stuck a short needle in the Center of the Horizon, close to which you must alwayes keep the Center of your Quadrant, set the foot of your Quadrant in the Meridian line of the Board, and from the Center of your Quadrant extend a thred by 14. 15. minutes of Altitude straight on to the Cieling (the thred only touching the plain of the Quadrant and making no angle with it, but held Parallel) and where the thred thus extended touches the Cieling make a point, then the Quadrant unmoved, extend the thred by 61. 15. minutes of Altitude, and make another point as before, and between these two points draw a straight line, and that shall be your Meridian, and shall be long enough for your use: then extend the thred by 37. 45. minutes of Altitude, and where it touches this Meridian cross the Meridian at Right angles with an infinite line, which shall be the Equator. Then seek upon your Planisphaer for one a clock, and you shall find in the *Tropique* of \vee the Suns *Azimuth* 14. and his Altitude 13. 06. In the *Tropique* of \S his *Azimuth* 27¹/₂ and his Altitude 59. 04. minutes: therefore setting the foot of the Quadrant in the *Azimuth* 14. from the Meridian Eastward, I extend the thred by 13. 06. of Altitude, and make a prick in the Cieling: and again setting the foot of the Quadrant in *Azimuth* 27¹/₂. and extending the thred by 59. 04. minutes of Altitude, I make another prick in the Cieling, and the straight line which I shall draw between these two pricks shall be all the Hourlines of One, and so of the rest. And if you be minded to have the other Parallels drawn, you may find points for them as you have done for the *Tropiques*, and by those points draw them. And note that two points made in the Cieling for the same Hour line in any two Parallels, or in the Equator and any Parallel, shall suffice to direct the line, though it is best to take your points in the *Tropiques*, at the largest distance, as I have here done, if there be room enough on the Cieling.

But because it often happens that part of your Dyal falls beside
the

the Cieling, and the plain of the Cieling and of the Walls is often interrupted, and made Irregular by Beams, Wal-plates, Cornishes, Wainscot, Chimney-peece, and such like bodyes, I will shew you one absolute device to carry on your Hour lines over all.

Extend the thred for any Hour line to the *Tropique* of *Cancer* in the Cieling, as you were taught before, and fix it there, and extend another thred in like manner to the *Tropique* of *Copricorn*; where ever it shall happen, (as perhaps beyond the middle beam, or quite beyond the Cieling upon the Wall) and fix that thred also. Then place your Ey to behind these threds that one of them may cover the other, and at the same instant where the upper line (to your Sight or Imagination) cuts the Cieling, Beams, Wall, or any Regular or Irregular body, above the end of the lower line, there shall the Hour line pass from *Tropique* to *Tropique*: direct any By-stander to make marks as many as you shall need; and by these marks draw the Hour line according to your desire.

If the arch of the Horizon between the *Tropiques* be within view of your Window, you shall draw the same on the Wall to bound the Parallels, the Horizons Altitude you know is nothing, and therefore he will be a level line; and the Suns *Azimuth* when he riseth (commonly called *Amplitude*, and *Orrive Latitude*) is in *Cancer* 40. 40. minutes East Northward, and in *Capricorn* as much Southward; and these will be reflected to the contrary coasts on the Dyal.

The end of the Fifth Book.

A breif Description Of a CROSS-STAFF.

THe Cross-staff consisteth of two Rules joyned (by a socket, or else pinned) in the form of a *Romane T*, and three Sights, or more.

The longer Ruler is called *Radius, Index*, and the *Yard*, as A B, of which I call A the neer end, B the further end. The breadth would be $\frac{3}{4}$ of an inch, the depth an inch and half, the length 70 or 80. inches: and every of those inches would be divided by Parallels and Diagonal lines into 100. equal parts.

The shorter Ruler E F is called the *Transom*; it would be half an inch or three quarters, both in breadth and depth, and in length about 2. foot: for the Sights there, if I may advise you, would never be set above 20. inches asunder.

This *Transom* would be divided into whole inches onely, beginning in the midst at B in the visual line \odot B, and numbred to 10 both wayes.

The Sights C and D must have sockets at the bottom, through which the *Transom* must pass, so that the Sights may be set to any division of the *Transom*. The Vanes or tops of those Sights must have onely two edges on their sides, visible to your ey, namely those edges which touch the *Transom*; and the two other edges must be pared away.

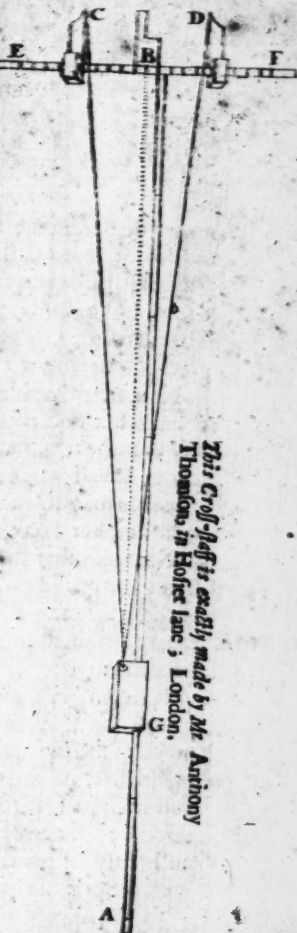
The middle Sight at B would have half his head cut away, and a shoulder left, as in the Figure, and a tenon at the bottom fitted to a mortise made in the middle of the *Transom*, that you may stick him in and take him out when you please, for to this mortise you shall do well to fit two other moveable Sights very narrow, for observing the Diameter of the Moon, or the distance of Stars which are very neer: one may be about half an inch broad, and the other about a quarter.

The *Index* must have one broad Sight, G \odot , made with a socket to ride upon the *Index*, it would be three inches and a half

half high above the Radius: the breadth at least three inches, and the mortise through which the Radius slippeth would be made neer the right side of the Sight, that full half of the Sights breadth (or more, may be on the left side the Radius. At the upper corner of this Sight leftward, as at \odot , you shall with a Gouge hollow a pit for your ey, on the backside: in the midtt of which pit you shall bore an hole quize through, big enough to receive a Goof-quill: also you shall round the corner of the Sight that it may fit the inner corner of your ey, that the left side of the Sight may lie close to your Nose in observing. The Fiducial edge of the middle Sight of the Transom must so answer this Ey-hole, that it keep the same distance from the side of the Radius leftward; and the distance would be about an inch and quarter, that your right Ey may easily come at the hole while the Index slippeth upon your right shoulder, and so your true Radius shall be the pricked line $\odot B$, running beside the Index, but Parallel to it, and this line must cut the middle of the Transom, and the middle of his middlemost Sights.

When you would use this Staff, you shall first set the Sights of the Transom to like inches, as at 10, and 10. if the angle be great, or at 5, and 5. as in the Figure they are placed: alwayes set them at whole inches, and at like numbers on both sides from the middle of the Transom: and choose to place those Sights so that your Ey-sight may be far distant from them in observing, for so you may the more distinctly observe the minutes and seconds of the angle inquired. Then resting the further end of the Index upon a Wall

This Cross-staff is exactly made by Mr Anthony Thompson in Holbe Lane; London.



or some device fixed for that purpose, put the neer end over your right shoulder : and setting your Ey to the Ey-hole, slip the Index backward or forward till you see the objects by the sides of the Sights of the Transom ; and mark what number the back-side of the Ey-sight cutteth upon the Index, for that shall give you the angle sought in this manner.

Example. The Sights of the Transom being set at 5, and 5, that is, 10. inches asunder, I observed two Steeples by their edges, and the Ey-sight then cut upon the Index, 6625. that is, inches $66\frac{1}{4}$ from the Transom. I say therefore, As C B 500. to B G 6625. so C B Radius or 100000. to B G the Co-tangent of half the angle. Here I have no more to do then to divide 662500000. by 500. or 6625000. by 5. which is an easy work, and the Quotient 1325000. is the Co-tangent of 4. degrees 18. minutes 57. seconds 43. thirds, for half the angle.

Note here, that if the Sights had stood at 10, and 10. then had the number 6625. been the very Co-tangent of half the angle : and remembring that your Radius on the Transom hath but 1000. actual parts, go to the Canon, and cutting off so many places as may leave the Radius there but 1000. you shall find your number 6625. to be the Co-tangent of 8. 35 minutes.

Note also, that you may observe the angle between the middle Sight and one of the other : and then you find the Co-tangent of the whole angle to that Radius to which your Sight is set on the Transom, as to the Radius 200. 300. or any other even hundred to 1000.

Note further, that you must evermore observe neer the tops of your Sights, that the visual lines may run above the Transom as much as the Ey is placed above the plain of it.

He that will, may have room to set several Scales of degrees and minutes to several Radiusses, as one to the Radius 300. another to 500. another to 700. by which the very degrees and minutes may be presently had, without recourse to the Tables. To me the Scale of equal parts is in stead of all.

The Commodities of this disposition of the Staff, are these.

1. It is better managed when it rests upon the shoulder, and the Ey-sight being made to move while the Transom and his Sights stand Fixed, shall save you much labour of coursing up and

and down from one end of the Staff to the other in observing.

2. The Ey-sight being made to shew the angle by the length of the Co-tangents, shall alwayes give you large differences: in-somuch, that if your Staff be but 6. foot long you may observe to Seconds, and Thirds in lesser angles, and till you come beyond 20. degrees, your Sight shall seldom move less then the tenth part of an inch for one minute. And beyond 30. or 40. degrees this Instrument would not be used, because the Ey cannot see both the Sights of the Transom at once, without rolling from one to another, whereby the Center of Vision is changed.

3. Your Ey is better fixed and shadowed by this Ey-sight, then when the end of the Index is placed by guess upon the Cheek-bone.

The inconvenience here is no more then what is found in all Cross-staffes of what form soever. And that is, they are subject to some errorr by reason of the Eccentricity of the Ey. For the visual Beams meet within the Ey at a depth uncertain, and they are also refracted in the Superficies of the apple of the Ey: the apple of the Ey also is not of the same convexity, nor of the same breadth in all Men: and it is contracted in a bright Air, and dilated in a darker Air; as you shall soon find if you go about to observe the Diameter of the Moon by this Instrument, without correction of the Eccentricity; for you shall alwayes find the apparent Diameter too great, and much greater in the Night, then in the Day. Thus, *November 18. 1653.* I observed the Moons Diameter 32. minutes 06. seconds in the Day Time, and that Night I observed it 58. minutes, by reason of the dilatation of the apple of my Ey in the Night.

This errorr may be rectified two wayes. The First is by examining the observations made with your Cross-staff, by some other Instrument which is not subject to like errorr. As for Example, I have devised to fasten an arch of a Circle containing 20. or 30. degrees to the end of a Ruler of 6. or 7. foot, and fix to it a Label with Sights, then having observed by my Cross-staff the length of *Orions Girdle*, I will set my other Instrument to it, turning the arch toward me that I may manage the Label better, and noting the difference of the observations, I will find how to correct my Staff in that posture an another time: and so by many observations I may frame a Table to correct the Eccentricity throughout: but my Table perhaps will not serve to correct

rect the eccentricity every Mans Ey, neither will a Table made for the Night serve me in the Day.

The other way is most exact and certain for all Men. Make another Transom in all points like the first, but shorter by half, and let the divisions thereof be into half-inches: this Transom must ride upon the Index with a socket, between the long Transom and your Ey. Now when you observe, set the Sights of the short Transom to the like number of half inches as the Sights of the long Transom stand at whole inches, and when you have placed your Ey-sight so that you see the Stars upon the edges of the Sights of the long Transom, draw your short Transom till you see the Stars by his Sights in like manner at once; then look what number is cut by the short Transom, the double thereof is the Co-tangent of the angle: and look what the number cut by the Ey-sight wants of that double, so much is the Eccentricity of your Ey in that place. This way is shewed by that Excellent Mathematician Mr *Edward Wright* in Chapter 15. of his Treatise of Errors in Navigation.

FINIS.

A Catalogue of Eclipses,

Observed since the Year of our Lord 1637.

First, At *Covenree*, whose Longitude is more West then *London* 1. degree 29. minutes of space. Latitude 52. 28. minutes. My especial friends Dr *John Twysden*, and Mr *Samuel Foster*, late Professor of *Astronomy* in *Gresham College*, and my self all together, observed the totall and great Eclipse of the Moon, which hapned in the Year 1638. on Tuesday December 11. before Noon. The totall obscuration began 1. hour 07. minutes: The time of emergence observed by the Altitude of *Benemae* was 2. hours 41. minutes; so the totall Obscuration continued 1. hour 34. minutes; during the greatest part of which time the Moon was quite lost, though the Skie was clear. When the Moon began to recover light she was in the foremost foot of *Apollo*, between the two Stars of the third Magnitude: a line drawn between those Stars did cut off the lower part of the Moons body to $\frac{1}{6}$ of her Diameter, and setting the distance of the Stars in 12. parts, the Moon had gone $7\frac{1}{2}$ of those parts toward the Easterly Star: which is in *Calce Apollinis*. Hence I compute the apparent Longitude of the Moon at the time of emergence π 29. 36. minutes 19 seconds, and her apparent Latitude 0. 44. minutes South.

2. At *Easton Macodis*, whose Longitude is West from *London* 0. 43. minutes of space, that is, almost 3 minutes of Time the Latitude 52. 13. minutes, Anno Dom. 1641. upon Fryday October 8. I observed the end of the totall Eclipse of the Moon, when *Lyra* had Altitude 48. 48. minutes, that is, at 8 hours 38. minutes 08. seconds after Noon.

3. At *Elton* whose Longitude is West from *London* 45. minutes of space, or 3. minutes of Time Latitude 52. 15. minutes, Anno Dom. 1645, upon Munday August 11. I observed the Eclipse of the Sun ending when the Center of the Sun was in Azimuth 0. 55. minutes past the South, that is, 0. hours 2 $\frac{1}{2}$. minutes after Noon. This Eclipse *Hewelius* observed to end at *Danzick* at 1. hour 53. minutes, as he writes in his *Selenographia*.

Ee

4. At

4. At *Elton* aforesaid, *Anno Dom.* 1649. upon *Wednesday May 16.* before Noon: I observed in the company of *Mr Samuel Sillesby*, late *Fellow* of *Queens College* in *Cambridge*, the totall Eclipse of the Moon. The beginning when the right *Knee* of *Ophiucus* was in *Azimuth* 7. 42. minutes past South: that is, 1. hour 08. minutes *a. m.* The totall obscuration began when the *Azimuth* of the said Star was 20. degrees Westward, that is, at 1. hour 55. minutes 44. seconds. By the *Medicean* Tables it should happen to be totally obscured at *Uraniburg* 2. hours 46. minutes 23. seconds, and at *Elton* 1. 53. minutes 23. seconds. By *Lantsbergius* Tables, at *Elton* 1. hour 40. minutes 48. seconds.

5. At *Elton*, *Anno Dom.* 1649. *October 25.* current, Afternoon, I observed by a *Telescope* the Eclipse of the Sun. The Digits Eclipsed and the Time were as followeth,

Dig. H. min sec.		Dig. Hour.		6. At <i>Easton Macodit</i>	
				<i>Anno Dom.</i> 1651. on	
0. $\frac{1}{8}$	0. 41. 56.	4.	1. 47. 28.	<i>Munday March 15.</i> in the	
1.	49. 48.	3.	2. 03. 28.	Morning, I observed with	
2.	59. 44.	2.	15. 32.	<i>Dr Twysden</i> , that the Moon	
3.	— 1. 09. 44.	1.	22. 40.	was Eclipsed about one Di-	
4.	26. 12.	0.	31. 04.	git when <i>Alkair</i> was in <i>A-</i>	
4. $\frac{1}{8}$ —	33. 32.			<i>zimuth</i> 79. 40. minutes from	
the South Eastward.				More we could not see for Clouds.	

7. At *Elton Anno Dom.* 1652. on *Munday March 29.* before Noon, I observed the great Eclipse of the Sun by a *Telescope* and a minute-watch Rectified by the *Azimuth* of the Sun, taken both before and after, in the company of half a score Gentlemen and Ministers my Neighbours, as followeth.

Di. mi.	Ti. mi. sec.	Digits.	Time
0. 03. —	9. 21. 12.	11.00. — 10.35 $\frac{1}{2}$	
1. 00. —	9. 27.	10.00. — 10.42 $\frac{1}{2}$	
2. 0. —	9. 31. 08.	9.00. — 10.48 $\frac{1}{2}$	
3. 0. —	9. 37.	8.00. — 10.55.	
4. 0. —	9. 44.	7.00. — 11.01.	
5. 0. —	9. 50.	6.00. — 11.06 $\frac{1}{2}$	
6. 0. —	9. 55.	5.00. — 11.11 $\frac{1}{4}$	
7. 0. —	10. 00.	4.00. — 11.19.	
8. 0. —	10. 06 $\frac{1}{2}$	3.00. — 11.24 $\frac{1}{2}$	
9. 0. —	10. 11. 28.	2.00. — 11.31.	
10. 0. —	10. 18.	1.00. — 11.35 $\frac{1}{2}$	
11. 0. —	10. 25.	0.00. — 11.42 $\frac{1}{2}$	
11. 22 $\frac{1}{2}$ —	10. 32. 04.		

And though this Eclipse was so great, yet we could read in the

the time of the greatest darkness within Dore's, notwithstanding that the Window was covered with a Blanket.

8. At *Elton, Anno Dom. 1652.* on *Tuesday September 7.* current, the Moon rose Eclipsed about 10. Digits, and while 8. Digits were yet darkned all the dark part of the Moon was visible of a Dusk and Tawny colour: this Eclipse ended when the double Star in *Cornu* γ wanted in *Azimuth* 6. 30. minutes of the South; that is, at 7. hours 51. minutes 52. seconds: but the Moon was not free of the *Penumbra* till 7. minutes after.

9. At *Elton, Anno Dom. 1654.* on *Wednesday August 2.* current, before Noon, I observed the great Eclipse of the Sun by a *Telescope* and a Minute-watch, sufficiently Rectified by the *Azimuth* of the Sun, in the company of many learned Men my Neighbours and friends, as followeth.

Di.	T. mi.	Di.	Time.
0.	7. 47.	10 ¹	—
1.	7. 52 ¹	10.	9. 00.
2.	7. 58 ¹	9.	9. 09.
3.	8. 04.	8.	9. 18.
4.	8. 09.	7.	—
5.	8. 15.	6.	9. 31.
6.	8. 20 ³	5.	9. 38.
7.	8. 28 ⁴	4.	9. 45 ¹
8.	8. 34.	3.	9. 51 ¹
9.	8. 40 ¹	2.	—
10.	8. 49.	1.	10. 03 ¹
10 ¹	—	0.	10. 09.

10. At *Elton, Anno Dom. 1654.* on *Thursday August 17.* I observed the Eclipse of the Moon by a *Telescope* and a Minute-watch, Rectified by the *Azimuth* of the first Star in the Horn of γ , as followeth,

Time After Noon. mi.

- | | | |
|-----|-----------------|--|
| 9. | 47 ¹ | I saw the <i>Penumbra</i> invading the Moon, with my bare Ey. |
| 9. | 54. | I saw the <i>Penumbra</i> invading through my <i>Telescope</i> . |
| 10. | 15 ¹ | Shadow 3 minutes deep. |
| 10. | 25. | Shadow 4. minutes deep Yet I could discern all the <i>Limb</i> . |
| 10. | 45. | Shadow more then 4. minutes deep. Yet the Moons <i>Limb</i> all seen. |
| 11. | 05. | Yet the darkness is more on the East side: shadow is 5. minutes deep, and the <i>Limb</i> is lost in the shadow. |
| 11. | 11. | All the <i>Limb</i> seen again, and the shadow seems but 3. minutes deep, and just under |

Time After Noon mi.

- the Moon so that the East and West side of the D are darkned alike.
- II. 22. The shadow litle above 1. minute deep in my Glafs.
- II. 25. The shadow half a minute deep by my Glafs.
- II. 27. The shadow gone in my Glafs: But the *Pennumbra* still covers almost $\frac{1}{3}$ of the Moons Diameter.
- II. 30. The shadow is here gone in the judgement of my naked Ey, but the *Pennumbra* is seen still.
- II. 35. The Moon as clear as at 9. 47 $\frac{1}{2}$. but yet the lower quarter of the Moon is much darker then the rest of her body.
- II. At *Elton*, Anno Dom. 1658. upon Tuesday January 1. afternoon, I observed the Eclipse of the Moon, by a Minute-watch Rectified by the Southing of the Stars. Clouds often hindered, but thus I observed.
- Ho. mi.
6. 43 $\frac{1}{2}$ The Moon growes dusk on the East side.
- 49 $\frac{1}{2}$ More dusk, yet all the *Limb* is seen.
- 51 $\frac{1}{2}$ Here I judge the Moon to touch the *Umbra*.
- 53 $\frac{1}{2}$ The *Limb* begins to be lost in the shadow so far as I can discern both with the *Telescope* and without it.
7. 00 $\frac{1}{2}$ D darkned 2. Digits by estimation.
- 07 $\frac{1}{2}$ Almost 4. Digits.
- 34 $\frac{1}{2}$ Almost 7. Digits: here the Clouds thicken.
8. 29 $\frac{1}{2}$ D darkned about 10. Digits, yet almost all the Moon is perceivable through the shadow.
- 36 $\frac{1}{2}$ About 10. Digits, yet almost all the *Limb* perceivable.
9. 11 $\frac{1}{2}$ About 8 Digits.
- 23 $\frac{1}{2}$ About 5 $\frac{1}{2}$ Digits.
- 28 $\frac{1}{2}$ About 4. Digits.
- 39 $\frac{1}{2}$ About 3. Digits.
- 51 $\frac{1}{2}$ Here I judge the ead, The *Limb* of the D is all restored, yet the West side of the Moon looks duskyish for 3. or 4. minutes longer.
12. At *Elton*, Anno Dom. 1657. on Munday June 15. the Moon

Moon rose Eclipsed : I observed the end thereof by the *Azimuth* of *Antares*, to be 16. minutes after 10.

13. At *Elton*, *Anno Dom.* 1657. on *Thursday* *December* 10. I observed the Eclipse of the Moon ending, when she was apparently 34 degrees high, and me thought I discerned the *Penumbra* till her *Altitude* 35. it was a thick flying mist, no Star but *Jupiter* could be seen with us, all the time of this Eclipse : about one third (at the most) of the Moons Diameter was darkned on the North side. From the first *Ecliptical* opposition mentioned in this *Catalogue* to this last is the space of a *Metronique* Year.

These Observations are faithfully reported, as I made them. I could have strained some of them to a better *Harmony*; if I would have forged any thing, or used my own judgement upon them : but I rather leave them to the judgement of the learned Readers ; especially such as have accustomed themselves to *Celestial* Observations.

FINIS.

The Rudiments of *Astronomy*, Put into plain *Rhythmes*.

The Constellations of the Fixed Stars.

THe Army of the Starry Skie
Declares the Glory of God most high;
Seen and perceived of all Nations
In eight and fortie Constellations.

First neer unto the Northern Pole
The *Dragon* and two *Bears* do Role.
Whose hinder parts and Tails contain
The lesser and the greater Wain.
The *Hair*, the *Bearward*, and the *Crown*,
And then comes *Hercules* kneeling down.
And next below a place doth take
Great *Serpentarius* with his *Snake*.
Under the *Harp* of *Orpheus*
The *Eagle* and *Antinous*.

The *Silver Swan* her Wings doth spread
Above the *Dart*, and *Dolphins* head.
Then *Pegasus* comes on amain;
Andromeda followes in her Chain.
The Triangle below her stands;
And at her feet in *Perseus* hands
The *Gorgons* Head. Above are seen
Her Parents *Cepheus*, with his Queen
Cassiope. Not far below
Heniochus his *Goat* doth show
On his left shoulder: in his hand
He doth the stormy *Kids* command.

Here in the *Zodiack* begins
The *Ram*, the *Bull*, the *Loving Twins*;
The *Crab*, the *Lion*, and *Virgin* Tender,
The *Ballance*, *Scorpion*, and *Bow* bender;
Goat, *Waterman*, then *Fishes* twain
Shall bring you round to th' *Ram* again:

Fifteen Images appear
In the *Southern Hemisphere*.
The Monstrous *Whale* before the rest,
Eridanus scarce wets his breast:
Over the *Hare* *Orion* bright

Sparkles in a *Winters* night.
Then comes the great *Dog*, at whose tayl
The famous *Argo* spreads her sayl.
Above the little *Dog* doth flame,
For whom the *Latines* had no name:
Long *Hydra* on her tail alow
Carries the *Pitcher* and the *Crow*.
The *Centaur* holds the *Wolfe* by th' heel:
The *Altar*, and *Ixions* Wheel
Are never seen of us: but here
The *Southern Fish* brings up the rear,

The Planets.

Under those fixed Stars above
Seven *Planets* in their *Orbes* do move;
The high'st is *Saturn*. Thirty Year
He spends in Compassing his *Sphere*.
Twelve *Jupiter*, and *Mars* in twain
Sets forward and comes round again.
Then in one Year the *Sun* displaies
Three hundred sixty and five dayes,
And near a quarter; which in four
Encompassings makes one day more.
Between the *Sun* and us there fly
Fair *Venus*, and swift *Mercury*.
These alwayes near the *Sun* we find;
Not far before, nor far behind.
The *Moon*'s the lowest, who in seven
And twenty dayes goes round the Heaven,
And above two dayes more do run
Before she overtakes the *Sun*.
So twenty nine and an half in all
Do make a Moneth *Synodical*.

These

These Planets make their course to th' East,
Though they be faster hurled West.
And six degrees the rest may stray
Beside the Suns Ecliptique way,

The Circles of the Sphear.

Six greater Circles mark you shall
Which equally divide this Ball.
Just in the midst between the Poles
From East to West th' Equator rolles.
Th' Ecliptique cuts him; and doth slide
Scarce twenty four degrees aside.
Horizon even with the ground
From Stars below our sight doth bound.
Meridian upright doth rise,
Parting the East and Western Skies.
Two Colures through the Poles do run
Quartring the Circle of the Sun.
One where the Spring and Fall begin,
Th' other where longest dayes come in.
Four lesser Circles (mark them well)
Are to th' Equator Parallel.

Two Tropiques bound the Suns high way
Shewing the Long'st and Shortest day,
The Arctic Circle cuts the Beares,
Th' Antarctic opposite appears.
Meridians half twenty four
For Hours, and for Degrees ninescore,
Through both the Poles oth World do
And th' Equinoctial down right cross. (pass,
And ninescore Parallels hath that line
By which Stars North and South decline,
Th' Ecliptique hath his Longitudes,
And Parallels of Latitudes
For Stars: but in Geography
The Towns beside th' Equator lie.
Over our Head, and under Feet,
The ninescore Azimuths do meet.
And here as many Parallels
Of Altitude Horizon tells.
Longitudes, and Meridians all,
And Azimuths, great Circles call-
But all their Parallels in Heavens,
Being lesser, cut the Globe uneven.
Degrees three hundred and threescore
Hath every Circle and no more.

When I consider thy Heavens, the work of thy Fingers, the
Moon and the Stars which thou hast ordained,
What is Man that thou art mindfull of him? Or the
Son of Man that thou visitest him, Ps. 8.

Errata.

Some Faults have been committed between the Writer and the Printer; the cheif whereof the Reader is desired to amend as followeth.

pag. and line.	Faults	Amendments.
2, 3, 4. &c. to pag. 30. in the Title	<i>The first Book of the Fabrique of the Planisphere.</i>	<i>The first Book. Of the Fabrique of the Planisphear.</i>
31 and 32. in the Title	<i>The second Book of the Projections of the Sphear.</i>	<i>The second Book. Of the Projections of the Sphere.</i>
1. 13.	massie	massie.
2. 7. } 3. ant. }	Declination	Delineation
4. 16.	look up	look upon
4. 36.	eye beam	eye-beame
5. 13.	Euclid. 4. 5.	Euclid 4. 5.
22.	required of your Compass over reach	required. If your Compass reach short
5. 23.	if it reach short	if it over-reach
6. 39.	structures	structure
8. secant 67.	25693.	25593.
	The 5. last Tangents want a place.	You must add a Cypher to each of them.
9. 16.	two	so
12. 18.	all but	all. But
13. 07.	working it	working. It
16. 19.	four	fewer
17. 18.	Alamath	Alamach
21.	Henerichus	Heniachus.
17. antop.	little rain	little Waine
18. 8.	brow	Crowne
18. 30.	Præpe	Præpe
19. 16.	Bedalgieure	Bedalgieuze
23.	Alhaber	Alhabor.
20. 6.	round the inner circle or edge of this Ring it must	round. The inner circle or edge of this Ring must
20. 14.	naile screws	male screws
17.	finall screws	female screws
19.	bare	beare
22. 30.	is made and gon, for that year: your scale	is made. And so for that year your scale.
24. 9.	but one degree	but for one degree
25. 7.		put out the marks of Parenthesis ()
26. 8.	year Henr. 3.	year of Henr. 3.
23.	Periodas	Periodus
28.	alwayes, upon	alwayes upon
35.	thus, set	thus set
28. 1. and 5.	Graftons	Graftons

pag. and link. Faulter.
 30. 3. second Meridional
 33. 6. see for London
 33. 21. on Elevation
 34. 1. with the
 9. Azimuth
 37. 6. the eyes place
 41. 3. Center B A
 48. 4. either; way
 22. A C
 50. 16. Zenith, of
 32. Zenith and B
 53. 12. 12 and 13 number
 56. 8. these sides
 20. subtendeth A
 62. 17. fall
 63. 7, 9. wayes
 ult. of
 54. 10. min. at 70
 11. between 8 degr. 34. min.
 12. Here Refraction is as the Sun
 65. 1. your Meridians
 66. 30. require
 67. 3. Michaels
 68. 39. long
 73. 6. CHAP. II
 74. 20. } Alrucaba
 75. 8. }
 75. 12. first made
 76. 29. prick here
 81. 16, 17. by Declin.
 82. 12. her Declin.
 antep. sta
 86. 16, 17, 18, 19. Pleiades { Riset
 86. 30. to be least { setteth
 87. ἀνθρόποι
 88. 4. could happen
 14. note
 17. Afera
 91. 7. Duct.
 99. 21. 23 degrees
 102. 6. and 30. Eniph. Alph.
 23. 35 $\frac{1}{3}$
 105. 8. Stars, I
 } Ceti
 19. 120 deg.
 110. pen. by Oblique Problemes
 111. 25. in 39 $\frac{1}{2}$
 114. 17. grees setting,
 11. Houses: also

Amendments.
 second, or the Meridional
 namely for London
 no Elevation
 which the
 Azimuthes
 the eye is placed
 Center, B A
 either way;
 C A
 Zenith of
 Zenith A and B
 12th and 13th numbred
 the sides
 which subtendeth A
 falls
 rayes
 delectur
 min. and at 70
 between 18 and 24 min.
 Her Refraction is as the Sun's
 your Meridian
 enquire
 Michaels
 long
 CHAP. XI
 Alrucaba
 first made
 prick; here
 by their Declin.
 his Declin.
 Star
 Pleiades { Rise
 set
 to be lost
 ἀνθρόποι
 could not happen
 know
 Afera
 Duct.
 23^d degree
 Eniph Alph.
 36 $\frac{1}{3}$
 Stars, I
 Ceti
 125 degr.
 by Probl. 2 Obliqu.
 in all 39 $\frac{1}{2}$
 grees. Setting
 Houses also
 F f

pag. and line.

Faults,

Amendments,

31. 49. 30	50, 51
118. 6. 7. 49. 50	50, 51
24. and 50	and to
119. 1. Astrologers	Astrologia
17. <i>futurus</i>	<i>futura</i>
122. 29. no man	no men
123. 3. <i>princeps. Nere</i>	<i>princeps Nere</i>
4. <i>cithara</i>	<i>cithara</i>
10. <i>dereliquit. Nere</i>	<i>dereliquit Nere.</i>
12. <i>persuatum</i>	<i>persuatum</i>
27. <i>se nore</i>	<i>teneret</i>
128. 26. as by	and by
29. setting go	setting therefore
130. 34. Jupiter in that Meridian;	Jupiter. In that Meridian
139. 6. Christ time	Christ's time
17. <i>Ticius</i>	<i>Tacitus</i>
141. 6. 4. 5. 11.	4. 5. 11.
145. 13. Suns Dyals	Sun Dials
147. 5. or Equinoctial	deleatur
19. so the hourlines	to the hour-lines
154. in the scheme the letter I is wanting at the lower end of the hour-line of 11.	
157. 17. with an extension	with any extension
174. 32. <i>precrucem</i>	<i>per crucem</i>
176. 11. by the arch	by R T the arch
180. 9. Declination plain	declining plain
181. 20. <i>pre</i>	<i>per</i>
184. 27. the Vertical of my Dial, and also	deleatur
185. 28. and so	and to
188. 9. <i>Tumiture</i>	furniture
190. 7. you use	you may use
192. in the scheme, the prickt line last save one should be put out.	
193. <i>ant.</i> a Vertical plain	a Vertical or a South Horizontal plain
194. 27. of 10. 2	of 10 and 2
199. 11. Box-lid of a	Box-lid or of a.

Also many words are mis-written, As Cannon for Canon. Lettess for Lettess. Finitor for Finitor. Semediameter for Semidiameter, Trygonometry for Trig. *Ophiusus* for *Ophiurus*. *Plaiades* for *Pleiades*. Acronically for Acronychally. Ascendant and Descendant for Ascendent and Descendent. *Equinoctiorum* for *Equinoctiorum*. exemplification for exemplification. Dial for Dial. Ceeling for Cieling &c, which the Reader is desired to amend or overlook as also the mis-placing or omitting of points of distinction, as Comma's Colons and Periods, which I could not prevent, being so remote from the Press. Many of these mistakes are here corrected in the Table of Errata: especially the most material,

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